

Technihadrons — spectrum and collider phenomenologies

**Masafumi Kurachi
KMI, Nagoya University**

In collaboration with S. Matsuzaki and K. Yamawaki,
and K. Terashi for further collider studies

**Sakata Memorial KMI Mini-Workshop on
"Strong Coupling Gauge Theories Beyond the Standard Model"
(SCGT14Mini)**

Outline

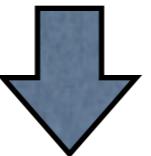
1. Introduction
2. Effective Lagrangian
3. Collider phenomenologies
4. Summary

I. Introduction

Higgs... Elementary or Composite ?

Higgs...

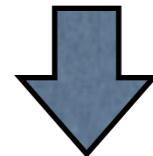
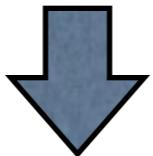
Elementary or Composite ?



Standard Model or Technicolor ?

(SM) (TC)

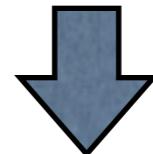
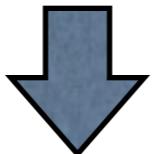
Higgs... Elementary or Composite ?



Standard Model or Technicolor ?
(SM) (TC)

Is TC an exotic model?

Higgs... Elementary or Composite ?

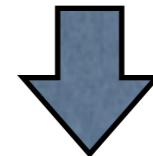
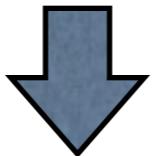


Standard Model or Technicolor ?
(SM) (TC)

Is TC an exotic model?

No, TC is based on the most **conservative** idea

Higgs... Elementary or Composite ?



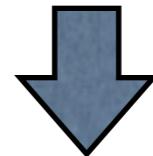
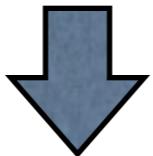
Standard Model or Technicolor ?
(SM) (TC)

Is TC an exotic model?

No, TC is based on the most **conservative** idea

It is an analogue of what actually happened in nature
(chiral symmetry breaking and confinement by QCD)

Higgs... Elementary or Composite ?



Standard Model or Technicolor ?
(SM) (TC)

Is TC an exotic model?

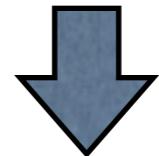
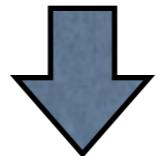
No, TC is based on the most **conservative** idea

It is an analogue of what actually happened in nature
(chiral symmetry breaking and confinement by QCD)

.....

And it is more **natural**: Higgs is a boundstate made of
techni-fermions (no fine-tuning problem)

Higgs... Elementary or Composite ?

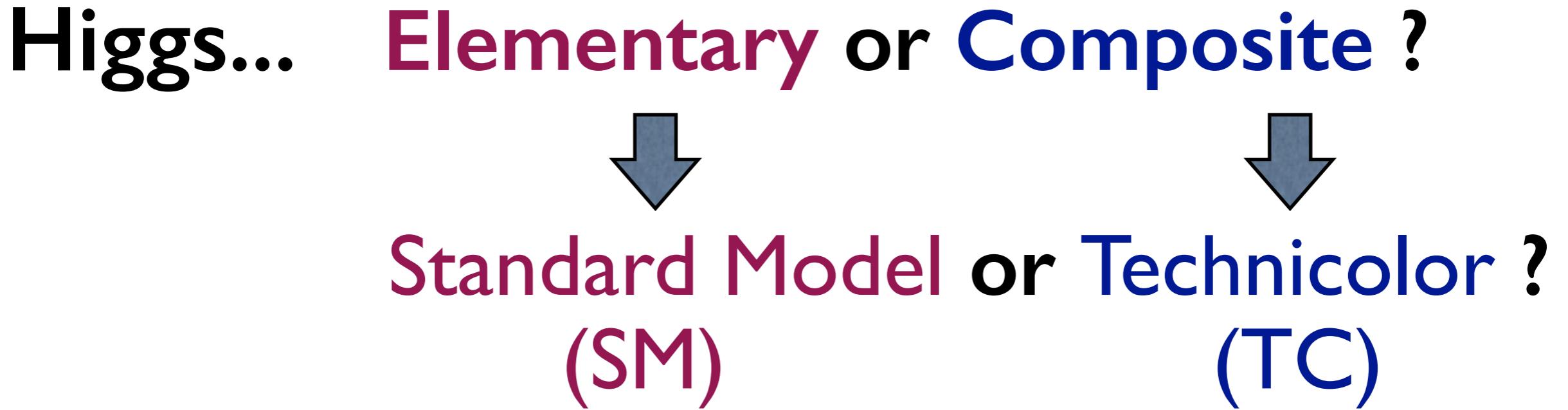


Standard Model or Technicolor ?
(SM) (TC)

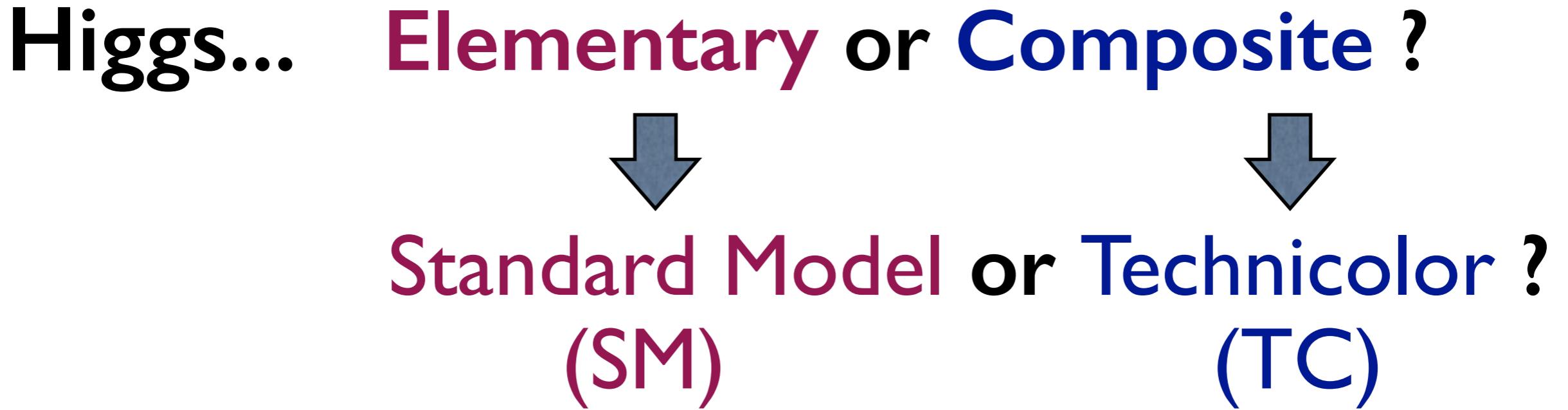
TC is interesting

- existence of the Higgs itself is related to the dynamical origin of the EWSB
- many types of techni-hadrons

(SM: just an elementary scalar + potential...)



Let's study a scenario which is
more **natural, conservative,**
and **interesting**



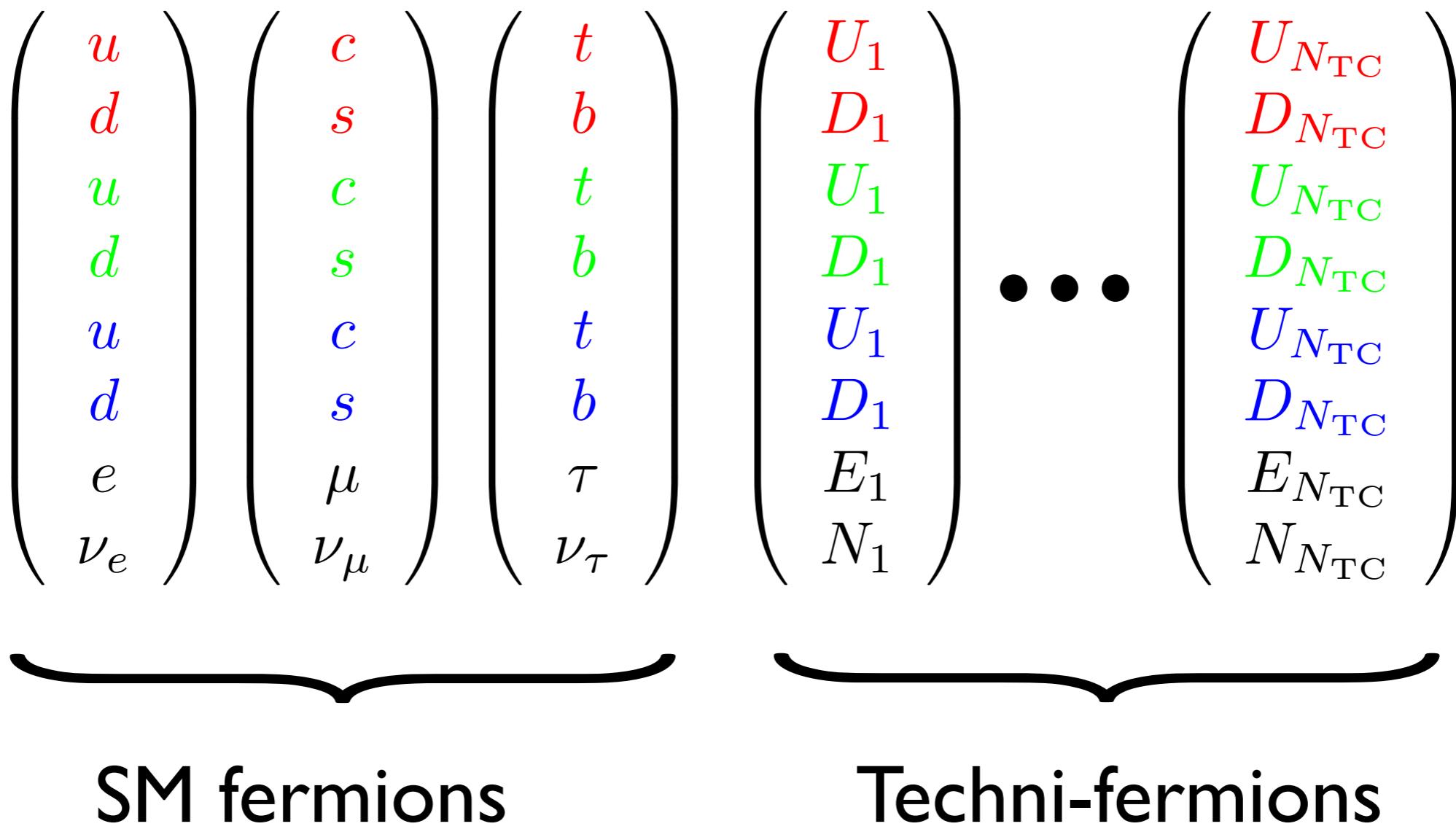
Let's study a scenario which is
more **natural, conservative,**
and **interesting**

Technicolor

What kind of Technicolor?

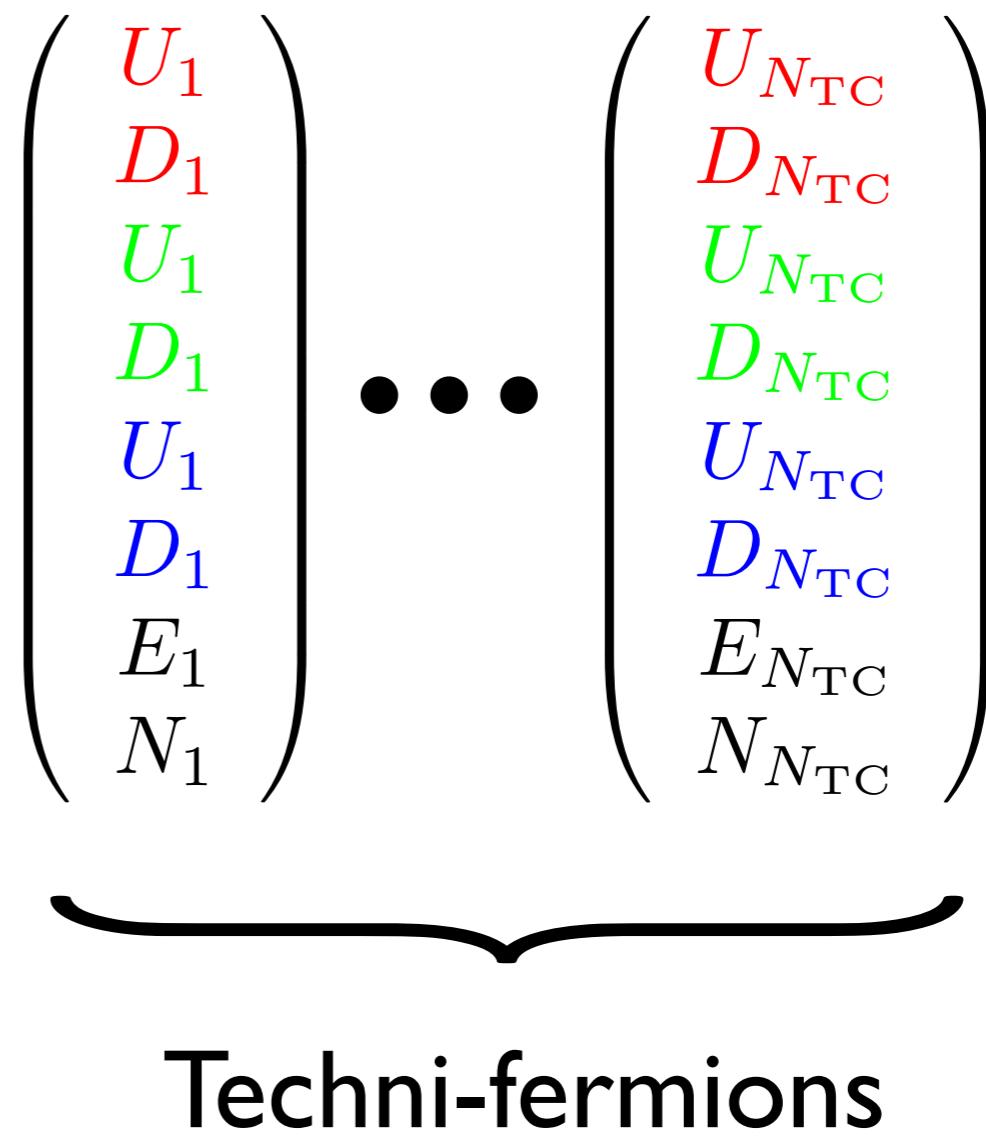
What kind of Technicolor?

One-family model (Farhi-Susskind model)



What kind of Technicolor?

$SU(N_{\text{TC}})$ gauge theory with 8 fundamental fermions

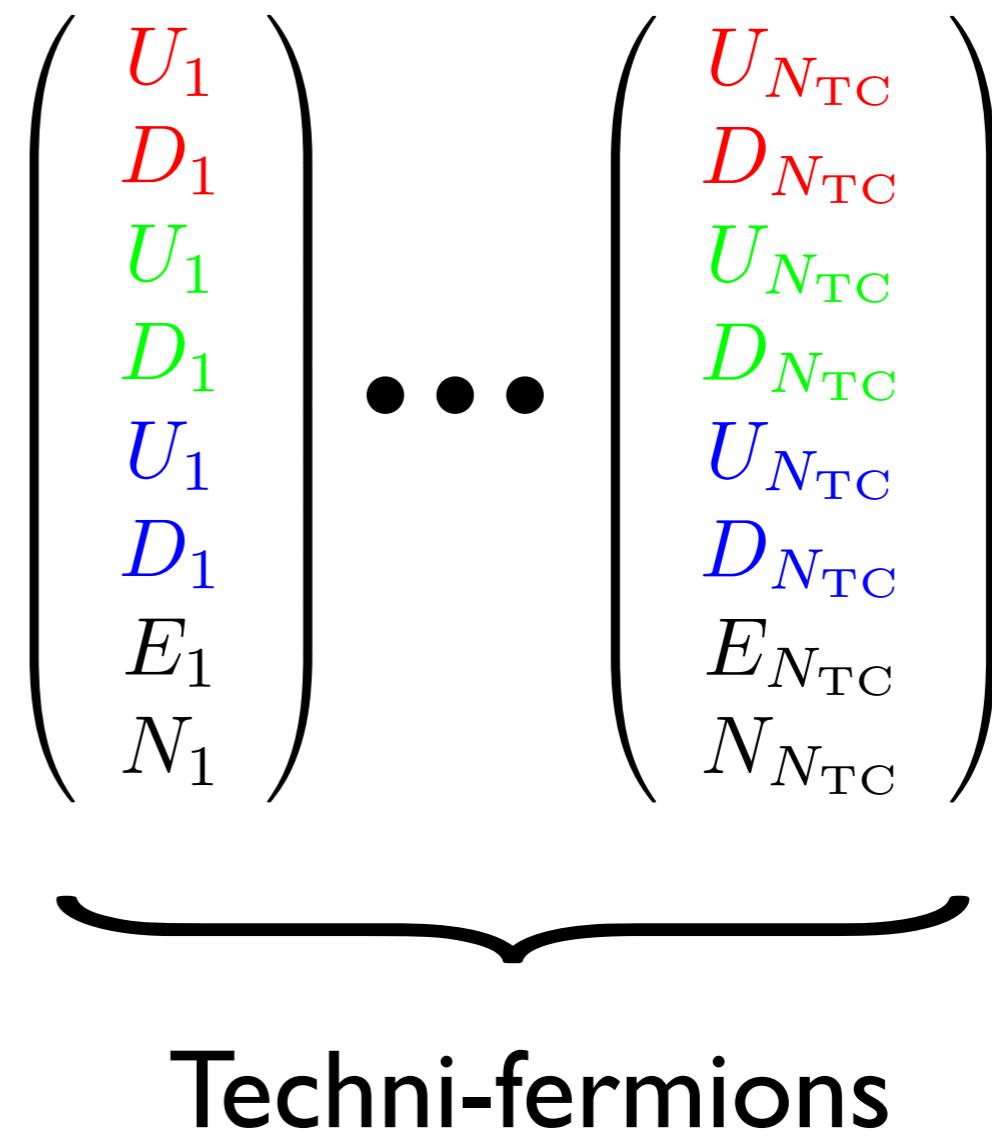


What kind of Technicolor?

$SU(N_{TC})$ gauge theory with 8 fundamental fermions

- simple model building

Farhi-Susskind (1979), Dimopoulos (1980)



What kind of Technicolor?

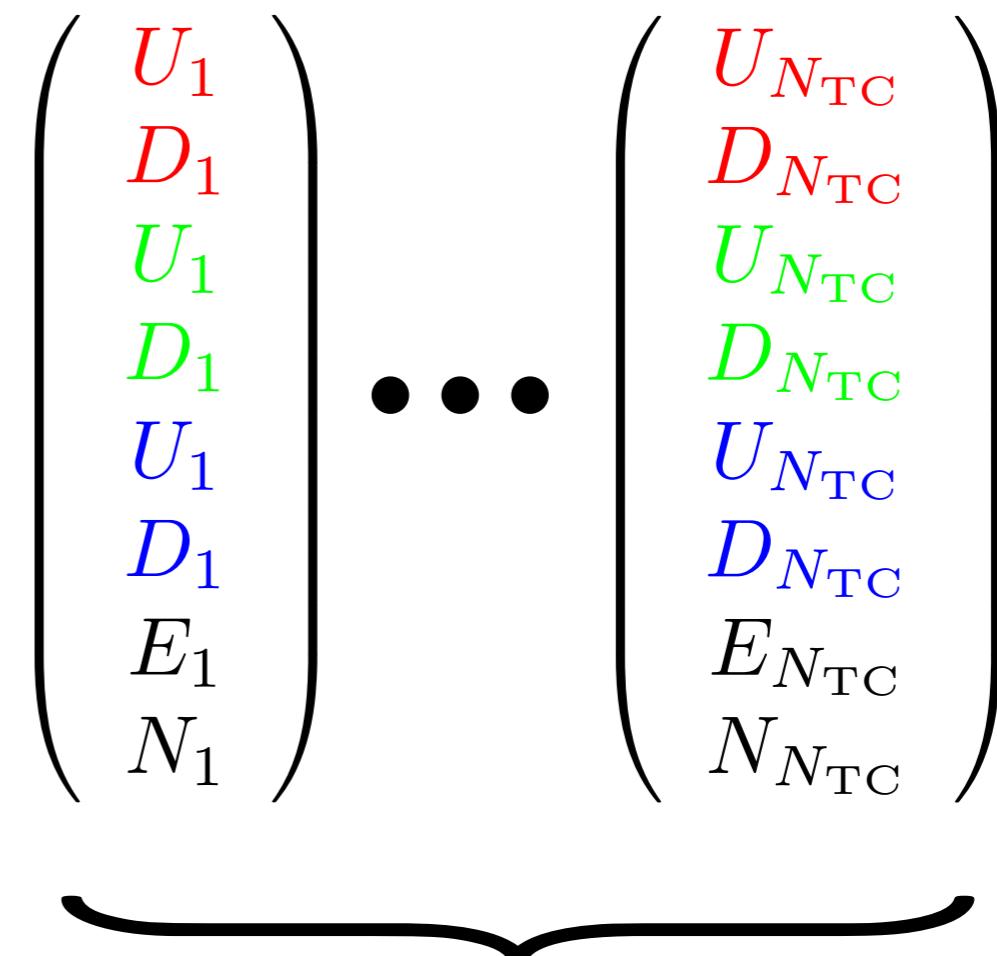
$SU(N_{TC})$ gauge theory with 8 fundamental fermions

- simple model building

Farhi-Susskind (1979), Dimopoulos (1980)

- rich spectrum of
techni-hadrons

combinations of
iso-singlet, -triplet &
color-singlet, -triplet, -octet



What kind of Technicolor?

$SU(N_{TC})$ gauge theory with 8 fundamental fermions

- simple model building

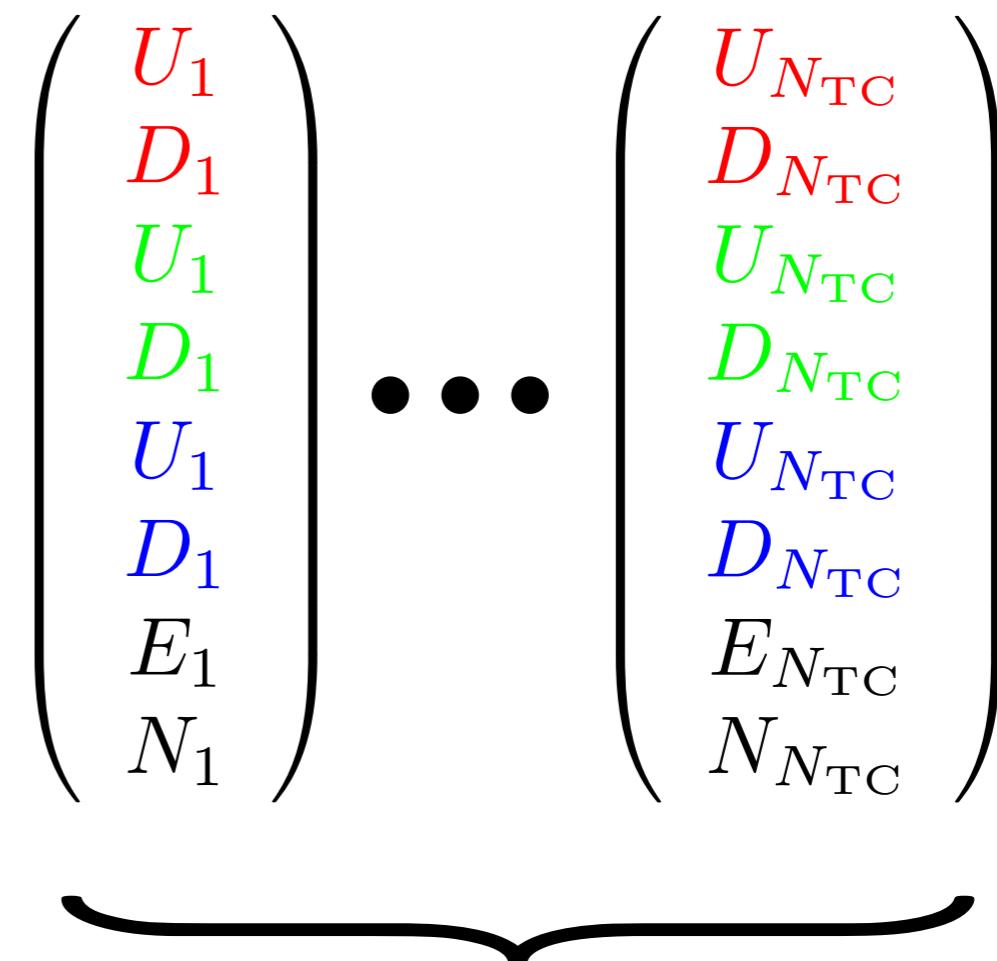
Farhi-Susskind (1979), Dimopoulos (1980)

- rich spectrum of techni-hadrons

combinations of
iso-singlet, -triplet &
color-singlet, -triplet, -octet

- candidate for Walking TC

LatKMI Collaboration (2013)



Techni-fermions

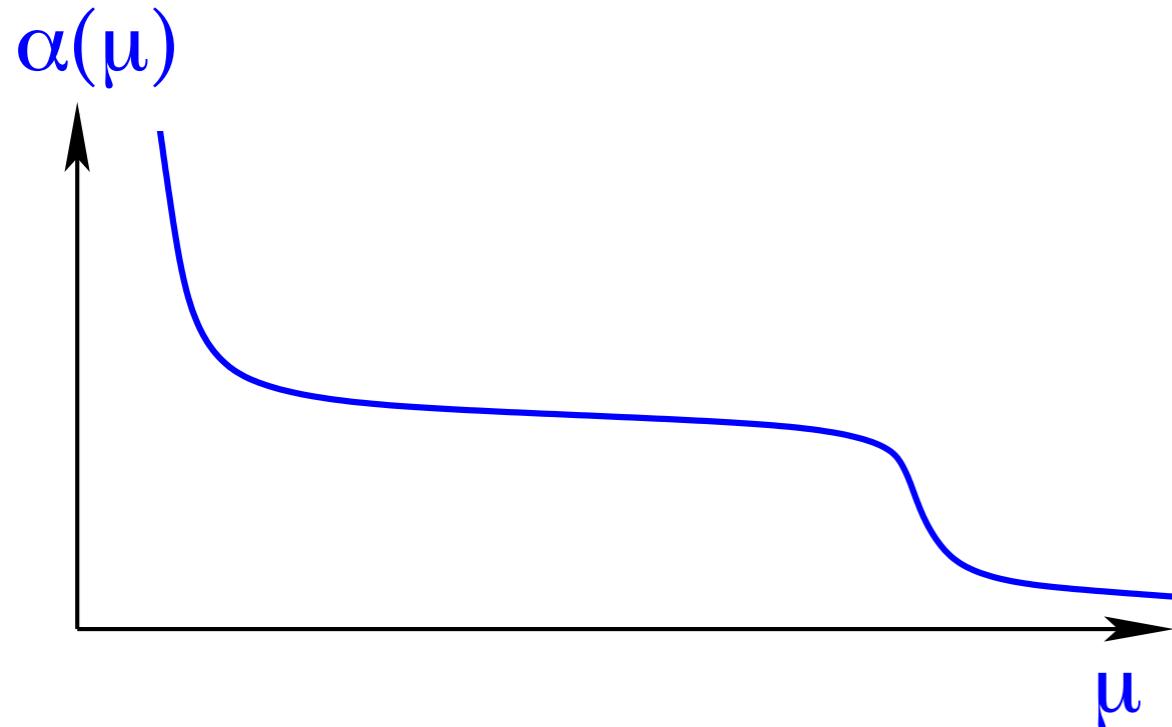
Walking Technicolor

K. Yamawaki, M. Bando, K.-i. Matumoto (1986)

Walking Technicolor

K. Yamawaki, M. Bando, K.-i. Matumoto (1986)

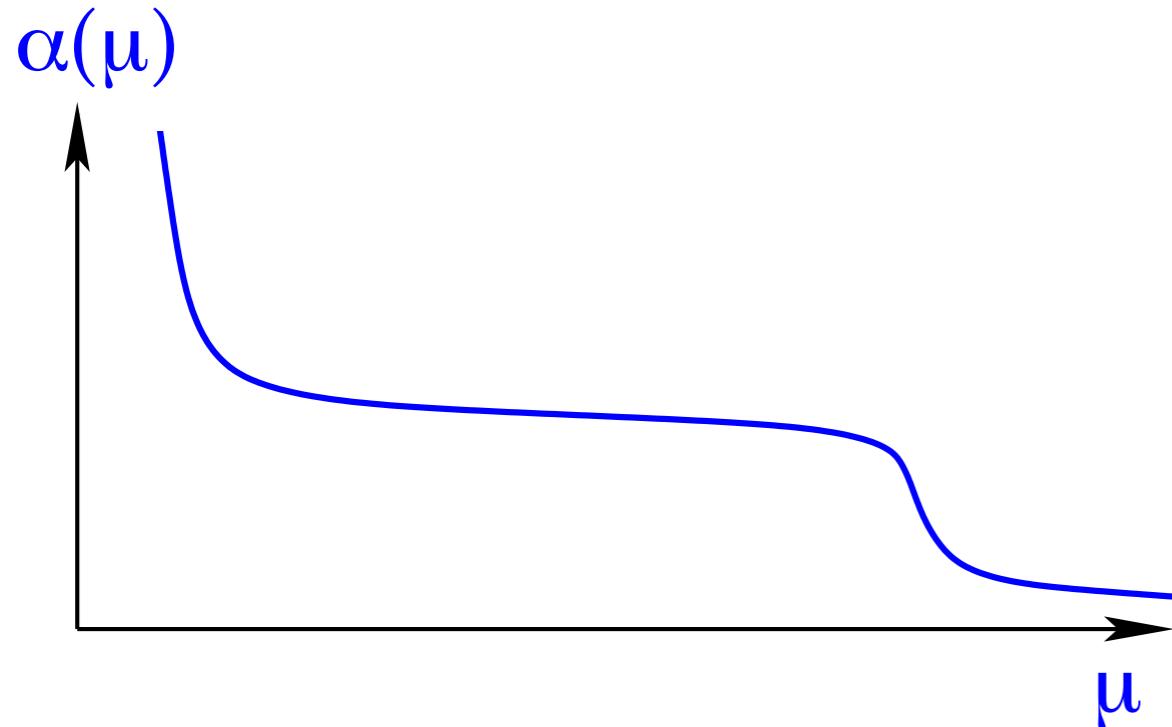
approximately scale invariant gauge theory
with large mass anomalous dimension



Walking Technicolor

K. Yamawaki, M. Bando, K.-i. Matumoto (1986)

approximately scale invariant gauge theory
with large mass anomalous dimension

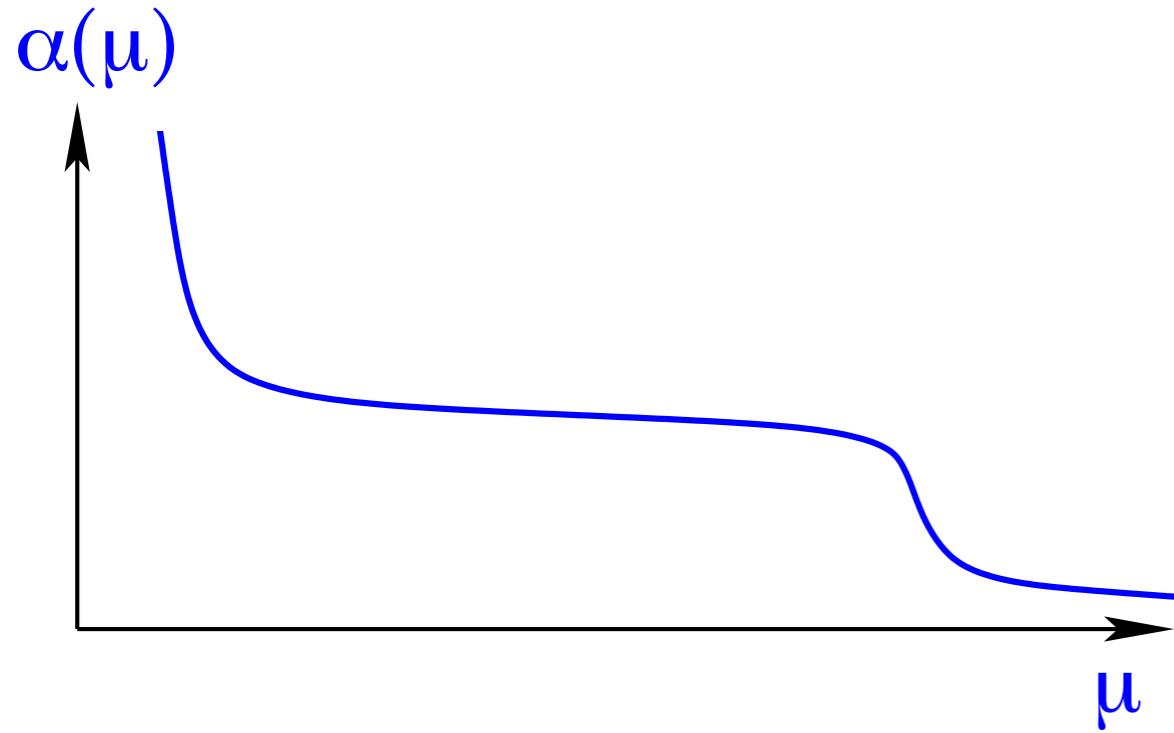


- phenomenologically favored

Walking Technicolor

K. Yamawaki, M. Bando, K.-i. Matumoto (1986)

approximately scale invariant gauge theory
with large mass anomalous dimension



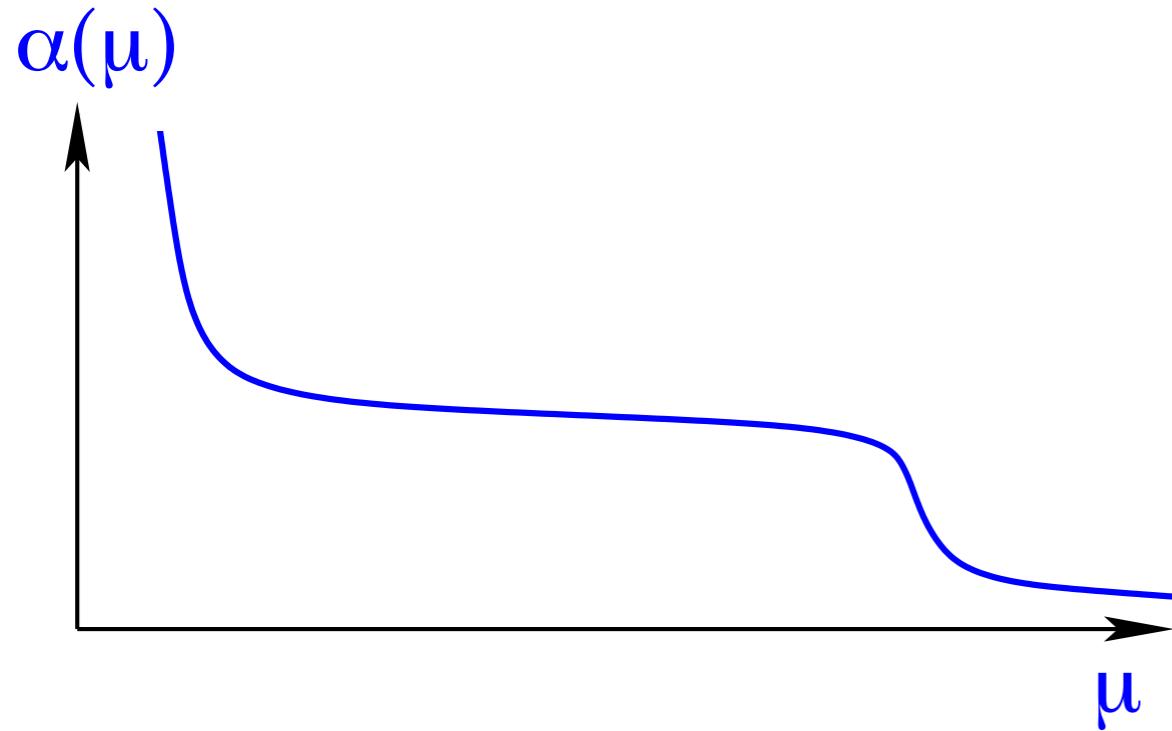
- phenomenologically favored
- existence of a light scalar boundstate (**Techni-Dilaton**)

K. Yamawaki, M. Bando, K.-i. Matumoto
(1986)

Walking Technicolor

K. Yamawaki, M. Bando, K.-i. Matumoto (1986)

approximately scale invariant gauge theory
with large mass anomalous dimension



- phenomenologically favored
- existence of a light scalar boundstate (**Techni-Dilaton**)

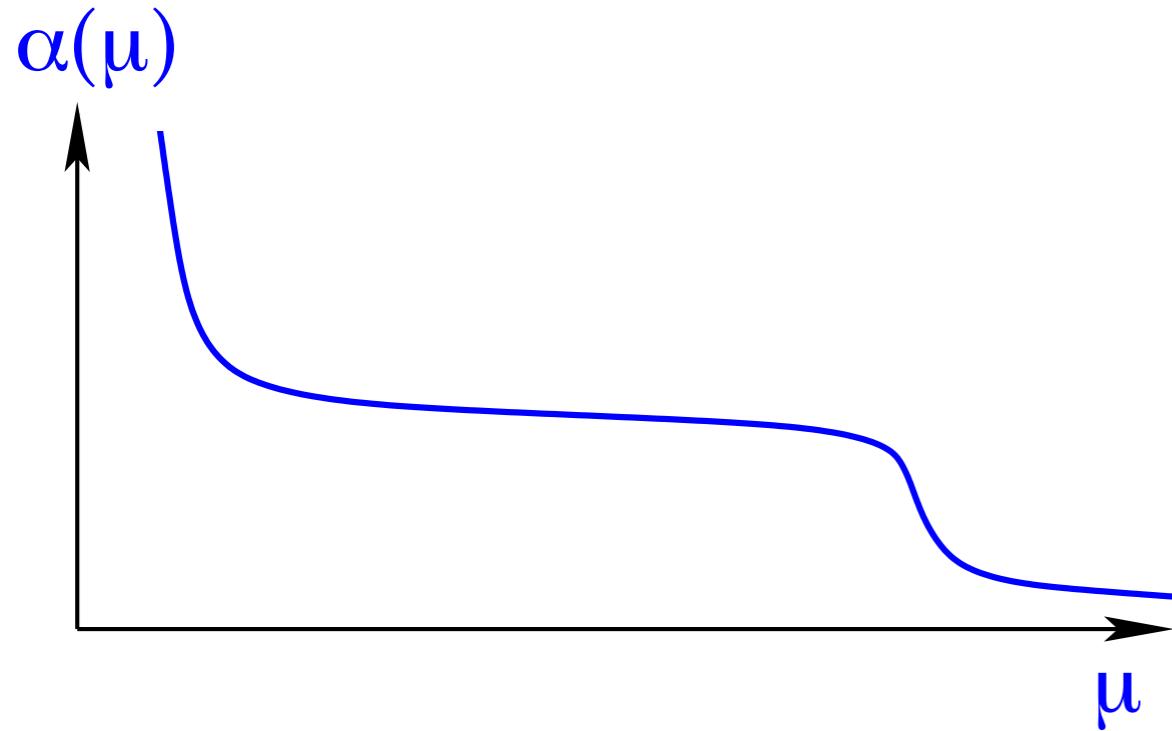
K. Yamawaki, M. Bando, K.-i. Matumoto
(1986)

Recent lattice study
(LatKMI Collaboration, 2013)
supports this idea

Walking Technicolor

K. Yamawaki, M. Bando, K.-i. Matumoto (1986)

approximately scale invariant gauge theory
with large mass anomalous dimension



- phenomenologically favored
- existence of a light scalar boundstate (Techni-Dilaton)

K. Yamawaki, M. Bando, K.-i. Matumoto (1986)

126 GeV Higgs
= Composite Higgs
= Techni-Dilaton

Recent lattice study
(LatKMI Collaboration, 2013)
supports this idea

Walking Technicolor

K. Yamawaki, M. Bando, K.-i. Matumoto (1986)

approximately scale invariant gauge theory
with large mass anomalous dimension



**What kind of signatures
can be found at the LHC?**

boundstate (Techni-Dilaton)

K. Yamawaki, M. Bando, K.-i. Matumoto
(1986)

126 GeV Higgs
= Composite Higgs
= Techni-Dilaton

Recent lattice study
(LatKMI Collaboration, 2013)
supports this idea

2. Effective Lagrangian

Low-energy spectrum

Low-energy spectrum

- Techni-Pions: NG bosons associated
with $\frac{\text{SU}(8)_L \otimes \text{SU}(8)_R}{\text{SU}(8)_V}$

Low-energy spectrum

- Techni-Pions: NG bosons associated with $\frac{\text{SU}(8)_L \otimes \text{SU}(8)_R}{\text{SU}(8)_V}$
- Techni-Dilaton: NG bosons associated with (Higgs) the scale symmetry breaking

Low-energy spectrum

- Techni-Pions: NG bosons associated with $\frac{\text{SU}(8)_L \otimes \text{SU}(8)_R}{\text{SU}(8)_V}$
- Techni-Dilaton: NG bosons associated with (Higgs) the scale symmetry breaking

We want to add something extra as typical resonances arising from strong dynamics

Low-energy spectrum

- Techni-Pions: NG bosons associated with $\frac{\text{SU}(8)_L \otimes \text{SU}(8)_R}{\text{SU}(8)_V}$
- Techni-Dilaton: NG bosons associated with (Higgs) the scale symmetry breaking
- Techni-Rho mesons: analogue of rho mesons in QCD

Techni-Pion

analogue of pions in QCD

$$\frac{\text{SU}(2)_L \otimes \text{SU}(2)_R}{\text{SU}(2)_V} \longrightarrow \begin{matrix} 3 \text{ NG bosons} \\ \pi^0, \pi^+, \pi^- \end{matrix}$$

Techni-Pion

in One-Family model

$$\frac{\text{SU}(8)_L \otimes \text{SU}(8)_R}{\text{SU}(8)_V} \longrightarrow \begin{matrix} 63 \text{ NG bosons} \\ \pi^A \quad (A = 1 \sim 63) \end{matrix}$$

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
&\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
&\quad + \sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right] + \sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]
\end{aligned}$$

$$\begin{aligned}
X_{\text{eaten}}^i &= \frac{1}{2} \left(\begin{array}{c|c} \tau^i \otimes 1_{3 \times 3} & \\ \hline & \tau^i \end{array} \right), \quad X_P^i = \frac{1}{2\sqrt{3}} \left(\begin{array}{c|c} \tau^i \otimes 1_{3 \times 3} & \\ \hline & -3 \cdot \tau^i \end{array} \right), \quad X_P = \frac{1}{4\sqrt{3}} \left(\begin{array}{c|c} 1_{6 \times 6} & \\ \hline & -3 \cdot 1_{2 \times 2} \end{array} \right), \\
X_{\theta a}^i &= \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} \tau^i \otimes \lambda_a & \\ \hline & 0 \end{array} \right), \quad X_{\theta a} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} 1_{2 \times 2} \otimes \lambda_a & \\ \hline & 0 \end{array} \right), \\
X_{Tc}^{(1)i} &= \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} \tau^i \otimes \xi_c & \\ \hline \tau^i \otimes \xi_c^\dagger & \end{array} \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} -i\tau^i \otimes \xi_c & \\ \hline i\tau^i \otimes \xi_c^\dagger & \end{array} \right), \\
X_{Tc}^{(1)} &= \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} 1_{2 \times 2} \otimes \xi_c & \\ \hline 1_{2 \times 2} \otimes \xi_c^\dagger & \end{array} \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} -i \cdot 1_{2 \times 2} \otimes \xi_c & \\ \hline i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger & \end{array} \right),
\end{aligned}$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Techni-Pion

$$\begin{aligned}
 \sum_{A=1}^{63} \pi^A(x) X^A &= \boxed{\sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i} + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
 &\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
 &\quad + \sum_{c=r,g,b} \sum_{i=1}^3 [T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i}] + \sum_{c=r,g,b} [T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)}]
 \end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\begin{array}{c|c} \tau^i \otimes 1_{3 \times 3} & \\ \hline & \tau \end{array} \right)$$

Color-singlet, Iso-triplet

$$X_{\theta a}^i = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} \tau^i \otimes \lambda_a & \\ \hline & 0 \end{array} \right)$$

$$X_{Tc}^{(1)i} = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} \tau^i \otimes \xi_c & \\ \hline \tau^i \otimes \xi_c^\dagger & \end{array} \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} -i\tau^i \otimes \xi_c & \\ \hline i\tau^i \otimes \xi_c^\dagger & \end{array} \right),$$

$$X_{Tc}^{(1)} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} 1_{2 \times 2} \otimes \xi_c & \\ \hline 1_{2 \times 2} \otimes \xi_c^\dagger & \end{array} \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} -i \cdot 1_{2 \times 2} \otimes \xi_c & \\ \hline i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger & \end{array} \right),$$

$$X_P = \frac{1}{4\sqrt{3}} \left(\begin{array}{c|c} 1_{6 \times 6} & \\ \hline -3 \cdot 1_{2 \times 2} & \end{array} \right),$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \boxed{\sum_{i=1}^3 P^i(x) X_P^i} + P^0(x) X_P \\
&\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
&\quad + \sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right] + \sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]
\end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\frac{\tau^i \otimes 1_{3 \times 3}}{\tau} \middle| \color{red} \boxed{\text{Color-singlet, Iso-triplet}} \right) \quad X_P = \frac{1}{4\sqrt{3}} \left(\frac{1_{6 \times 6}}{-3 \cdot 1_{2 \times 2}} \right),$$

$$X_{\theta a}^i = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \lambda_a}{0} \right), \quad X_{\theta a} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \lambda_a}{0} \right),$$

$$X_{Tc}^{(1)i} = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \xi_c}{\tau^i \otimes \xi_c^\dagger} \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\frac{-i\tau^i \otimes \xi_c}{i\tau^i \otimes \xi_c^\dagger} \right),$$

$$X_{Tc}^{(1)} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \xi_c}{1_{2 \times 2} \otimes \xi_c^\dagger} \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\frac{-i \cdot 1_{2 \times 2} \otimes \xi_c}{i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger} \right),$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
&\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
&\quad + \sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right] + \sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]
\end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\frac{\tau^i \otimes 1_{3 \times 3}}{\tau} \middle| \color{red} \boxed{\text{Color-singlet, Iso-singlet}} \right) \quad X_P = \frac{1}{4\sqrt{3}} \left(\frac{1_{6 \times 6}}{-3 \cdot 1_{2 \times 2}} \right),$$

$$X_{\theta a}^i = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \lambda_a}{0} \right), \quad X_{\theta a} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \lambda_a}{0} \right),$$

$$X_{Tc}^{(1)i} = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \xi_c}{\tau^i \otimes \xi_c^\dagger} \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\frac{-i\tau^i \otimes \xi_c}{i\tau^i \otimes \xi_c^\dagger} \right),$$

$$X_{Tc}^{(1)} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \xi_c}{1_{2 \times 2} \otimes \xi_c^\dagger} \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\frac{-i \cdot 1_{2 \times 2} \otimes \xi_c}{i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger} \right),$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
&\quad + \boxed{\sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i} + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
&\quad + \sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right] + \sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]
\end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\frac{\tau^i \otimes 1_{3 \times 3}}{\tau} \middle| \tau \right)$$

Color-octet, Iso-triplet

$$X_P = \frac{1}{4\sqrt{3}} \left(\frac{1_{6 \times 6}}{-3 \cdot 1_{2 \times 2}} \right),$$

$$X_{\theta a}^i = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \lambda_a}{0} \middle| 0 \right), \quad X_{\theta a} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \lambda_a}{0} \middle| 0 \right),$$

$$X_{Tc}^{(1)i} = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \xi_c}{\tau^i \otimes \xi_c^\dagger} \middle| \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\frac{-i\tau^i \otimes \xi_c}{i\tau^i \otimes \xi_c^\dagger} \middle| \right),$$

$$X_{Tc}^{(1)} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \xi_c}{1_{2 \times 2} \otimes \xi_c^\dagger} \middle| \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\frac{-i \cdot 1_{2 \times 2} \otimes \xi_c}{i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger} \middle| \right),$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
&\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \boxed{\sum_{a=1}^8 \theta_a^0(x) X_{\theta a}} \\
&\quad + \sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right] + \sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]
\end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\frac{\tau^i \otimes 1_{3 \times 3}}{\tau} \middle| \color{red} \boxed{\text{Color-octet, Iso-singlet}} \right) \quad X_P = \frac{1}{4\sqrt{3}} \left(\frac{1_{6 \times 6}}{-3 \cdot 1_{2 \times 2}} \right),$$

$$X_{\theta a}^i = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \lambda_a}{0} \middle| \right), \quad X_{\theta a} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \lambda_a}{0} \middle| \right),$$

$$X_{Tc}^{(1)i} = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \xi_c}{\tau^i \otimes \xi_c^\dagger} \middle| \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\frac{-i\tau^i \otimes \xi_c}{i\tau^i \otimes \xi_c^\dagger} \middle| \right),$$

$$X_{Tc}^{(1)} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \xi_c}{1_{2 \times 2} \otimes \xi_c^\dagger} \middle| \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\frac{-i \cdot 1_{2 \times 2} \otimes \xi_c}{i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger} \middle| \right),$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
&\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
&\quad + \boxed{\sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right]} + \sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]
\end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\begin{array}{c|c} \tau^i \otimes 1_{3 \times 3} & \\ \hline & \tau^i \end{array} \right), \quad X_P^i = \frac{1}{2\sqrt{3}} \left(\begin{array}{c|c} \tau^i \otimes 1_{3 \times 3} & \\ \hline & -3 \cdot \tau^i \end{array} \right), \quad X_P = \frac{1}{4\sqrt{3}} \left(\begin{array}{c|c} 1_{6 \times 6} & \\ \hline & -3 \cdot 1_{2 \times 2} \end{array} \right),$$

$$X_{\theta a}^i = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} \tau^i \otimes \lambda^a & \\ \hline & \lambda^a \end{array} \right)$$

$$X_{Tc}^{(1)i} = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} \tau^i \otimes \xi_c & \\ \hline \tau^i \otimes \xi_c^\dagger & \end{array} \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} -i\tau^i \otimes \xi_c & \\ \hline i\tau^i \otimes \xi_c^\dagger & \end{array} \right),$$

$$X_{Tc}^{(1)} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} 1_{2 \times 2} \otimes \xi_c & \\ \hline 1_{2 \times 2} \otimes \xi_c^\dagger & \end{array} \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} -i \cdot 1_{2 \times 2} \otimes \xi_c & \\ \hline i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger & \end{array} \right),$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Color-triplet, Iso-triplet

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
&\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
&\quad + \sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right] + \boxed{\sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]}
\end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\begin{array}{c|c} \tau^i \otimes 1_{3 \times 3} & \\ \hline & \tau^i \end{array} \right), \quad X_P^i = \frac{1}{2\sqrt{3}} \left(\begin{array}{c|c} \tau^i \otimes 1_{3 \times 3} & \\ \hline & -3 \cdot \tau^i \end{array} \right), \quad X_P = \frac{1}{4\sqrt{3}} \left(\begin{array}{c|c} 1_{6 \times 6} & \\ \hline & -3 \cdot 1_{2 \times 2} \end{array} \right),$$

$$X_{\theta a}^i = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} \tau^i \otimes \lambda_a & \\ \hline & 0 \end{array} \right), \quad X_{\theta a} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} 1_{2 \times 2} \otimes \lambda_a & \\ \hline & 0 \end{array} \right)$$

$$X_{Tc}^{(1)i} = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} \tau^i \otimes \xi_c & \\ \hline \tau^i \otimes \xi_c^\dagger & \end{array} \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\begin{array}{c|c} -i\tau^i \otimes \xi_c & \\ \hline i\tau^i \otimes \xi_c^\dagger & \end{array} \right),$$

$$X_{Tc}^{(1)} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} 1_{2 \times 2} \otimes \xi_c & \\ \hline 1_{2 \times 2} \otimes \xi_c^\dagger & \end{array} \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\begin{array}{c|c} -i \cdot 1_{2 \times 2} \otimes \xi_c & \\ \hline i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger & \end{array} \right),$$

Color-triplet, Iso-singlet

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
&\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
&\quad + \sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right] + \sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]
\end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\frac{\tau^i \otimes 1_{3 \times 3}}{\tau^i} \right), \quad X_P^i = \frac{1}{2\sqrt{3}} \left(\frac{\tau^i \otimes 1_{3 \times 3}}{-3 \cdot \tau^i} \right), \quad X_P = \frac{1}{4\sqrt{3}} \left(\frac{1_{6 \times 6}}{-3 \cdot 1_{2 \times 2}} \right),$$

$$X_{\theta a}^i = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \lambda_a}{\tau^i} \right)$$

Rich spectrum!!

$$X_{Tc}^{(1)i} = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \xi_c^\dagger}{\tau^i \otimes \xi_c^\dagger} \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \xi_c^\dagger}{i\tau^i \otimes \xi_c^\dagger} \right),$$

$$X_{Tc}^{(1)} = \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \xi_c}{1_{2 \times 2} \otimes \xi_c^\dagger} \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\frac{-i \cdot 1_{2 \times 2} \otimes \xi_c}{i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger} \right),$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Techni-Pion

$$\begin{aligned}
\sum_{A=1}^{63} \pi^A(x) X^A &= \sum_{i=1}^3 \pi_{\text{eaten}}^i(x) X_{\text{eaten}}^i + \sum_{i=1}^3 P^i(x) X_P^i + P^0(x) X_P \\
&\quad + \sum_{i=1}^3 \sum_{a=1}^8 \theta_a^i(x) X_{\theta a}^i + \sum_{a=1}^8 \theta_a^0(x) X_{\theta a} \\
&\quad + \sum_{c=r,g,b} \sum_{i=1}^3 \left[T_c^{(1)i}(x) X_{Tc}^{(1)i} + T_c^{(1)i}(x) X_{Tc}^{(2)i} \right] + \sum_{c=r,g,b} \left[T_c^{(1)}(x) X_{Tc}^{(1)} + T_c^{(1)}(x) X_{Tc}^{(2)} \right]
\end{aligned}$$

$$X_{\text{eaten}}^i = \frac{1}{2} \left(\frac{\tau^i \otimes 1_{3 \times 3}}{\tau^i} \right), \quad X_P^i = \frac{1}{2\sqrt{3}} \left(\frac{\tau^i \otimes 1_{3 \times 3}}{-3 \cdot \tau^i} \right), \quad X_P = \frac{1}{4\sqrt{3}} \left(\frac{1_{6 \times 6}}{-3 \cdot 1_{2 \times 2}} \right),$$

Similarly for Techni-Rho mesons

$$\begin{aligned}
X_{Tc}^{(1)i} &= \frac{1}{\sqrt{2}} \left(\frac{\tau^i \otimes \xi_c^\dagger}{\tau^i \otimes \xi_c^\dagger} \right), \quad X_{Tc}^{(2)i} = \frac{1}{\sqrt{2}} \left(\frac{-\tau^i \otimes \xi_c}{i\tau^i \otimes \xi_c^\dagger} \right), \\
X_{Tc}^{(1)} &= \frac{1}{2\sqrt{2}} \left(\frac{1_{2 \times 2} \otimes \xi_c}{1_{2 \times 2} \otimes \xi_c^\dagger} \right), \quad X_{Tc}^{(2)} = \frac{1}{2\sqrt{2}} \left(\frac{-i \cdot 1_{2 \times 2} \otimes \xi_c}{i \cdot 1_{2 \times 2} \otimes \xi_c^\dagger} \right),
\end{aligned}$$

τ^i : Pauli matrix, λ^a : Gell – Mann matrix

Low-energy Effective Lagrangian

Techni-Pions

Low-energy Effective Lagrangian

Techni-Pions

$$\frac{\mathrm{SU}(8)_L \otimes \mathrm{SU}(8)_R}{\mathrm{SU}(8)_V} \text{ chiral Lagrangian}$$

Low-energy Effective Lagrangian

Techni-Pions

$$\frac{\text{SU}(8)_L \otimes \text{SU}(8)_R}{\text{SU}(8)_V} \text{ chiral Lagrangian}$$

$$\mathcal{L} = F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

$$\hat{\alpha}_{\mu\perp} = \frac{(D_\mu \xi_R) \xi_R^\dagger - (D_\mu \xi_L) \xi_L^\dagger}{2i}$$

$$D_\mu \xi_L = \partial_\mu \xi_L + i \xi_L \mathcal{L}_\mu$$

$$D_\mu \xi_R = \partial_\mu \xi_R + i \xi_R \mathcal{R}_\mu$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F_\pi}}, \quad \pi = \pi^A X^A$$

SM gauge fields

Techni-Pions

Low-energy Effective Lagrangian

Techni-Pions

$$\frac{\text{SU}(8)_L \otimes \text{SU}(8)_R}{\text{SU}(8)_V} \text{ chiral Lagrangian}$$

$$\mathcal{L} = F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

$$\hat{\alpha}_{\mu\perp} = \frac{(D_\mu \xi_L)}{2i}$$

Techni-Pions obtain
their masses from
explicit breaking effects

J. Jia, S. Matsuzaki, K. Yamawaki (2012)

$$D_\mu \xi_L = \partial_\mu \xi_L + i \xi_L \mathcal{L}_\mu$$

$$D_\mu \xi_R = \partial_\mu \xi_R + i \xi_R \mathcal{R}_\mu$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F_\pi}}, \quad \pi = \pi^A X^A$$

SM gauge fields

Techni-Pions

Low-energy Effective Lagrangian

Techni-Pions

$$\frac{\text{SU}(8)_L \otimes \text{SU}(8)_R}{\text{SU}(8)_V} \text{ chiral Lagrangian}$$

$$\mathcal{L} = F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

Holographic estimate shows
Techni-pions are rather heavy:

$$m_\pi > O(1) \text{ TeV}$$

$$\hat{\alpha}_{\mu\perp} = -\frac{M_K, S. Matsuzaki, K. Yamawaki, arXiv:1403.0467}{2i}$$

$$D_\mu \xi_L = \partial_\mu \xi_L + i \xi_L \mathcal{L}_\mu$$

$$D_\mu \xi_R = \partial_\mu \xi_R + i \xi_R \mathcal{R}_\mu$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F_\pi}}, \quad \pi = \pi^A X^A$$

SM gauge fields

Techni-Pions

Low-energy Effective Lagrangian

Techni-Pions + Techni-Dilaton
(Composite Higgs)

$$\mathcal{L} = F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

$$\hat{\alpha}_{\mu\perp} = \frac{(D_\mu \xi_R) \xi_R^\dagger - (D_\mu \xi_L) \xi_L^\dagger}{2i}$$

$$D_\mu \xi_L = \partial_\mu \xi_L + i \xi_L \mathcal{L}_\mu$$

$$D_\mu \xi_R = \partial_\mu \xi_R + i \xi_R \mathcal{R}_\mu$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F_\pi}}, \quad \pi = \pi^A X^A$$

Low-energy Effective Lagrangian

Techni-Pions + Techni-Dilaton
(Composite Higgs)
requiring scale invariance

$$\mathcal{L} = F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

$$\hat{\alpha}_{\mu\perp} = \frac{(D_\mu \xi_R) \xi_R^\dagger - (D_\mu \xi_L) \xi_L^\dagger}{2i}$$

$$D_\mu \xi_L = \partial_\mu \xi_L + i \xi_L \mathcal{L}_\mu$$

$$D_\mu \xi_R = \partial_\mu \xi_R + i \xi_R \mathcal{R}_\mu$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F_\pi}}, \quad \pi = \pi^A X^A$$

Low-energy Effective Lagrangian

Higgs

$$\chi = e^{\frac{\phi}{F\phi}}$$

Techni-Pions + Techni-Dilaton
(Composite Higgs)

requiring scale invariance

$$\mathcal{L} = \boxed{\chi^2} - F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

$$\hat{\alpha}_{\mu\perp} = \frac{(D_\mu \xi_R) \xi_R^\dagger - (D_\mu \xi_L) \xi_L^\dagger}{2i}$$

$$D_\mu \xi_L = \partial_\mu \xi_L + i \xi_L \mathcal{L}_\mu$$

$$D_\mu \xi_R = \partial_\mu \xi_R + i \xi_R \mathcal{R}_\mu$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F\pi}}, \quad \pi = \pi^A X^A$$

Low-energy Effective Lagrangian

Higgs

Techni-Pions + Techni-Dilaton
(Composite Higgs)

requiring scale invariance

$$\chi = e^{\frac{\phi}{F\phi}}$$

$$\mathcal{L} = \boxed{\chi^2} F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

Consistent with LHC data

S. Matsuzaki, K. Yamawaki (2012), (2013)

$$\hat{\alpha}_{\mu\perp} = \frac{(E)}{F_\phi}$$

Best fit: $\frac{v_{\text{EW}}}{F_\phi} = 0.22$ (for $N_{\text{TC}} = 4$)

$$D_\mu \xi_L = \partial_\mu \xi_L + i \xi_L \mathcal{L}_\mu$$

$$D_\mu \xi_R = \partial_\mu \xi_R + i \xi_R \mathcal{R}_\mu$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F\pi}}, \quad \pi = \pi^A X^A$$

Low-energy Effective Lagrangian

Higgs

Techni-Pions + Techni-Dilaton
(Composite Higgs)

requiring scale invariance

$$\chi = e^{\frac{\phi}{F\phi}}$$

$$\mathcal{L} = \boxed{\chi^2} F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

Consistent with LHC data

S. Matsuzaki, K. Yamawaki (2012), (2013)

$$\hat{\alpha}_{\mu\perp} = \frac{(E)}{F_\phi}$$

Best fit: $\frac{v_{\text{EW}}}{F_\phi} = 0.22$ (for $N_{\text{TC}} = 4$)

$$D_\mu \xi_L = \partial_\mu \xi_L$$

More details in the talk
by S. Matsuzaki

$$D_\mu \xi_R = \partial_\mu \xi_R$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F\pi}}, \quad \pi = \pi^A X^A$$

Low-energy Effective Lagrangian

Techni-Pions + Techni-Dilaton

+ Techni-Rho mesons
(Hidden Local Symmetry)

$$\chi = e^{\frac{\phi}{F\phi}}$$

$$\mathcal{L} = \chi^2 - F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2]$$

$$\hat{\alpha}_{\mu\perp} = \frac{(D_\mu \xi_R) \xi_R^\dagger - (D_\mu \xi_L) \xi_L^\dagger}{2i}$$

$$D_\mu \xi_L = \partial_\mu \xi_L + i \xi_L \mathcal{L}_\mu$$

$$D_\mu \xi_R = \partial_\mu \xi_R + i \xi_R \mathcal{R}_\mu$$

$$\xi_{L,R} = e^{\mp \frac{i\pi}{F\pi}}, \quad \pi = \pi^A X^A$$

Low-energy Effective Lagrangian

Techni-Pions + Techni-Dilaton

+ Techni-Rho mesons
(Hidden Local Symmetry)

$$\chi = e^{\frac{\phi}{F\phi}}$$

$$\mathcal{L} = \chi^2 \left(F_\pi^2 \text{tr}[\hat{\alpha}_{\mu\perp}^2] + F_\sigma^2 \text{tr}[\hat{\alpha}_{\mu\parallel}^2] \right) - \frac{1}{2g^2} \text{tr} [V_{\mu\nu}^2]$$

$$\hat{\alpha}_{\mu\perp,\parallel} = \frac{(D_\mu\xi_R)\xi_R^\dagger \mp (D_\mu\xi_L)\xi_L^\dagger}{2i}$$

$$D_\mu\xi_L = \partial_\mu\xi_L + i\xi_L \mathcal{L}_\mu - iV_\mu\xi_L^\dagger$$

$$D_\mu\xi_R = \partial_\mu\xi_R + i\xi_R \mathcal{R}_\mu - iV_\mu\xi_R^\dagger$$

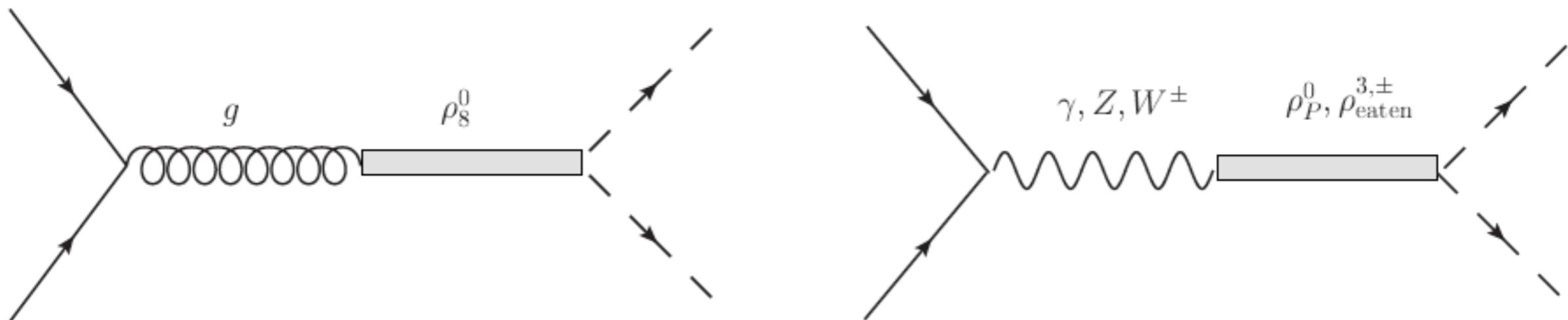
Techni-Rho
mesons

$$\xi_{L,R} = e^{\frac{i\sigma}{F\sigma}} e^{\mp\frac{i\pi}{F\pi}}, \quad \pi = \pi^A X^A, \quad \sigma = \sigma^A X^A$$

3. Collider phenomenology

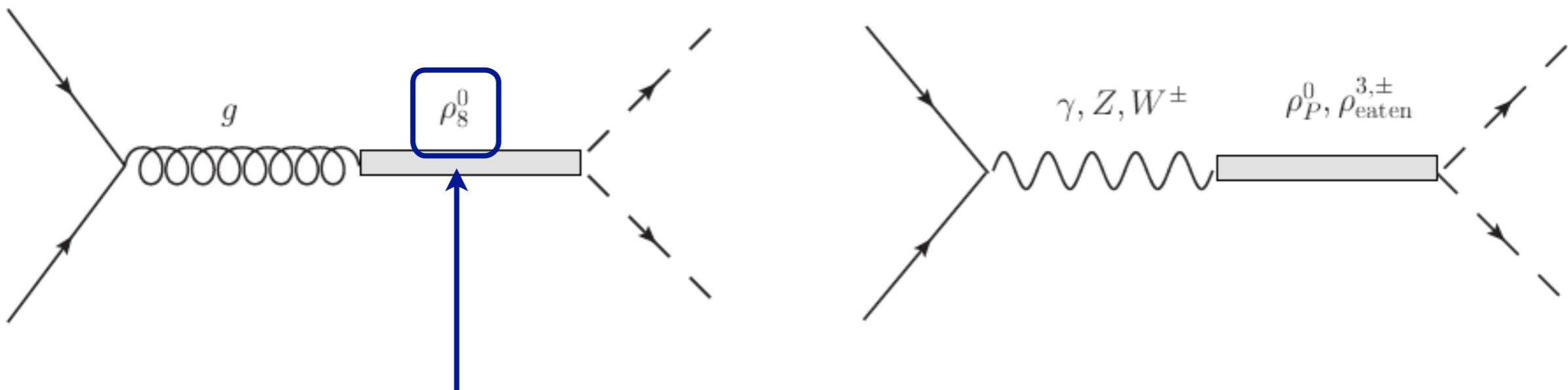
Techni-Rho productions

Ones that mix with SM gauge bosons are produced through the Drell-Yan process



Techni-Rho productions

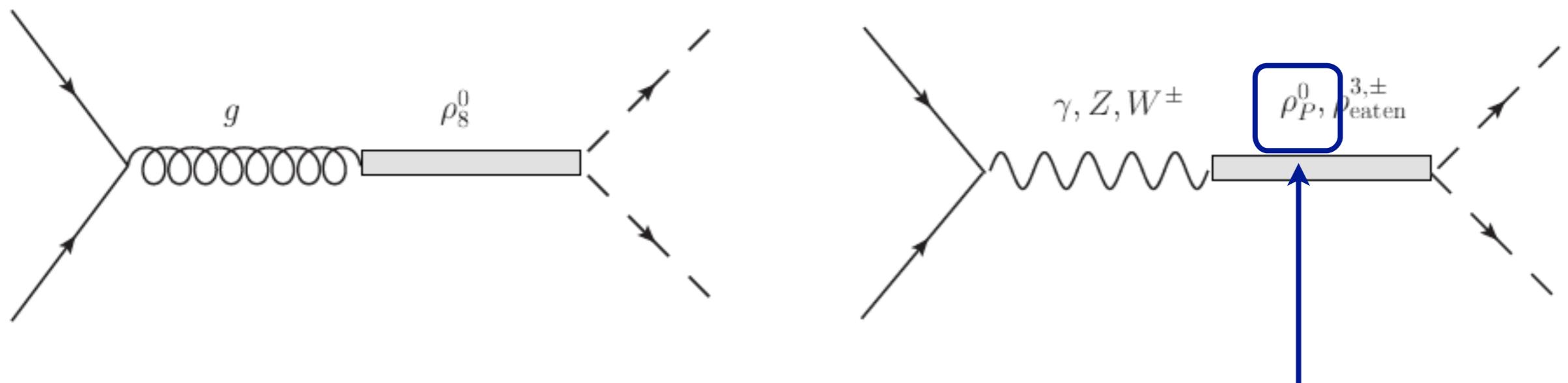
Ones that mix with SM gauge bosons are produced through the Drell-Yan process



Color-octet, Iso-singlet
Techni-Rho meson

Techni-Rho productions

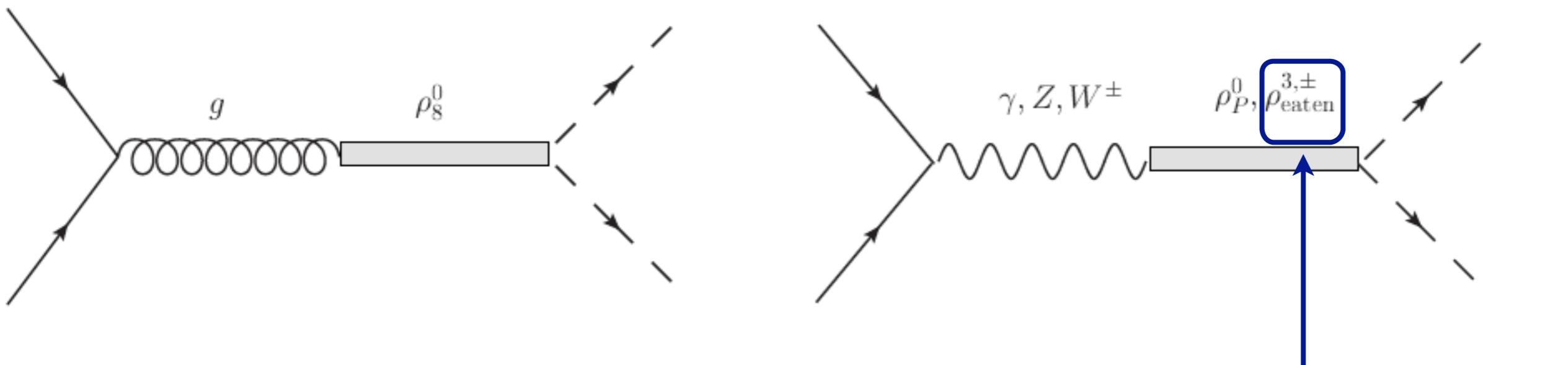
Ones that mix with SM gauge bosons are produced through the Drell-Yan process



Color-singlet, Iso-singlet
Techni-Rho meson

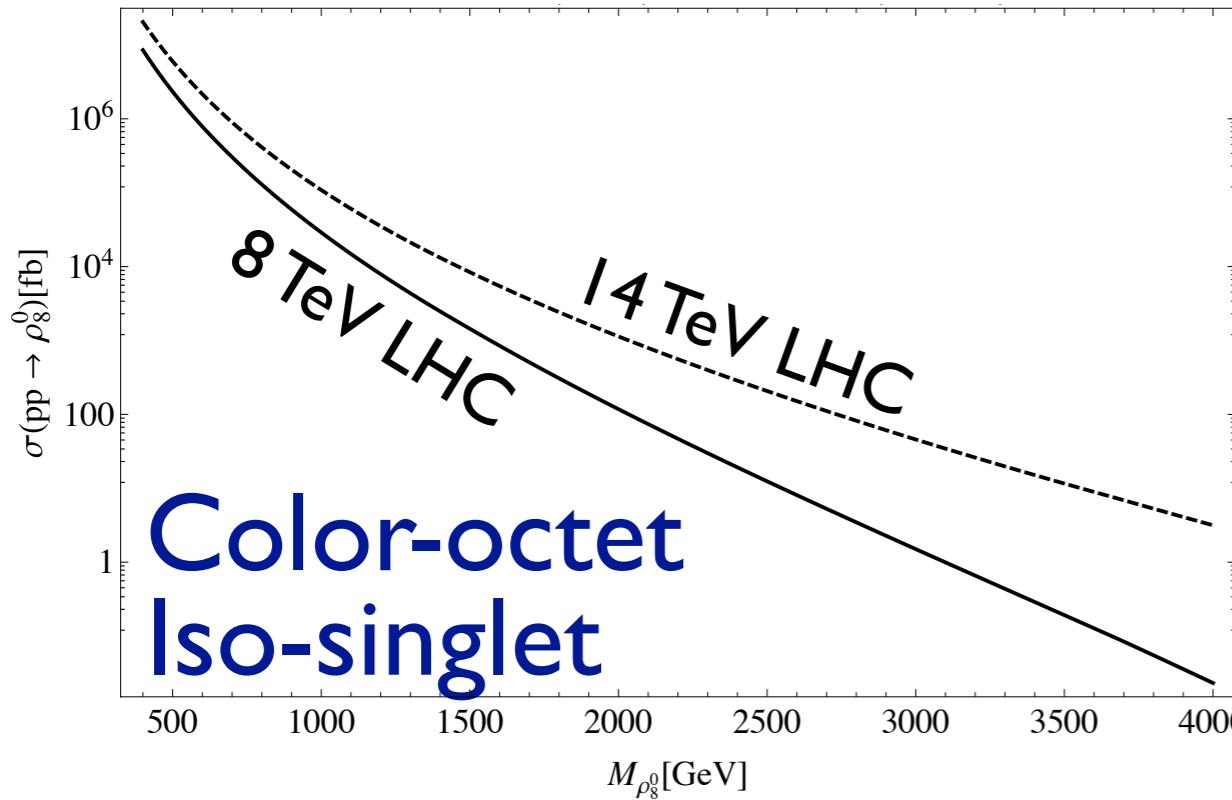
Techni-Rho productions

Ones that mix with SM gauge bosons are produced through the Drell-Yan process

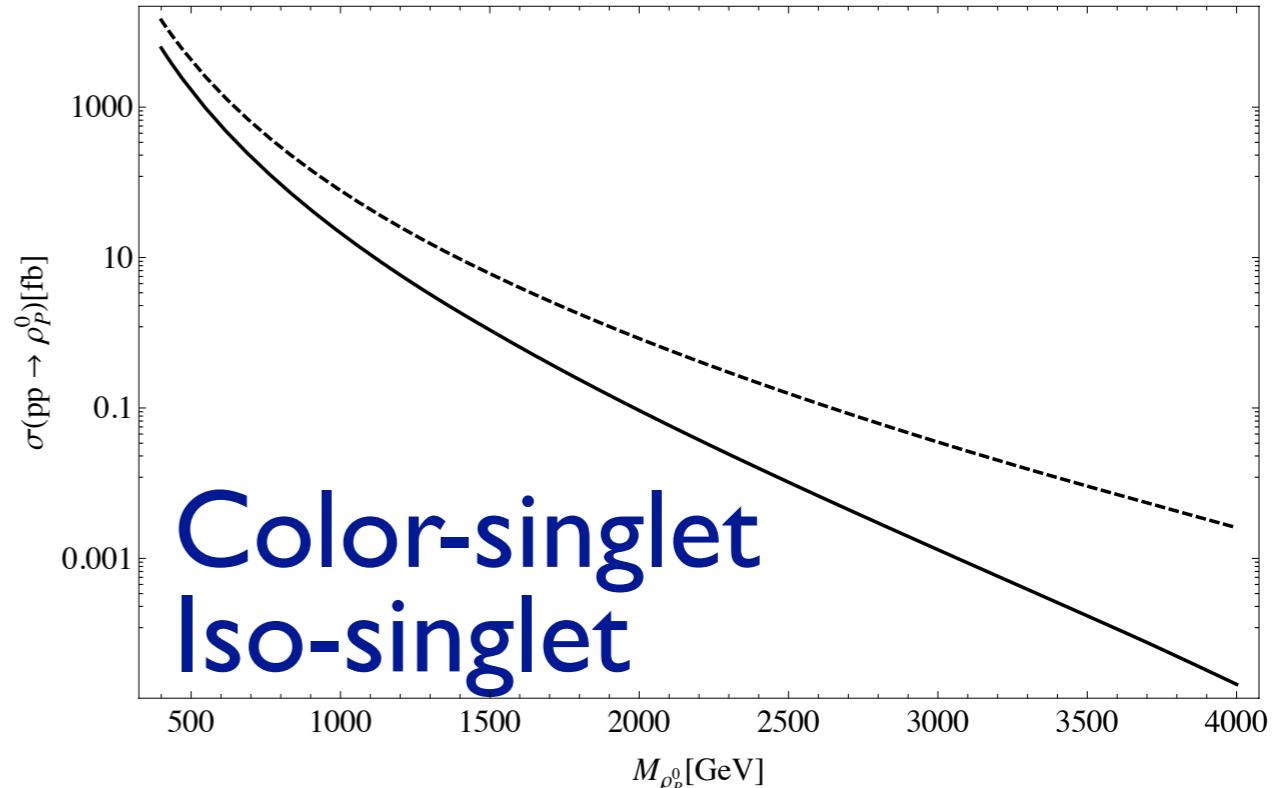


Color-singlet, Iso-triplet
Techni-Rho meson

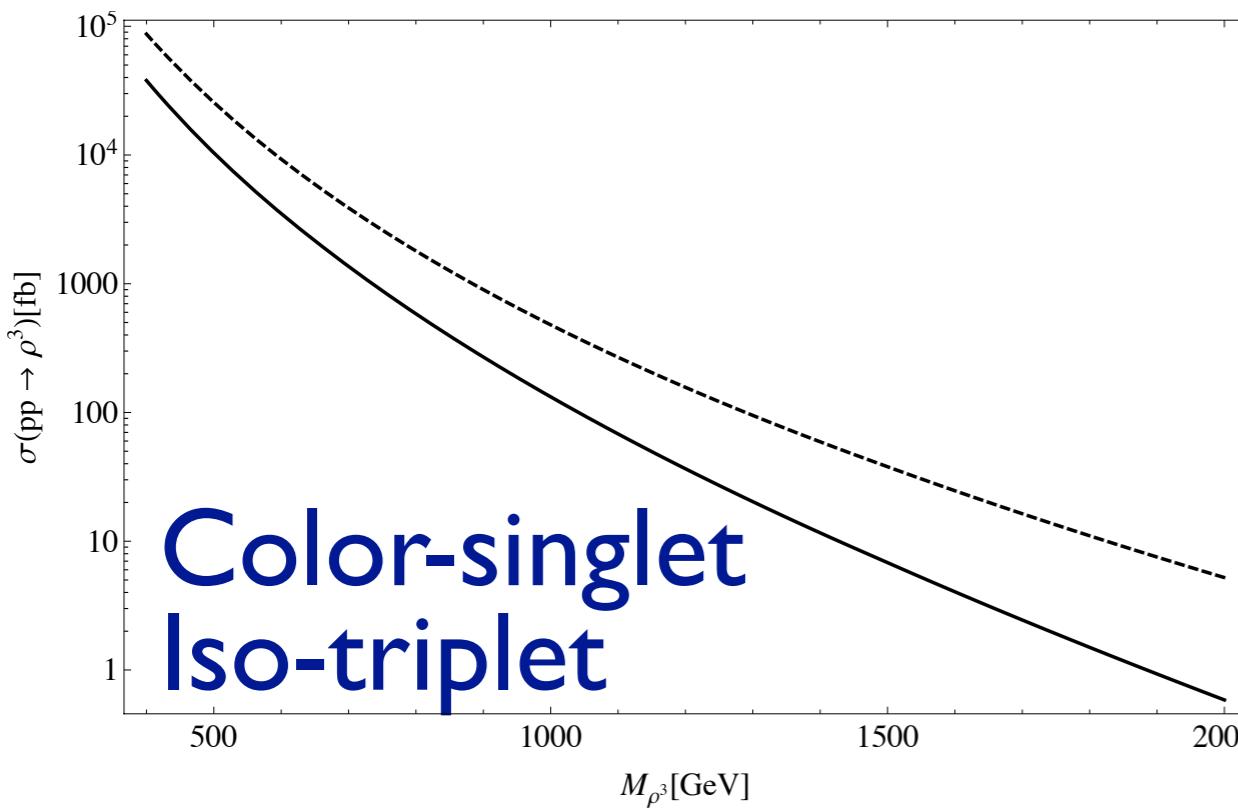
Techni-Rho productions cross section



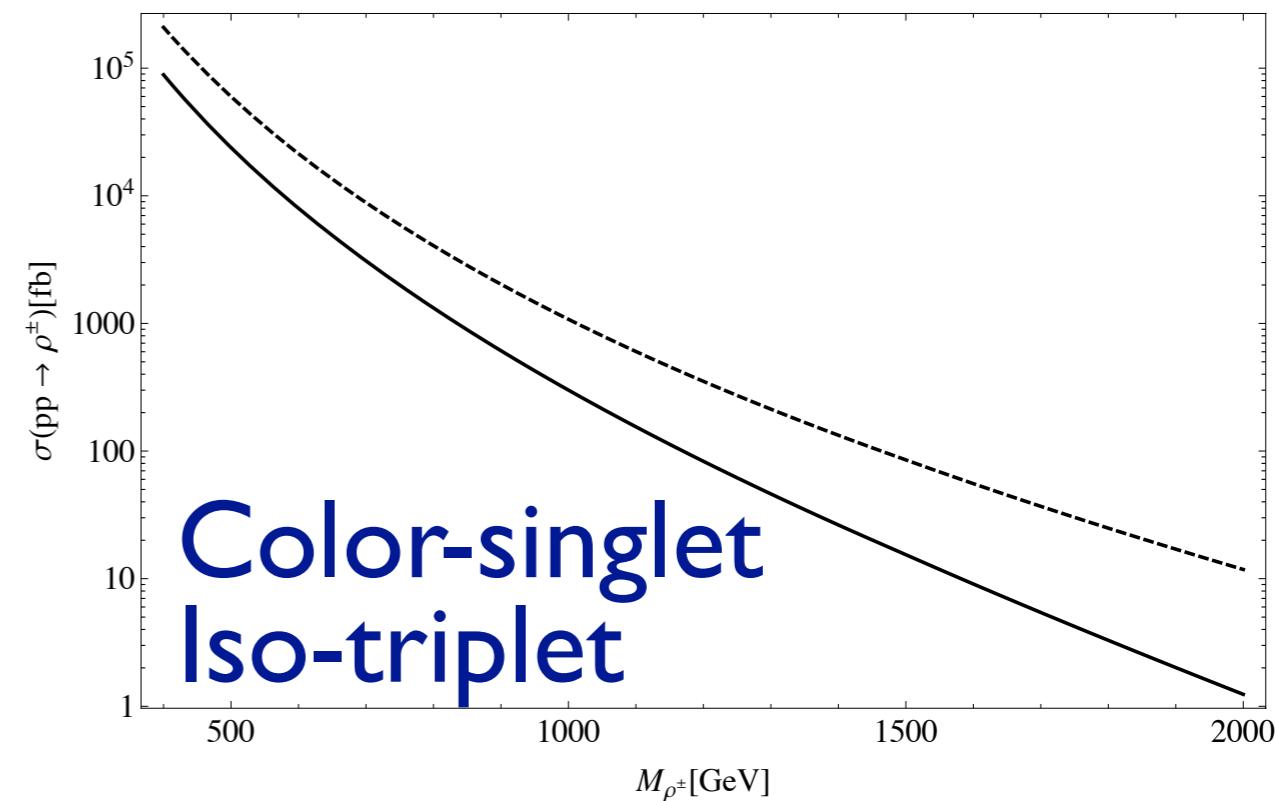
Color-octet
Iso-singlet



Color-singlet
Iso-singlet



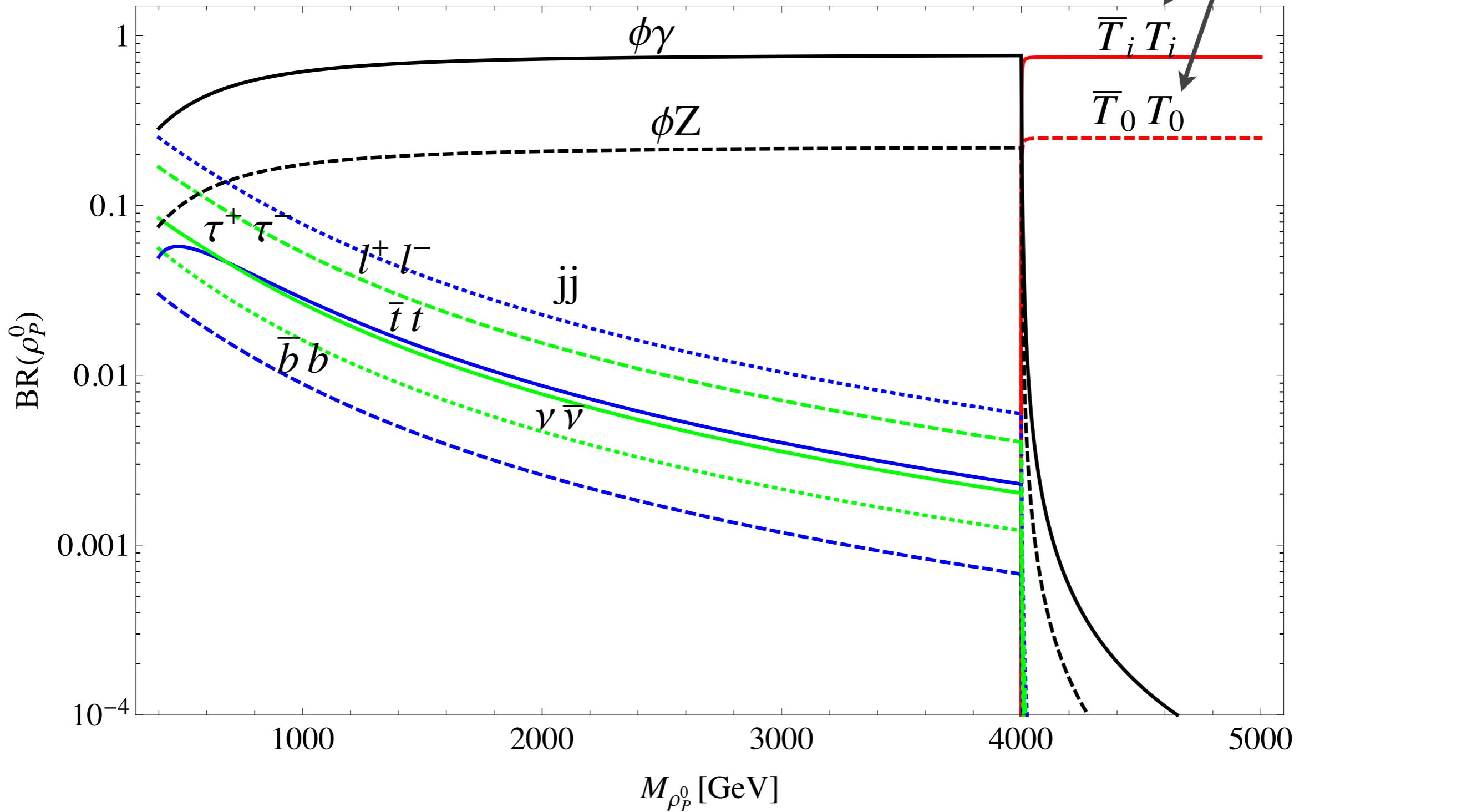
Color-singlet
Iso-triplet



Color-singlet
Iso-triplet

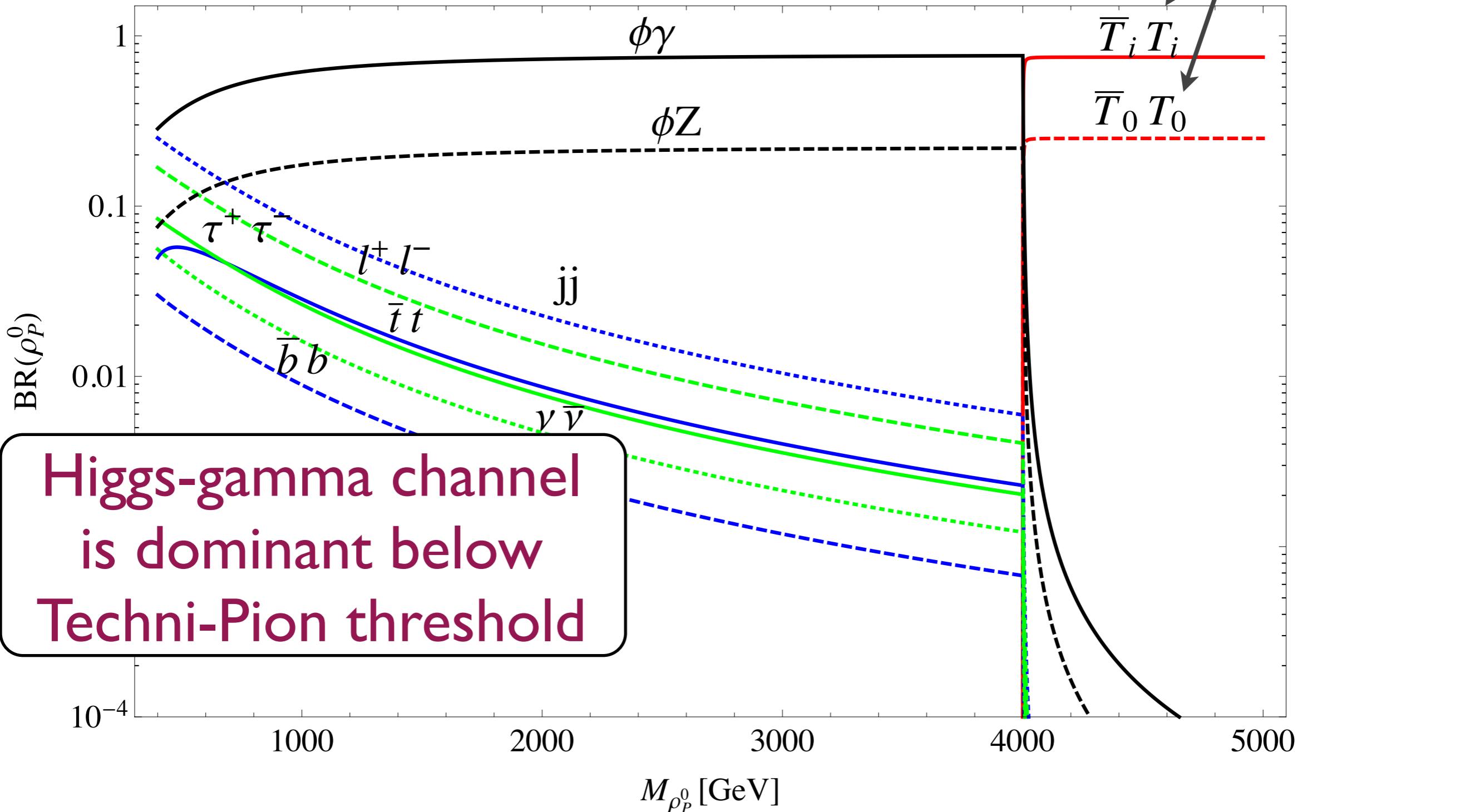
ρ_P^0

Color-singlet Iso-singlet

Branching ratio

ρ_P^0

Color-singlet Iso-singlet

Branching ratio

ρ_P^0

Color-singlet Iso-singlet

Branching ratio

Constraint from LHC?

$Z' \rightarrow \ell^+ \ell^-$ search would

ATLAS-CONF-2013-017, CMS-PAS-EXO-12-061

constrain ρ_P^0 mass to be

$$M_{\rho_P^0} > 1.3 \text{ TeV}$$

$\text{BR}(\rho_P^0)$

0.01

Higgs-gamma channel
is dominant below
Techni-Pion threshold

10^{-4}

1000

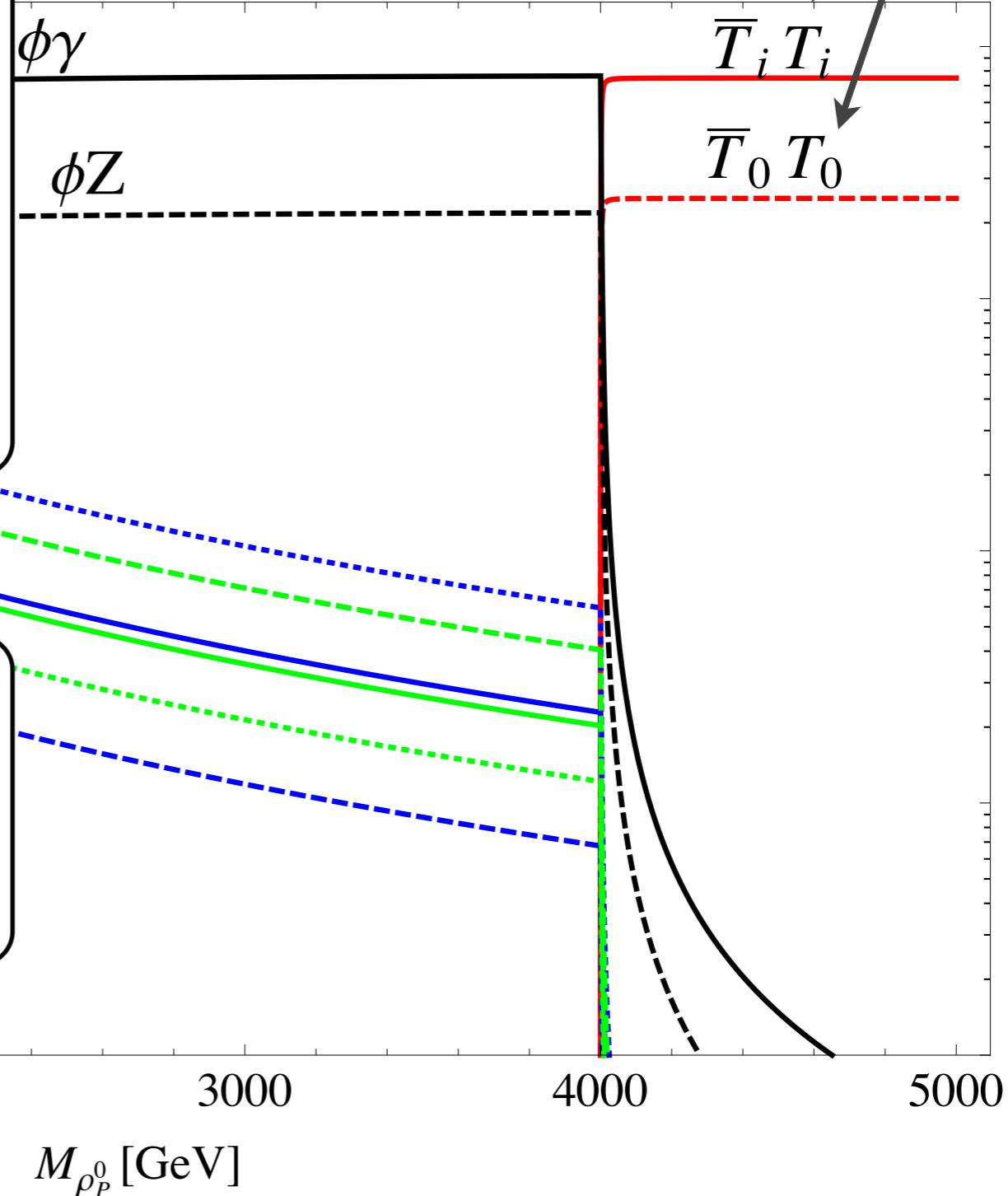
2000

3000

4000

5000

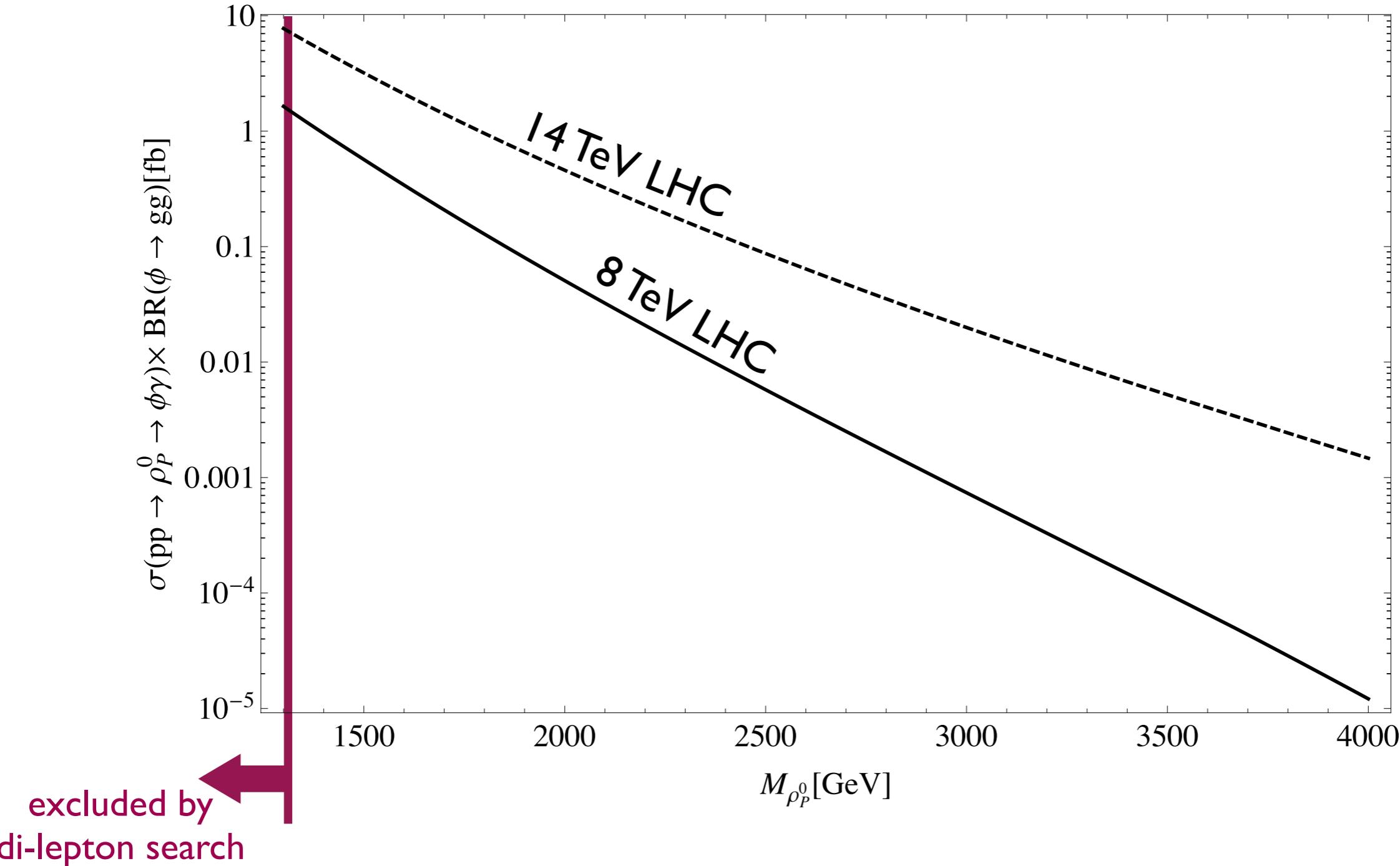
$M_{\rho_P^0} [\text{GeV}]$



ρ_P^0

Color-singlet Iso-singlet

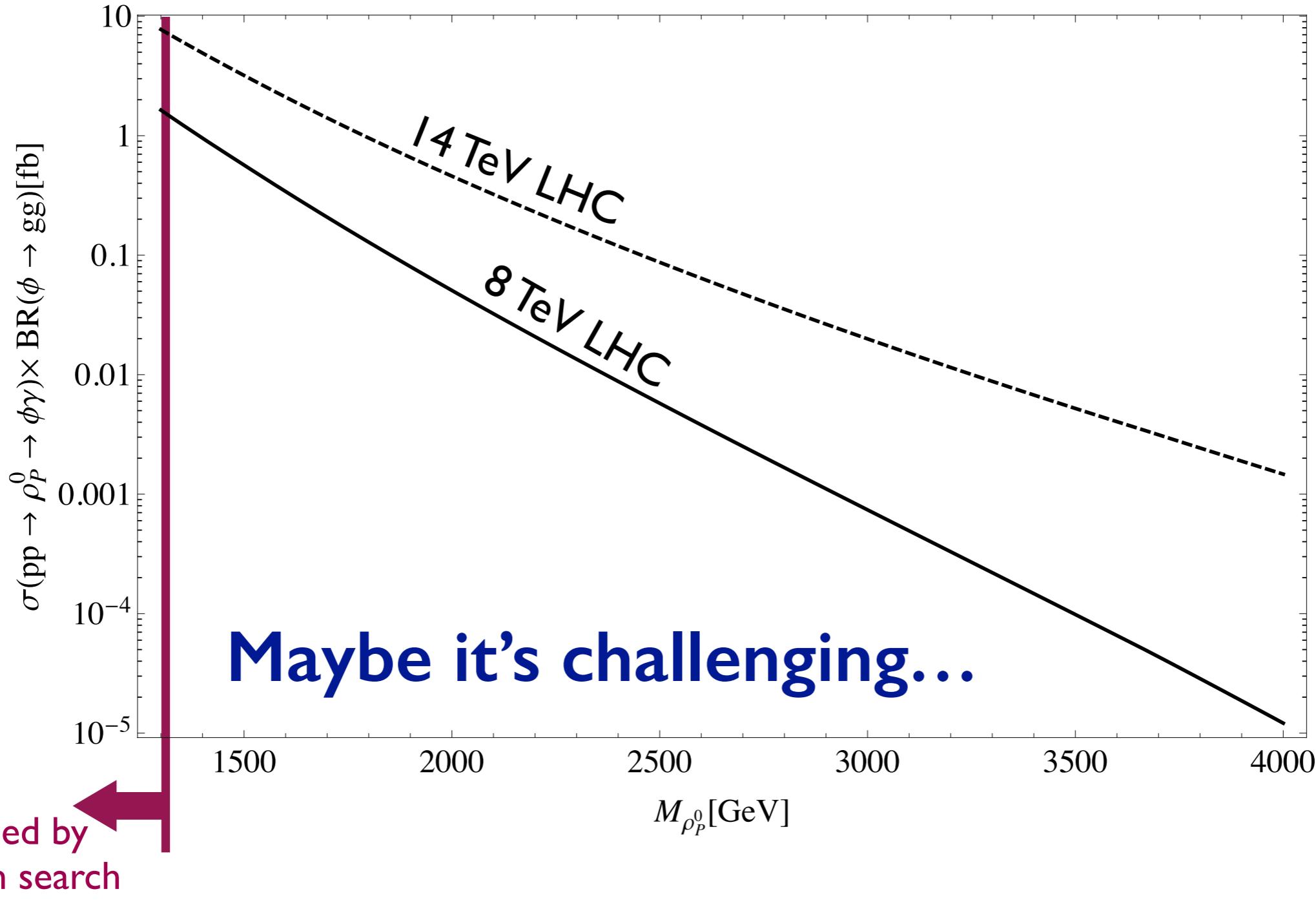
$$\sigma(pp \rightarrow \rho_P^0 \rightarrow \phi \gamma) \times \text{BR}(\phi \rightarrow gg)$$

 $\sim 75\%$ 

ρ_P^0

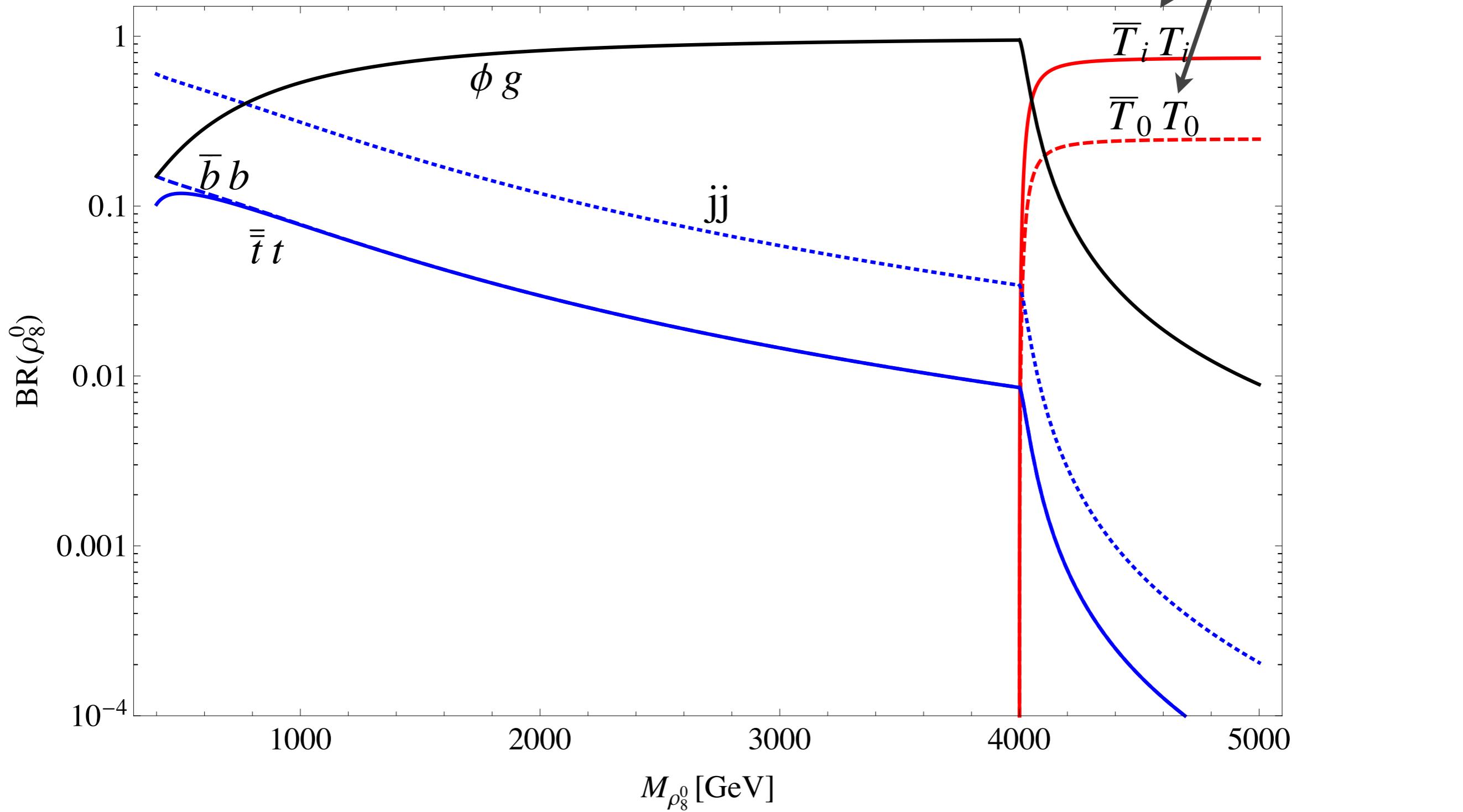
Color-singlet Iso-singlet

$$\sigma(pp \rightarrow \rho_P^0 \rightarrow \phi \gamma) \times \text{BR}(\phi \rightarrow gg)$$

 $\sim 75\%$ 

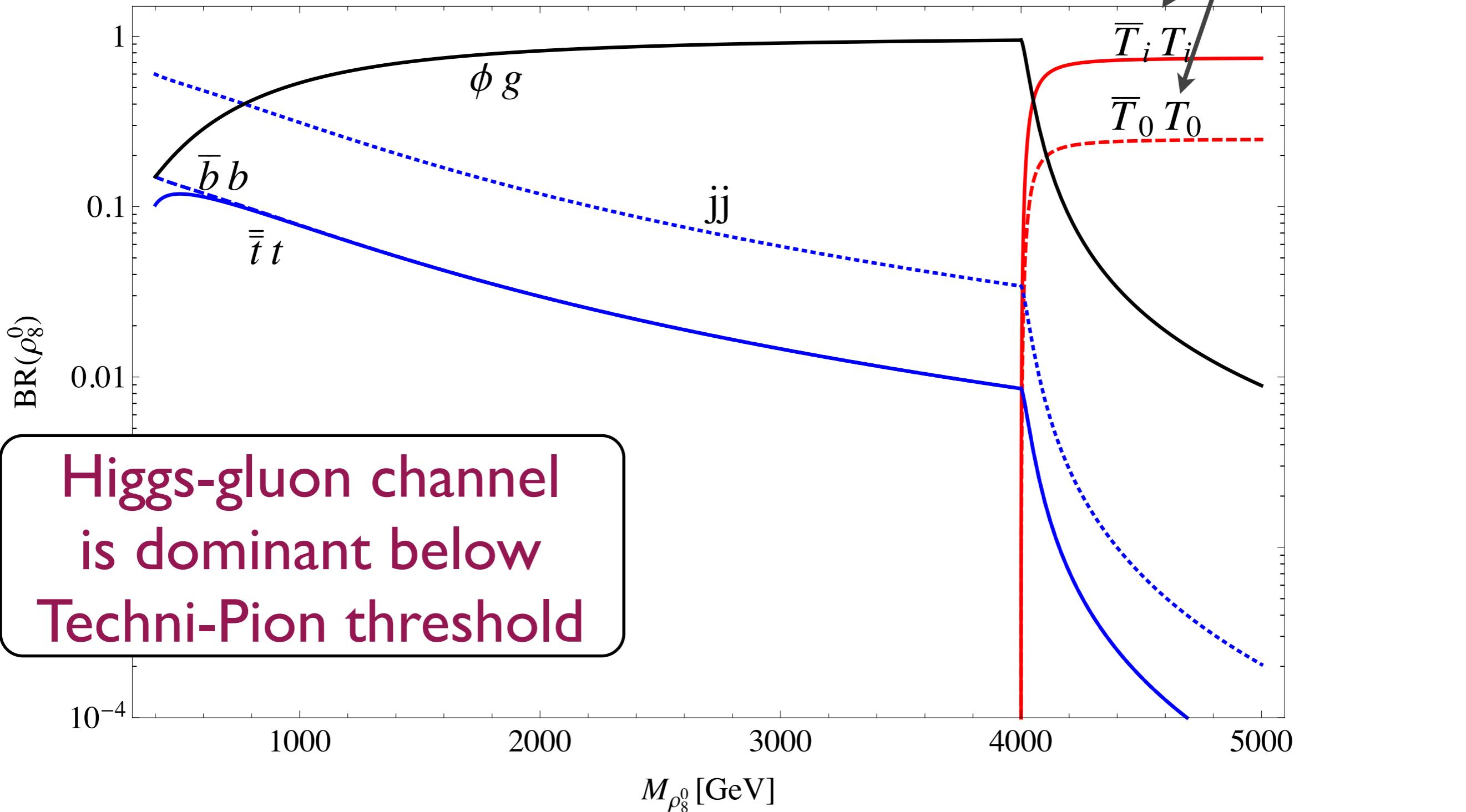
ρ_8^0

Color-octet Iso-singlet

Branching ratio

ρ_8^0

Color-octet Iso-singlet

Branching ratio

ρ_8^0

Color-octet Iso-singlet

Branching ratio

Constraint from LHC?

dijet resonance search would

CMS-PAS-EXO-12-016

constrain ρ_8^0 mass to be

$M_{\rho_8^0} > 1.6 \text{ TeV}$

$\text{BR}(\rho_8^0)$

0.01

Higgs-gluon channel
is dominant below
Techni-Pion threshold

10^{-4}

1000

2000

3000

4000

5000

$M_{\rho_8^0} [\text{GeV}]$

Color-triplet
Techni-Pions
($M_T = 2 \text{ TeV}$)

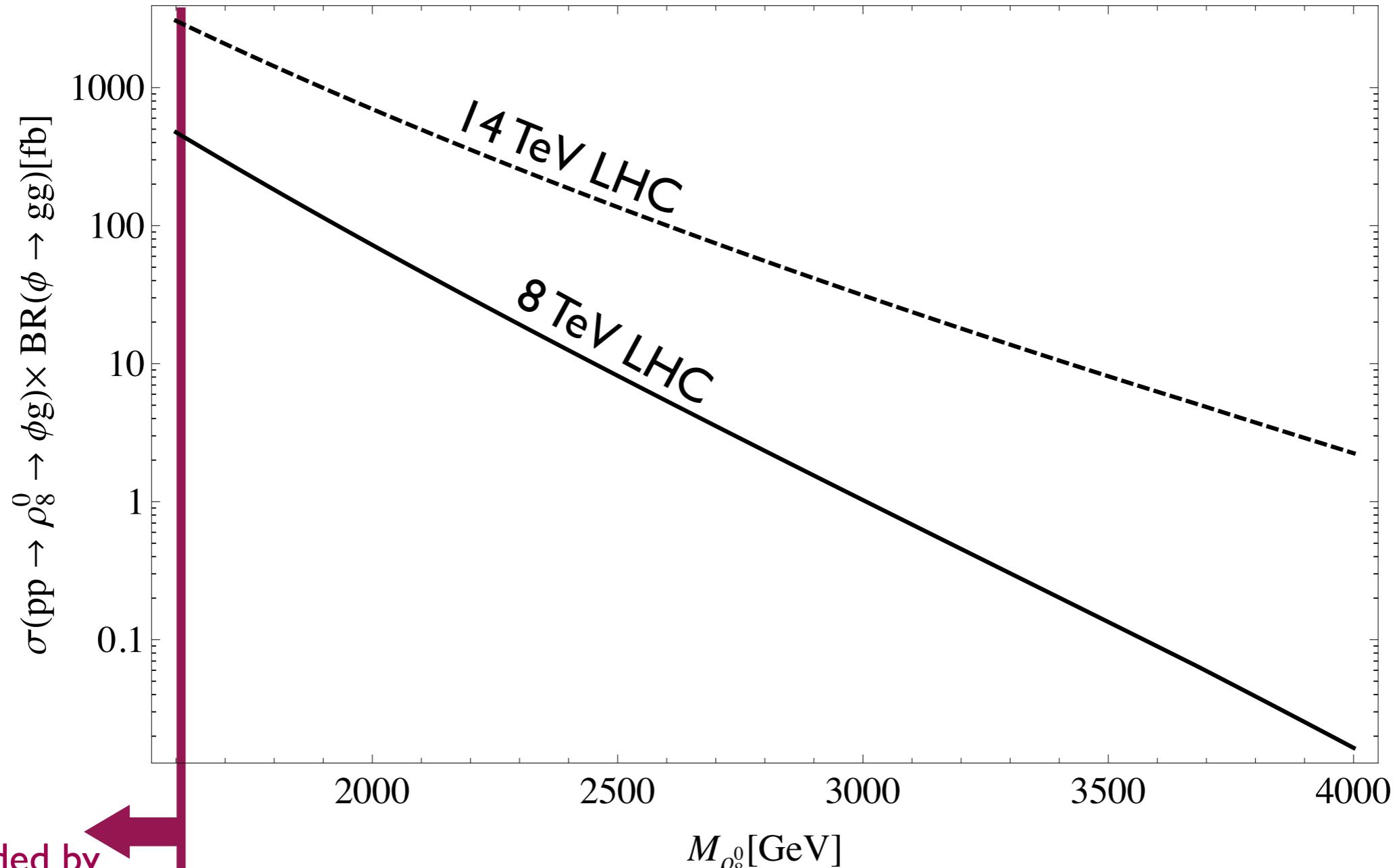
$\bar{T}_i T_i$
 $\bar{T}_0 T_0$

jj

ρ_8^0

Color-octet Iso-singlet

$$\sigma(pp \rightarrow \rho_8^0 \rightarrow \phi g) \times \text{BR}(\phi \rightarrow gg)$$

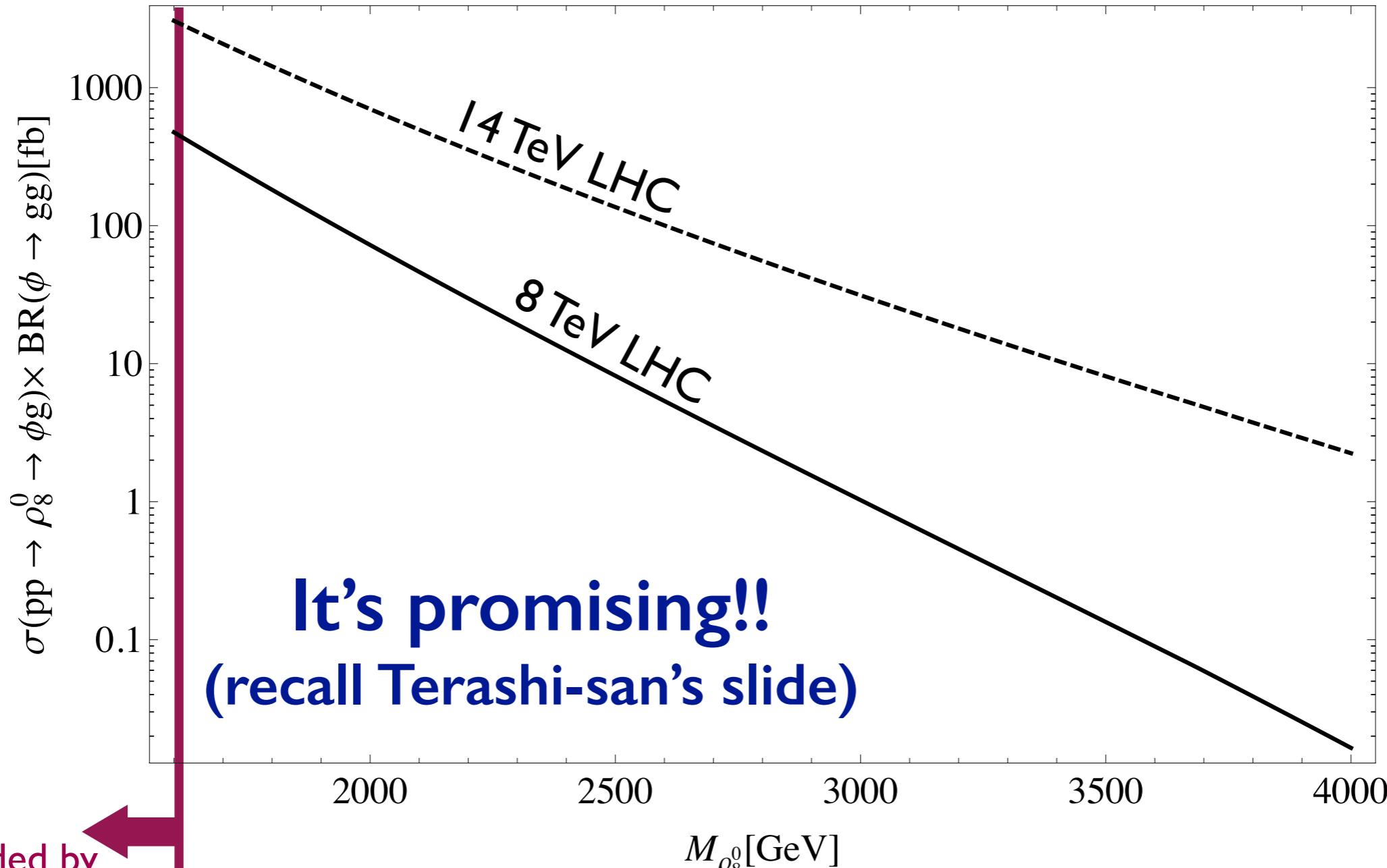
 $\sim 75\%$ 

excluded by
di-jet search

ρ_8^0

Color-octet Iso-singlet

$$\sigma(pp \rightarrow \rho_8^0 \rightarrow \phi g) \times \text{BR}(\phi \rightarrow gg)$$

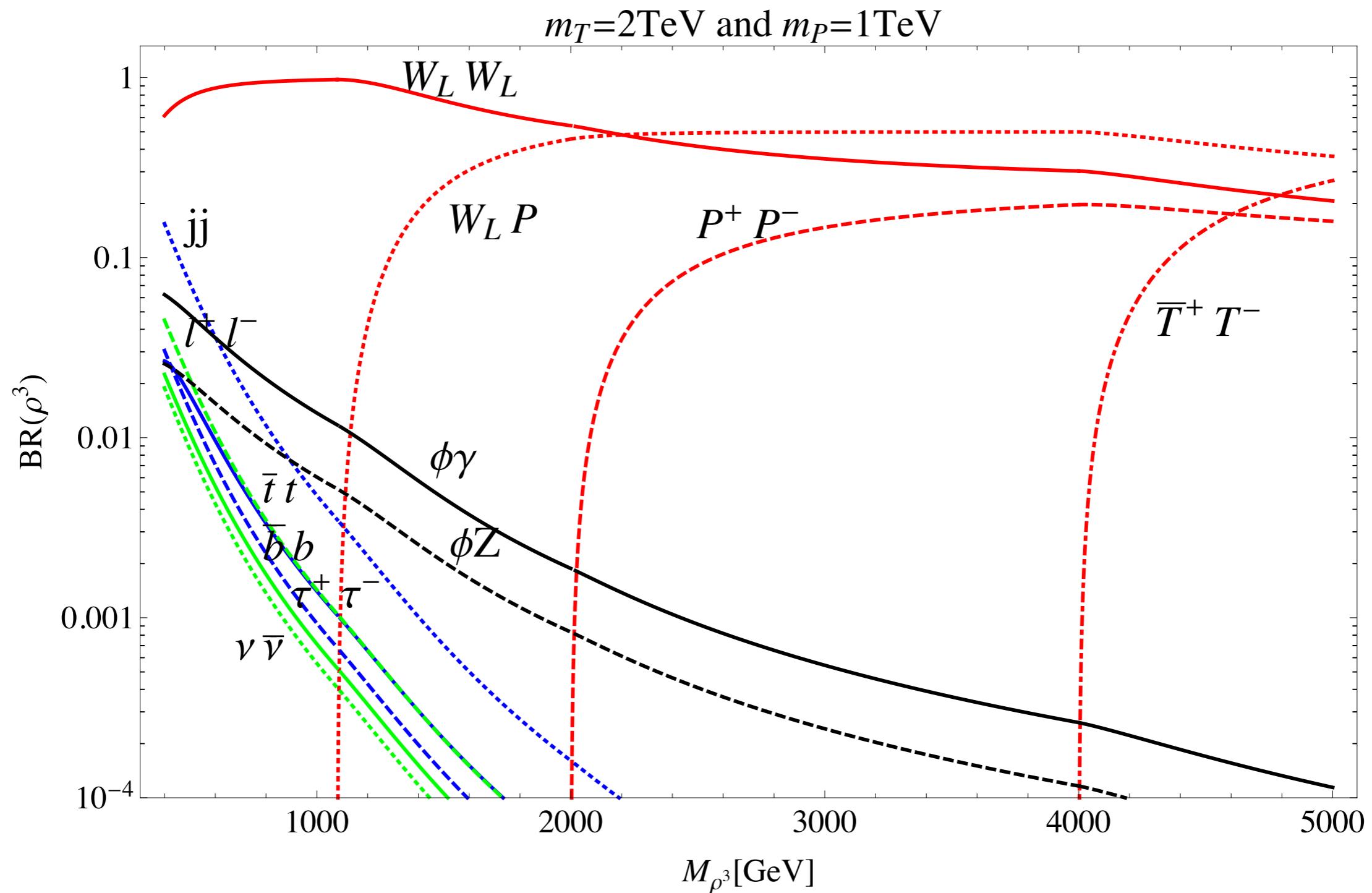
 $\sim 75\%$ 

4. Summary

- Techni-Pions, Techni-dilaton, and Techni-Rho mesons as Low-energy spectrum of the one-family TC
- Scale-invariant chiral Lagrangian with the HLS
- Techni-Dilaton production through Techni-Rho decay
- Color-octet technirho decaying into the Higgs (Techni-dilaton) and gluon is promising channel
- Detailed collider study is in progress

Backups

Branching ratio (ρ^3)



Branching ratio (ρ^\pm)

