

# Lepton-Specific two-Higgs doublet model as a solution of the muon $g-2$ anomaly

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in Collaboration with

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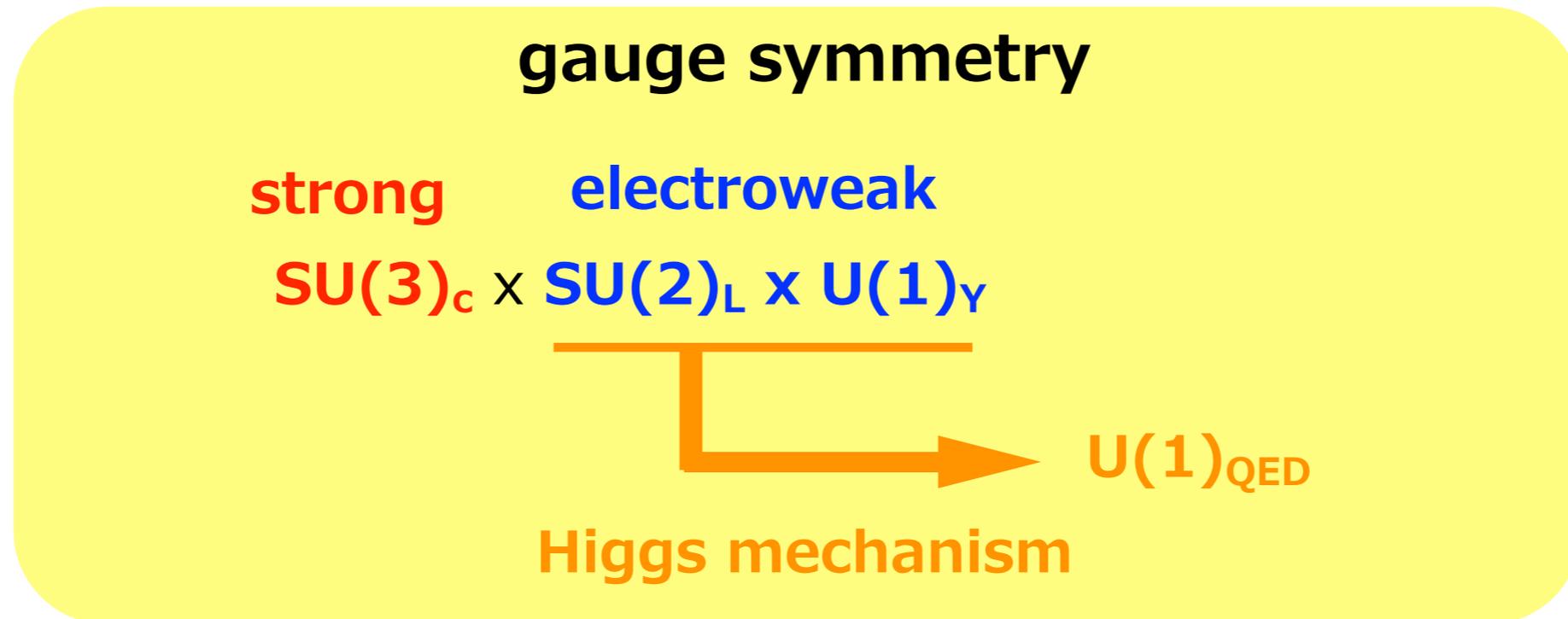
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KMI topics

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# Success of the Standard Model



## Yukawa interaction

$$-\bar{q}_L^i \tilde{H} y_u^{ij} u_R^j - \bar{q}_L^i H y_d^{ij} d_R^j - \bar{\ell}_L^i H y_e^{ij} e_R^j$$

- ★ fermion mass
- ★ CKM matrix
- ★ CP violation

## Higgs potential

$$V = \mu^2 H^\dagger H + \lambda (H^\dagger H)^2$$

- ★ spontaneous symmetry breaking
- ★ Higgs mass

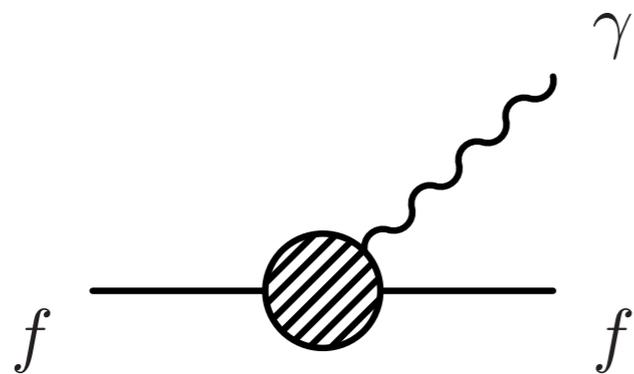
# We need a model beyond the Standard Model

- **SM cannot explain that**

- ★ dark matter
- ★ baryon asymmetry (matter  $\gg$  anti-matter in the universe)
- ★ the origin of neutrino mass
- ★ **muon  $g-2$**
- ★ ...

# Muon g-2

- the property of muon as *a magnet*



$$i\mathcal{M} = -i\bar{u}_f e Q_f \left( F_1(q^2) \gamma^\mu + F_2(q^2) i \frac{\sigma^{\mu\nu} q_\nu}{2m_f} \right) u_f$$

$$a_f = \frac{g_f - 2}{2} = F_2(0)$$

- **Status: more than  $3\sigma$  deviation**

$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (28.7 \pm 8.0) \times 10^{-10}, \quad \text{Davier et.al. (2011)}$$

$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (26.1 \pm 8.0) \times 10^{-10}, \quad \text{Hagiwara et.al. (2011)}$$

- **three interpretations:**

- ★ error in experiments
- ★ error in theoretical prediction
- ★ *new physics*

# Muon g-2 and new physics scale

SM + dim. 6 operators

$$+ \frac{c'}{(4\pi)^2} \frac{g'}{\Lambda'^2} (\bar{\ell}_L \sigma^{\mu\nu} H e_R B_{\mu\nu}) - \frac{c}{(4\pi)^2} \frac{g}{\Lambda^2} (\bar{\ell}_L \sigma^{\mu\nu} W_{\mu\nu} H e_R) + (h.c.)$$

Amp  $\sim \bar{u} i \sigma^{\mu\nu} q_\nu \epsilon_\mu \frac{\delta a_\mu}{2m_\mu} u$    $\delta a_\mu = 2m_\mu \frac{v}{\sqrt{2}} \frac{1}{(4\pi)^2} \left( 2 \frac{c'}{\Lambda'^2} + \frac{c}{\Lambda^2} \right)$

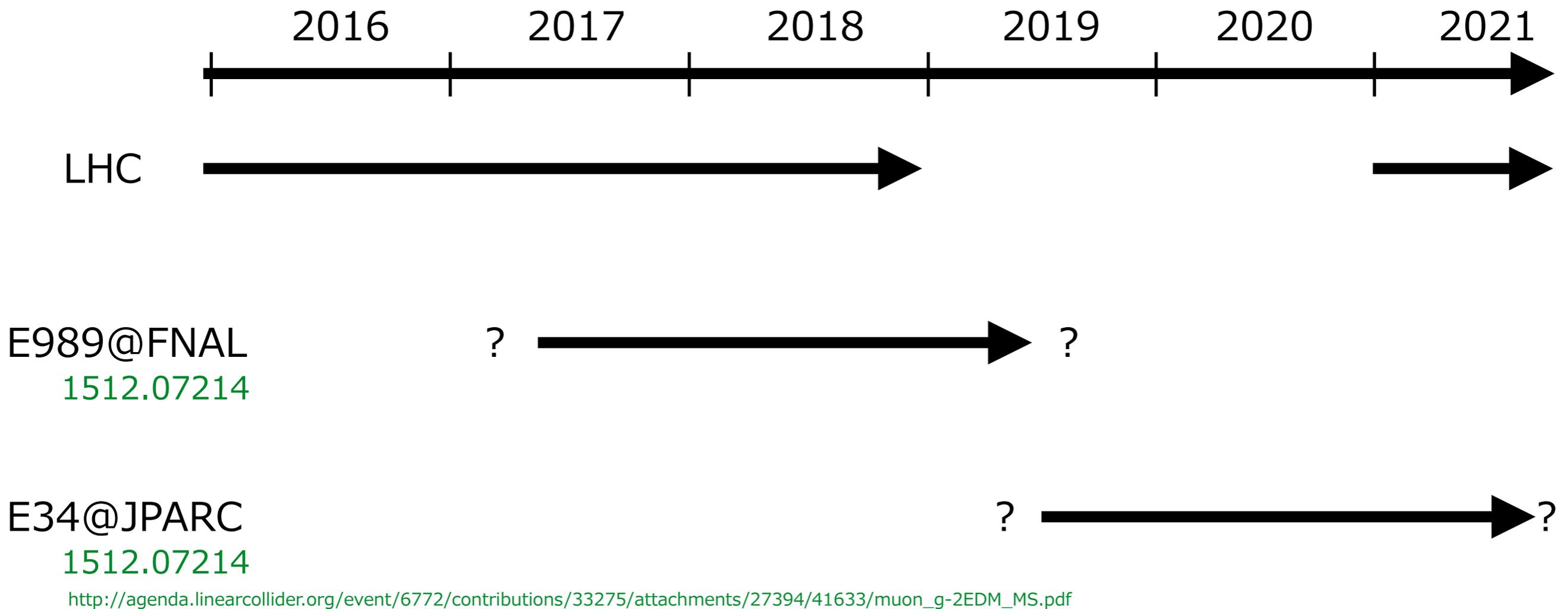
ex)  $c = 0$

$c'$	1	0.1	0.01	0.001
$\Lambda' [\text{TeV}]$	13	4.2	1.3	0.42

**strong expectation** of the existence new physics

around **TeV scale**

# exp. schedule



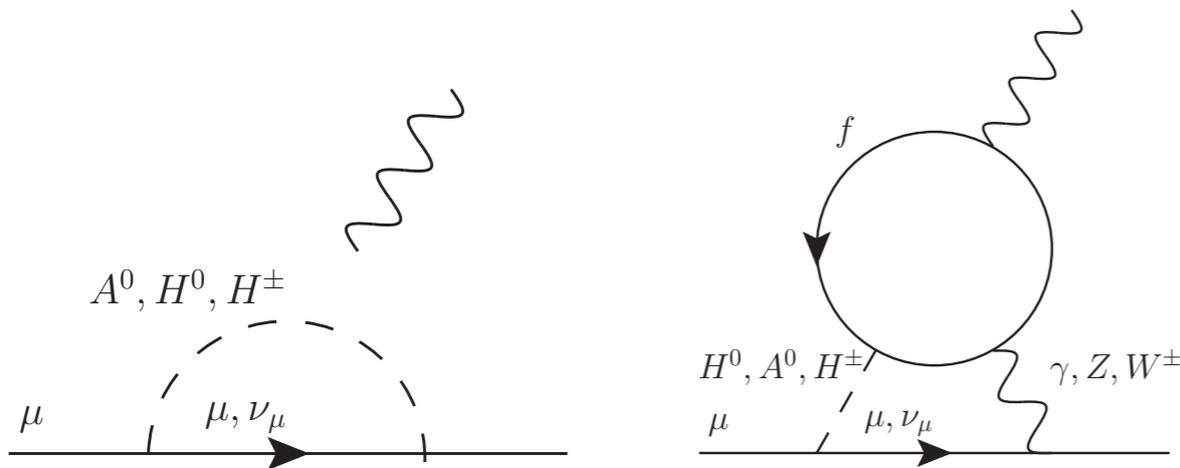
**Now** is the time for g-2

# Muon $g-2$ and new physics

## What kind of models are preferred?

- ★ new particle must coupling to lepton (muon)
- ★ simple model
- ★ verifiable model in the near future

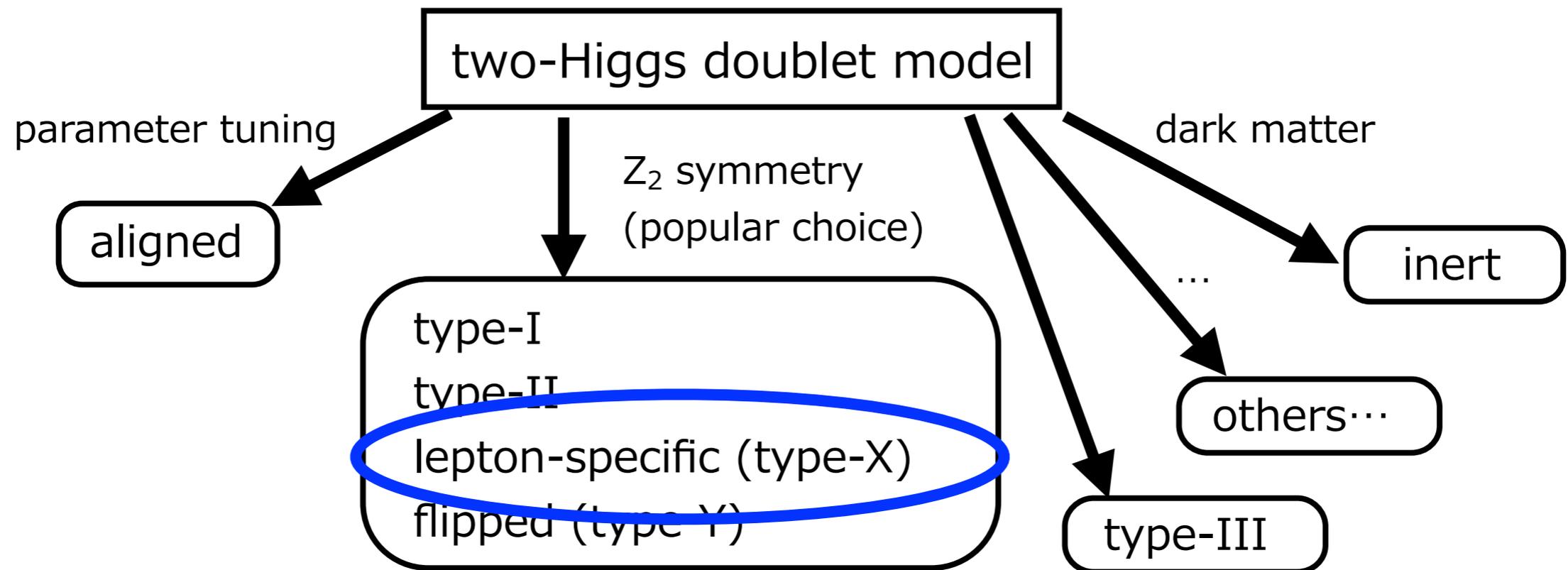
## two-Higgs doublet model



- ★ simple extension from SM
- ★ new scalar particles ( $H^0, A^0, H^\pm$ )
- ★ mass  $\sim O(10)$ -  $O(1000)$ GeV
- ★ large coupling to leptons
- ★ the great candidate for muon  $g-2$ !

# two-Higgs doublet model

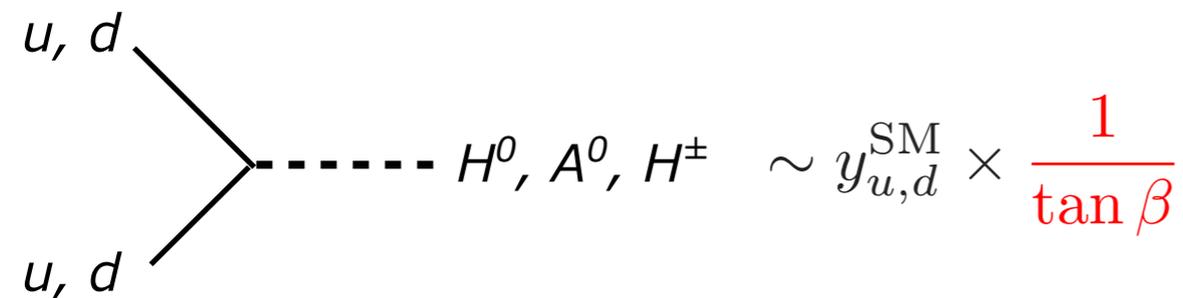
- “two-Higgs doublet model” = a set of many models
- Many models exist for different structure of Yukawa interactions
  - ★ different names for different models

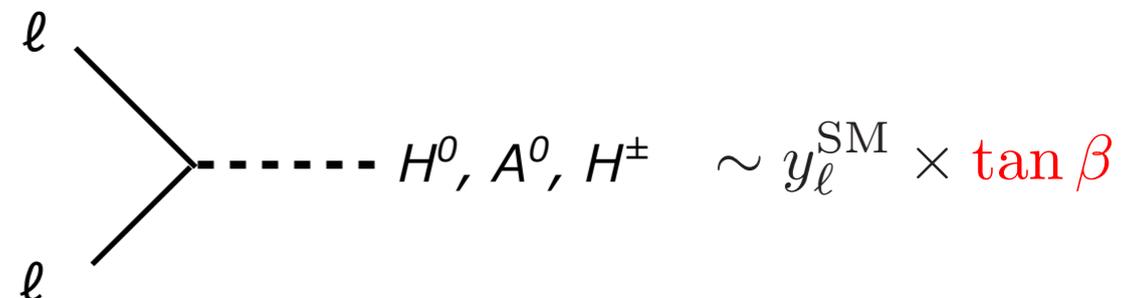


**A viable model for muon  $g-2$  !**

# lepton specific two-Higgs doublet model

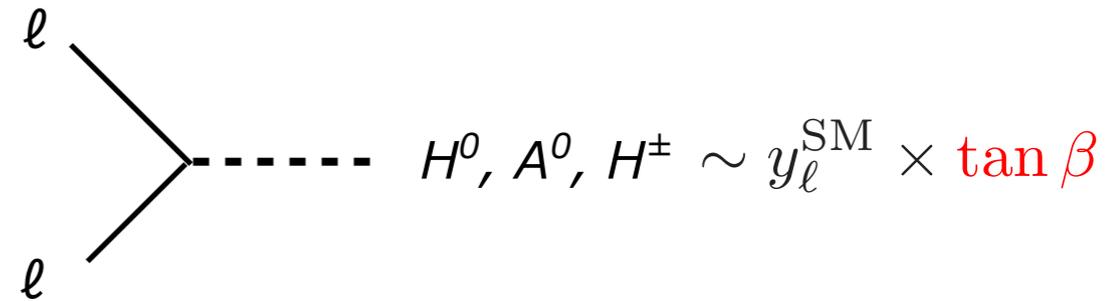
- SM + one more Higgs doublet
- two Higgs :  $H_1$  and  $H_2$ 
  - ★ SM-like Higgs ( $h$ )
  - ★ new scalars ( $H^0, A^0, H^\pm$ )
- important parameter:  **$\tan\beta$**  ( $1 < \tan\beta < 100$ )
- the lepton Yukawa interactions are enhanced by  $\tan\beta$


$$u, d \quad u, d \quad \text{---} \quad H^0, A^0, H^\pm \quad \sim y_{u,d}^{\text{SM}} \times \frac{1}{\tan\beta}$$

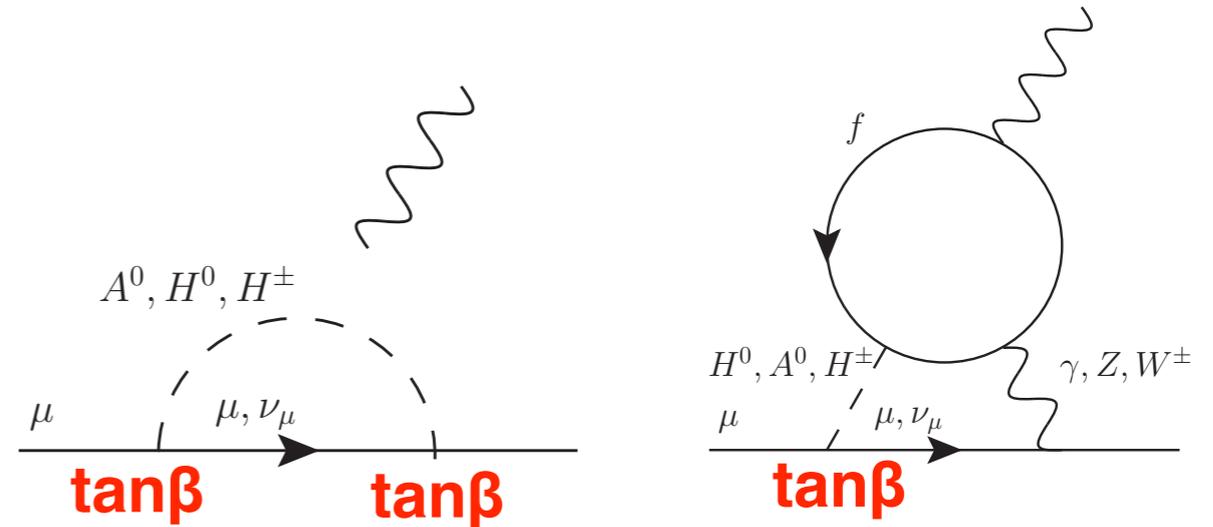

$$l \quad l \quad \text{---} \quad H^0, A^0, H^\pm \quad \sim y_l^{\text{SM}} \times \tan\beta$$

# lepton physics

- new particles affect to all the physics with leptons



- **good point** : muon g-2

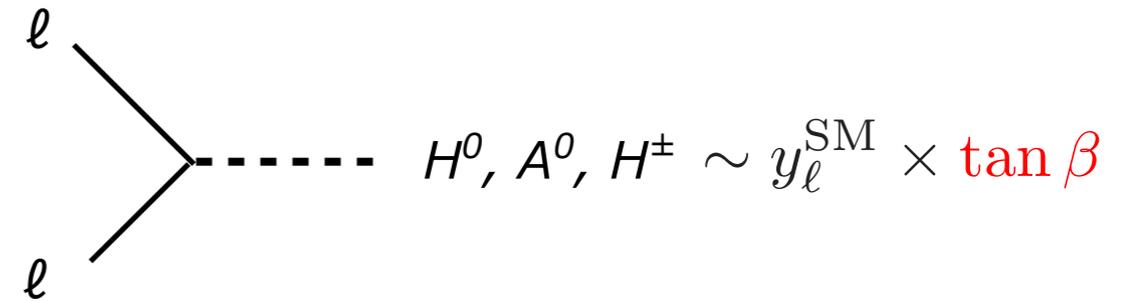


- **On the other hand**, constraints on the lepton couplings are important

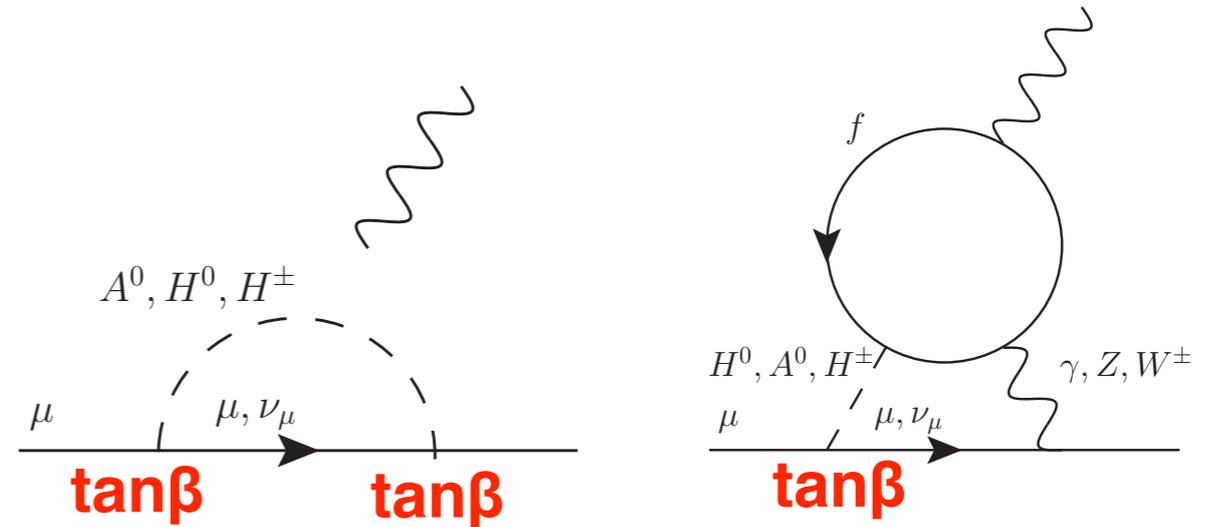
- ★  $Z \rightarrow \tau\tau$
- ★  $Z \rightarrow \tau\tau A^0$
- ★  $\tau \rightarrow \mu\nu_\tau\bar{\nu}_\mu, \tau \rightarrow e\nu_\tau\bar{\nu}_e$ 
  - \* Michel parameters
  - \* lepton coupling universality

# lepton physics

- new particles affect to all the physics with leptons



- **good point** : muon g-2



- **On the other hand**, constraints on the lepton couplings are important

- ★  $Z \rightarrow \tau\tau$
- ★  $Z \rightarrow \tau\tau A^0$
- ★  $\tau \rightarrow \mu\nu_\tau\bar{\nu}_\mu, \tau \rightarrow e\nu_\tau\bar{\nu}_e$

\* Michel parameters

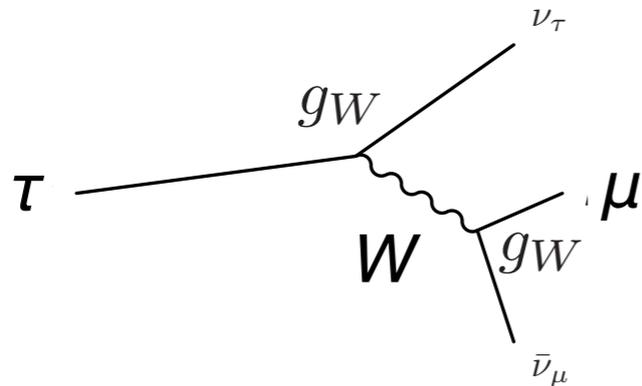
\* **lepton coupling universality**

the most stringent bound

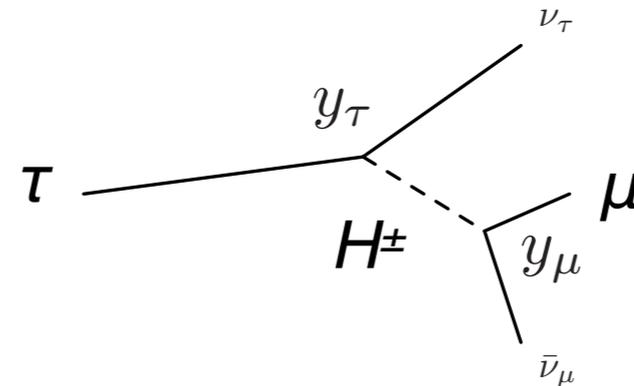


# lepton $\beta$ decays

- $H^\pm$  breaks lepton universality



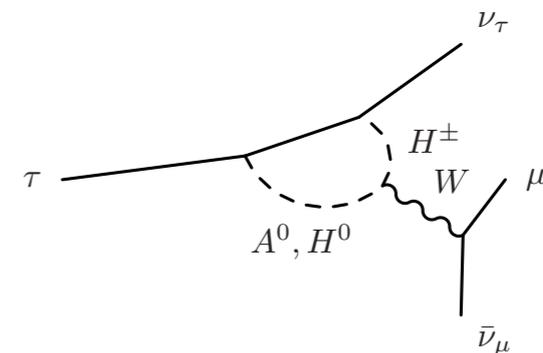
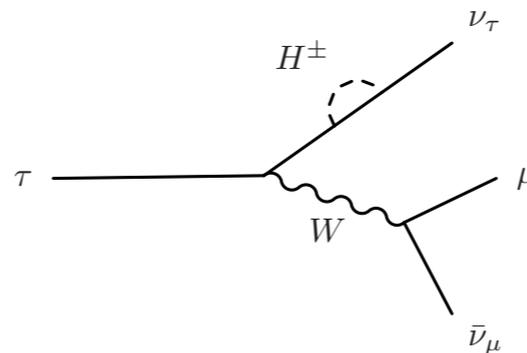
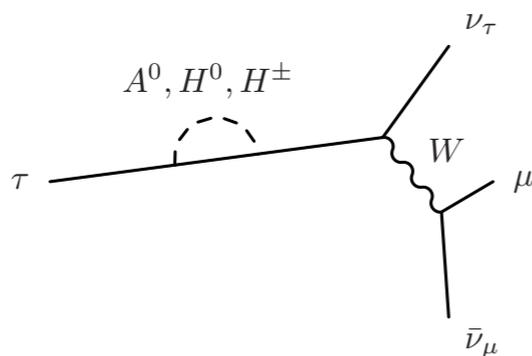
flavor universal interaction



flavor dependent interaction (Yukawa)

- large contributions in  $\tau \rightarrow \mu \nu \bar{\nu}$  process
- small contributions in  $\mu \rightarrow e \nu \bar{\nu}$  process

- loop diagrams also there



# constraint from lepton coupling universality

- define  $G_{\mu\tau}$ ,  $G_{e\tau}$ ,  $G_{e\mu}$

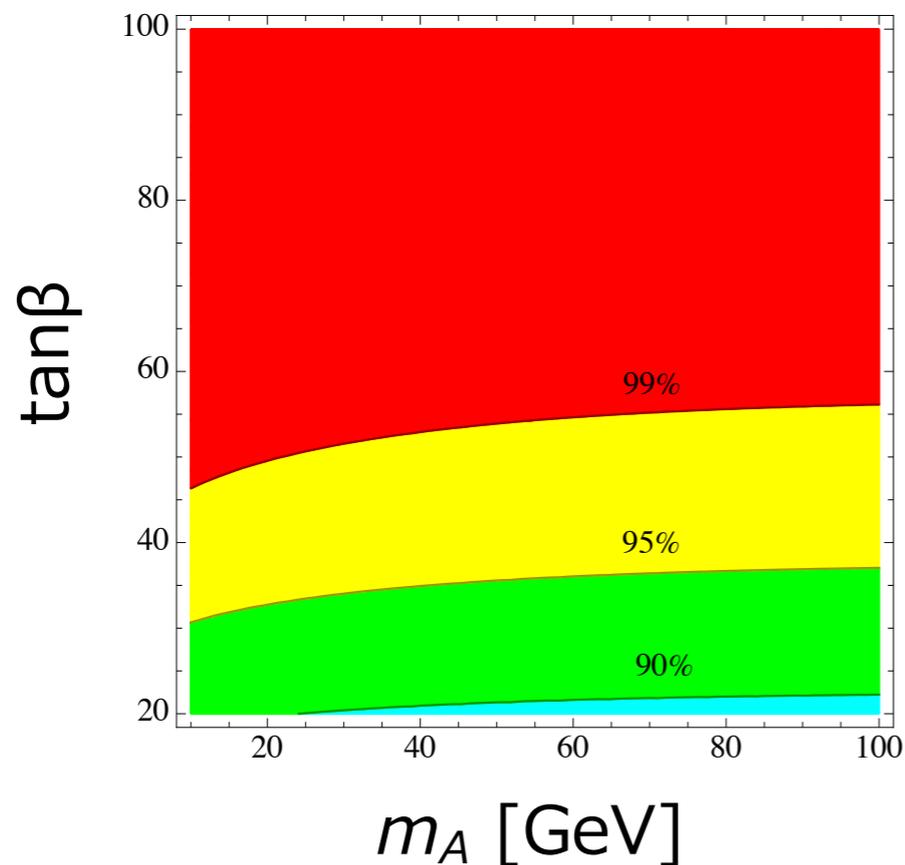
$$\left(\frac{G_{\mu\tau}}{G_F}\right)^2 \equiv \frac{\Gamma(\tau \rightarrow \mu\nu\nu)_{2\text{HDM}}}{\Gamma(\tau \rightarrow \mu\nu\nu)_{\text{SM}}}$$

- constraints [HFAG \(1412.7515\)](#)

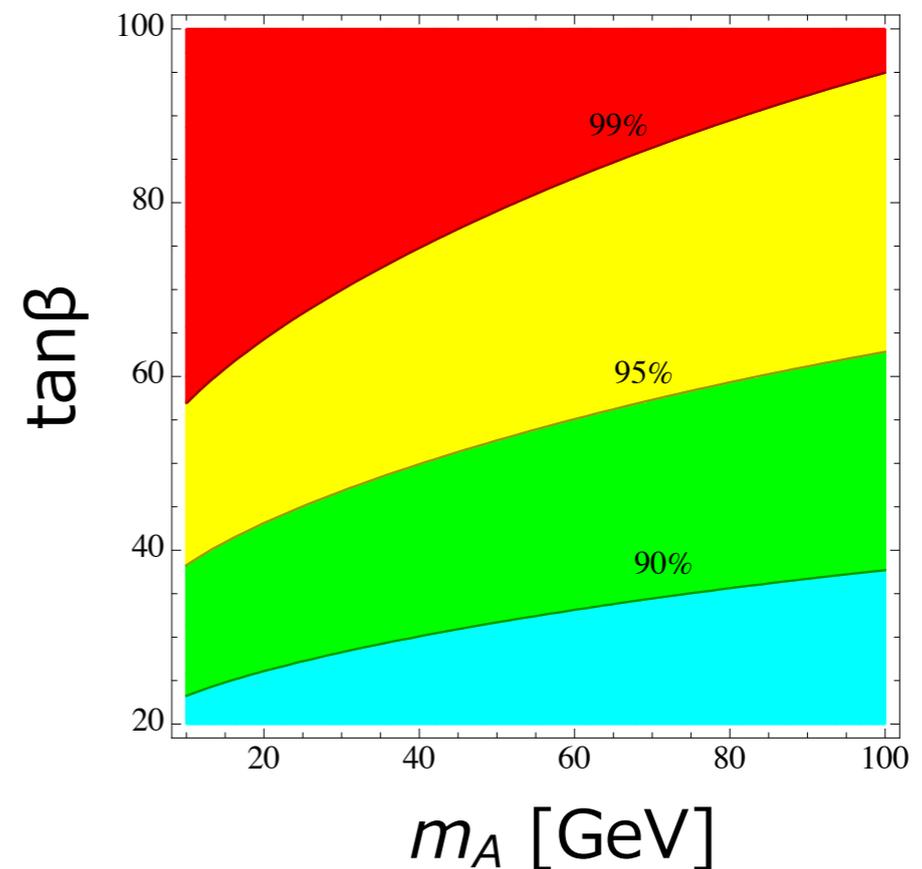
$$\frac{G_{\mu\tau}}{G_{e\mu}} = 1.0029 \pm 0.0015, \quad \frac{G_{\mu\tau}}{G_{e\tau}} = 1.0018 \pm 0.0014,$$

- we find severe constraint on **tanβ** (large **tanβ** is excluded!)

$m_{H\pm} = 150 \text{ GeV}$



$m_{H\pm} = 300 \text{ GeV}$



# $\tan\beta$ dilemma

new particle couplings to lepton is enhanced by  $\tan\beta$

- **large  $\tan\beta$**  is better for muon  $g-2$

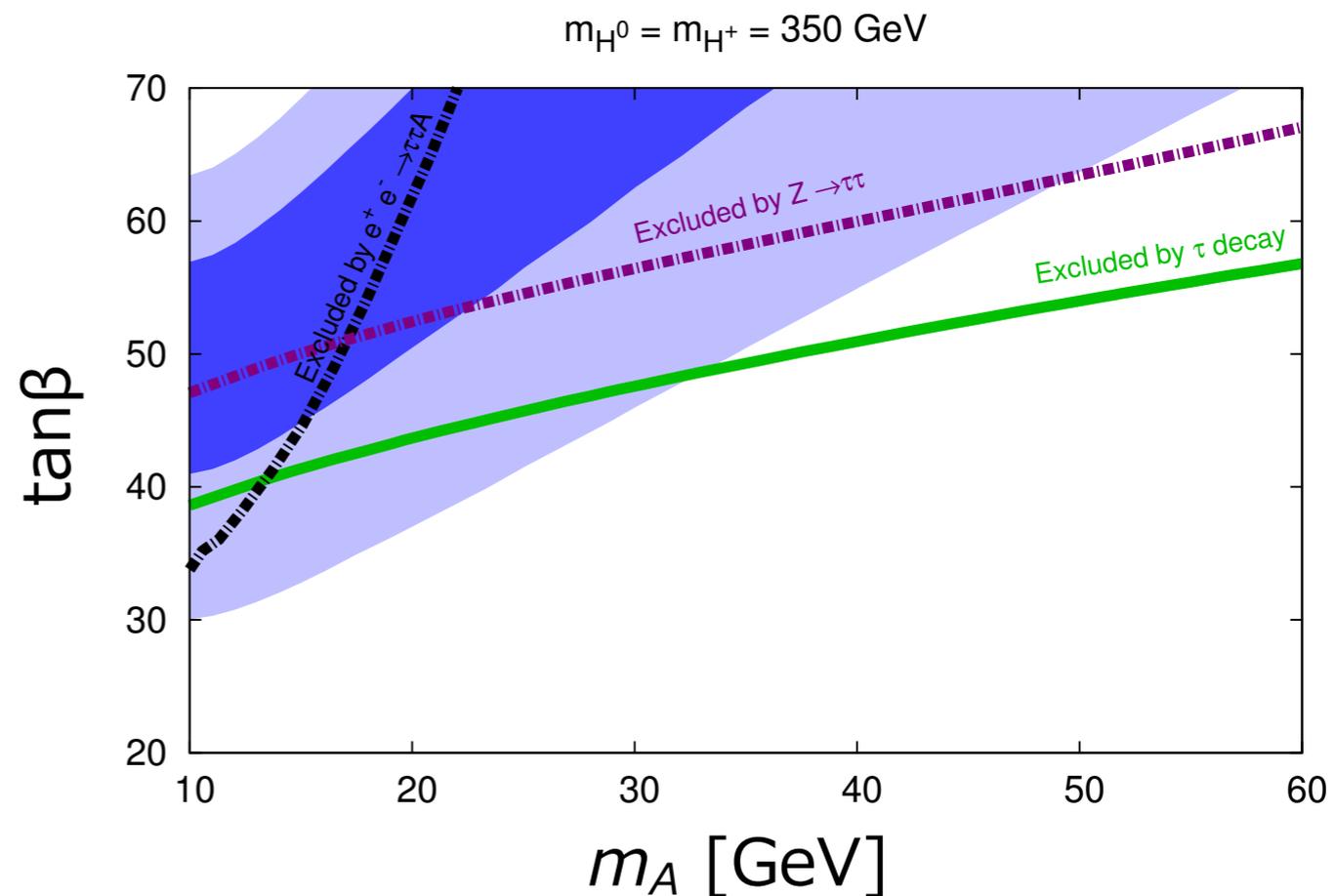
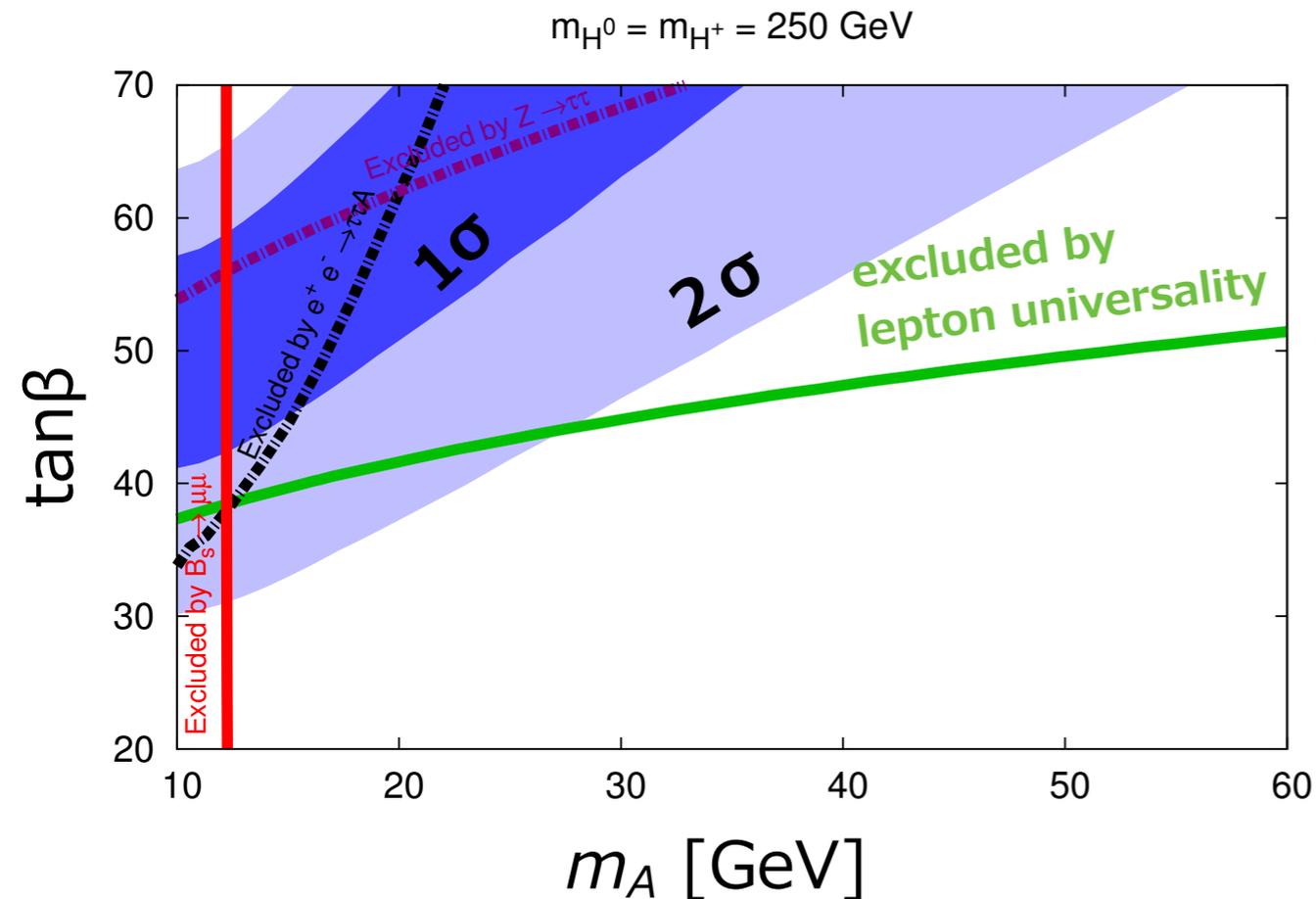
strong constraint from lepton coupling universality

- **small  $\tan\beta$**  is required to avoid the constraint



- $\tan\beta$  is in a dilemma between  **$g-2$**  and **lepton flavor universality**
- Is it possible to explain muon  $g-2$  in this model?  
( $\rightarrow$  see next slide !)

# Result: $g-2$ with constraints



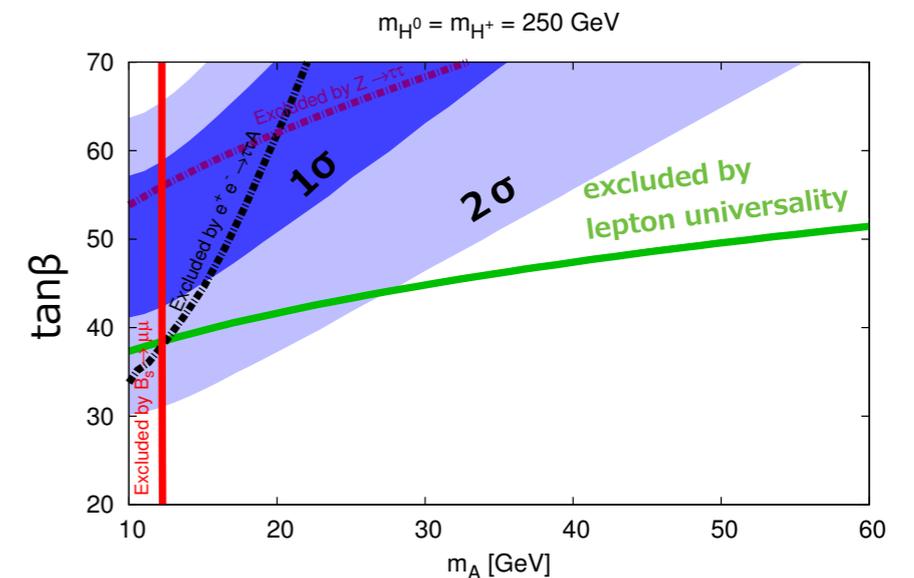
- **$g-2$  within  $1\sigma$  region (dark blue)** is completely excluded!
- **$g-2$  within  $2\sigma$  region (light blue)** is survive!
- constraint from **lepton universality** is strong.

# short summary

- lepton specific two-Higgs doublet model can explain muon  $g-2$  within  $2\sigma$

- **parameters for the muon  $g-2$**

- ★  $10 \text{ GeV} < m_A < 30 \text{ GeV}$
- ★  $250 \text{ GeV} < m_{H^\pm} < 350 \text{ GeV}$
- ★  $m_{H^0} = m_{H^\pm}$
- ★  $30 < \tan\beta < 40$



- **What else ...?**
- **phenomenology at the LHC is a good complement**

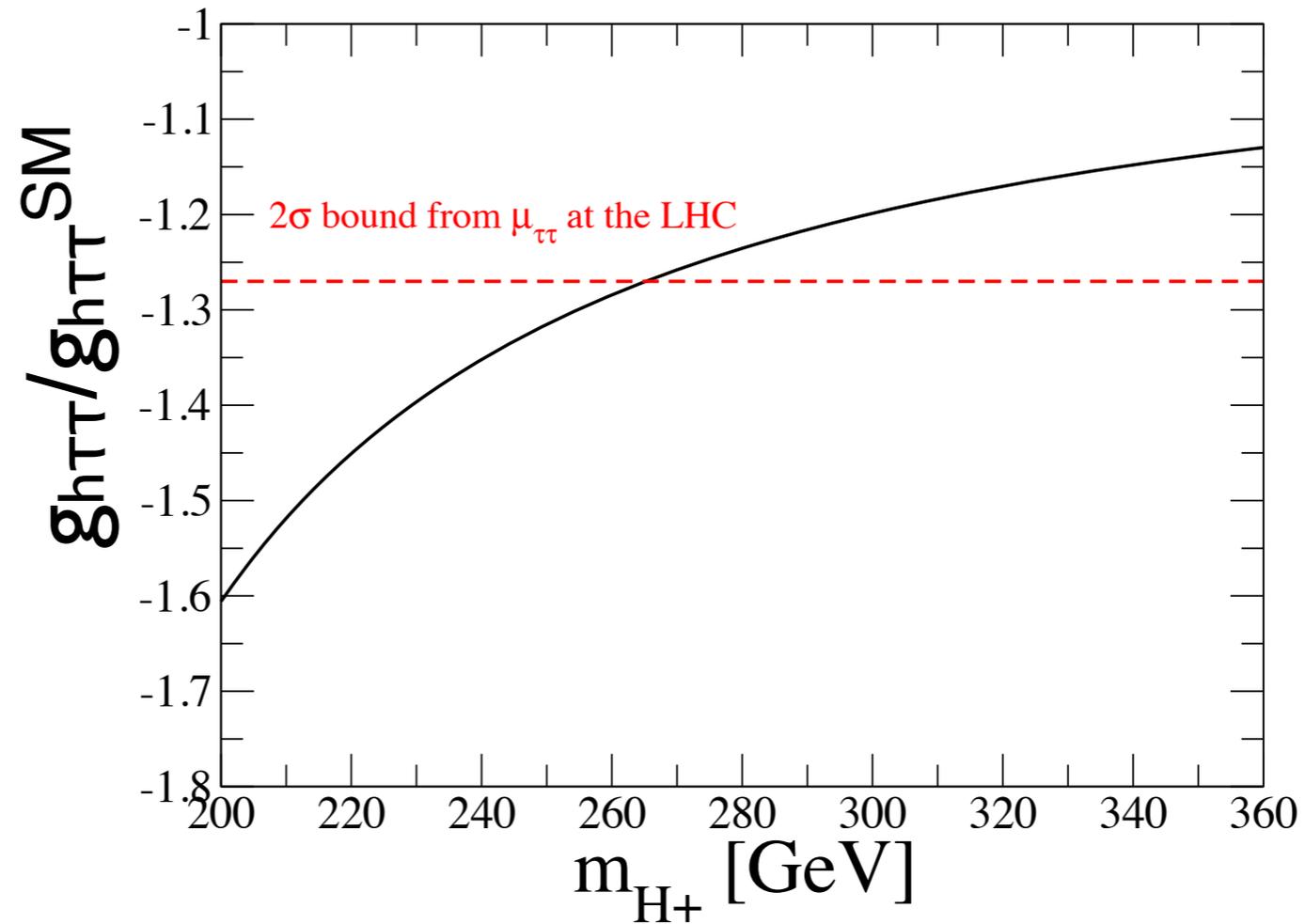
# ***Collider physics***

# h(125) couplings (1)

- $h_{\tau\tau}$  : *more than 10% deviation* from the SM prediction

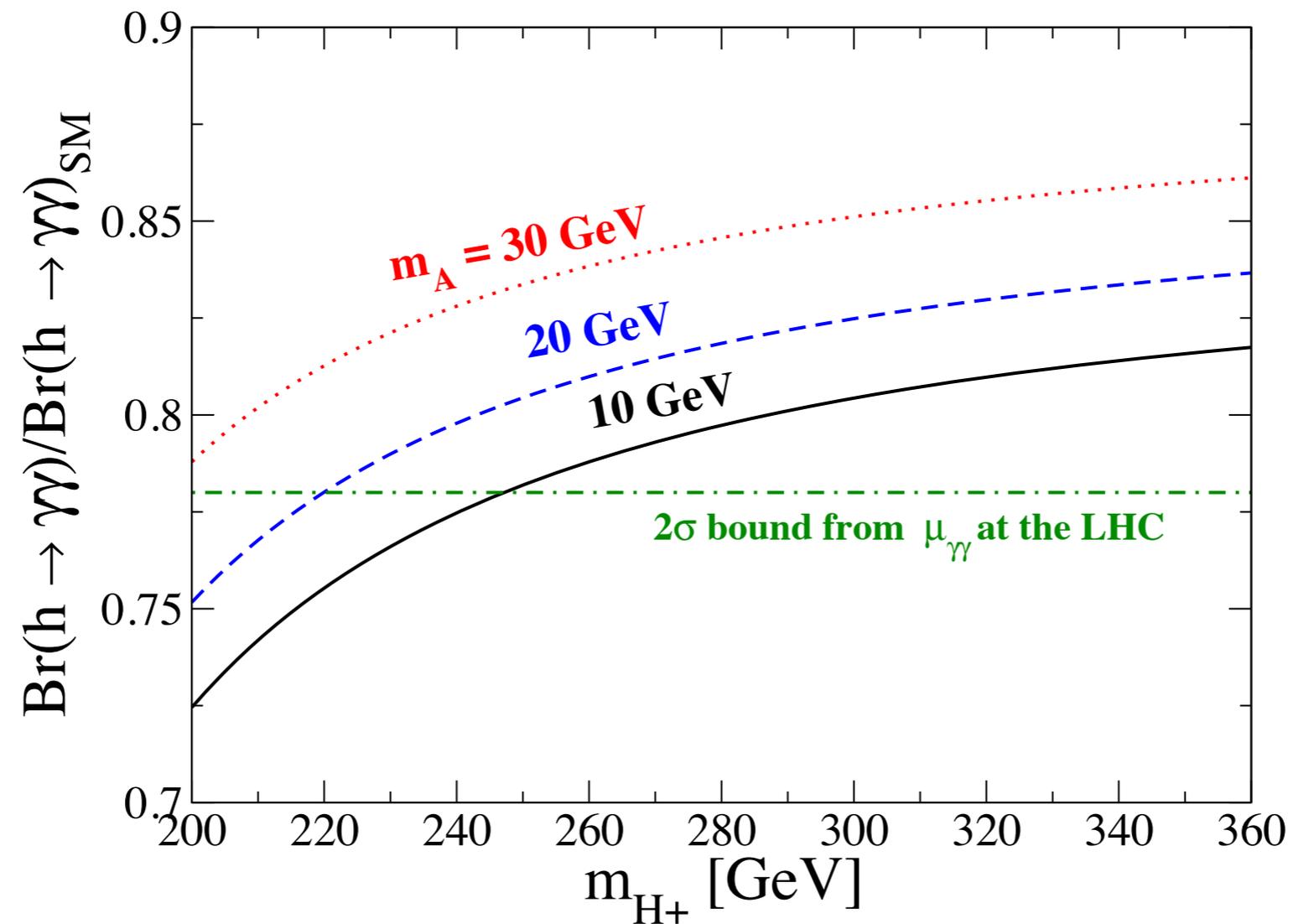
$$\kappa_\ell \simeq -1 - \frac{m_h^2}{m_{H^\pm}^2} + \frac{2m_A^2}{m_{H^\pm}^2}$$

$$\kappa_X = g_{hXX}/g_{hXX}^{\text{SM}}$$



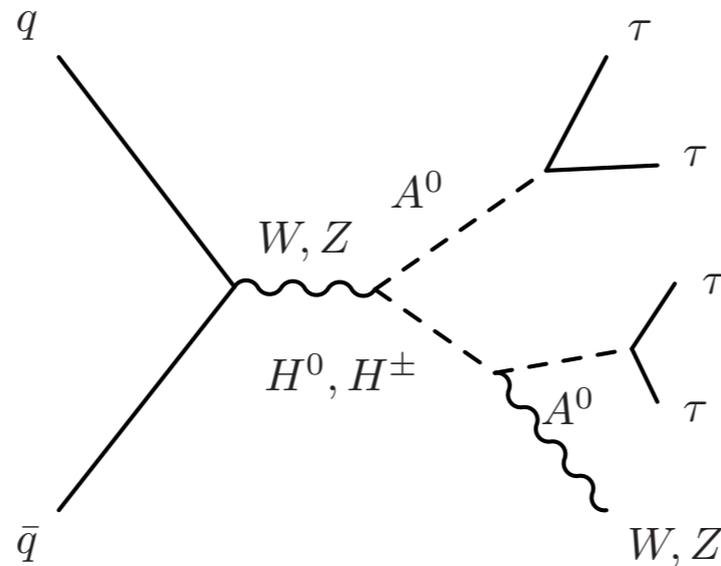
# $h(125)$ couplings (2)

- $h\gamma\gamma$  : *more than 10% deviation* from the SM prediction



# $H^0, A^0, H^\pm$ at the LHC

- *many tau leptons* are produced at the LHC 14TeV



- xsec [fb]

$m_{H^\pm}$ [GeV]	$\sigma_{H^+H^-}$	$\sigma_{H^+H}$	$\sigma_{H^-H}$	$\sigma_{H^+A}$	$\sigma_{H^-A}$	$\sigma_{AH}$	$\sigma_{4\tau}$	$\sigma_{3\tau}$	$\sigma_{4\tau W}$	$\sigma_{4\tau Z}$
200	18.6	22.0	11.3	116	67.0	101	29.3	50.1	143	70.7
250	8.0	9.7	4.7	53.5	29.5	45.1	7.2	12.8	72.5	37.4
300	3.9	4.8	2.3	28.2	14.9	23.2	2.3	4.3	39.4	20.6
350	2.1	2.6	1.1	16.2	8.2	13.0	0.9	1.7	22.9	12.0

Table 2: Cross sections of the electroweak production processes expressed in Eq. (65), and those of the multi-tau processes expressed in Eqs. (67)-(70) at  $\sqrt{s} = 14$  TeV in the unit of fb. We take  $m_A = 20$  GeV,  $m_H = m_{H^\pm}$ ,  $\sin(\beta - \alpha) = 1$  and  $\tan \beta = 35$ .

# *Summary*

# Summary

- **lepton specific two-Higgs doublet model**

- ★ simple extension from the SM
- ★ large new particle couplings to the leptons by  **$\tan\beta$**
- ★  **$\tan\beta$**  is in a dilemma between  **$g-2$**  and **lepton flavor universality**
- ★ **can explain muon  $g-2$  within  $2\sigma$**

- **parameters for the muon  $g-2$**

- ★  $10 \text{ GeV} < m_A < 30 \text{ GeV}$
- ★  $250 \text{ GeV} < m_{H^\pm, H^0} < 350 \text{ GeV}$
- ★  $30 < \tan\beta < 40$

- **LHC phenomenology**

- ★ **more than 10%** deviation in  **$h\tau\tau$**  and  **$h\gamma\gamma$**  couplings  
(within the reach of LHC14TeV 300fb<sup>-1</sup> (year 2022?))
- ★  **$O(10)$  fb multi- $\tau$  events** will be observed

