

# Long-lived CHAMPs

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# Long-lived charged massive particle

- ☑ Long-lived CHAMPs in many models beyond SM
- ☑ Various hunting  
(collider, neutrino telescope observations, etc)
- ☑ Cosmological constraints on its property  
(big-bang nucleosynthesis, large scale structure., etc)

One of the interesting objects for particle physics, astrophysics, and nuclear physics

# Long-lived stau

Candidate of long-lived CHAMP: NLSP stau in SUSY models

NLSP: Next lightest SUSY particle

- ☑ Illustrative example in this talk  
(same phenomenology also for other long-lived CHAMPs)
  
- ☑ Three scenarios of long-lived stau
  - Gravitino dark matter scenario (coupling suppression)
  - Neutralino dark matter scenario (phase space suppression)
  - Axino dark matter scenario (loop suppression)

# Long-lived stau

- ☑ Similar but different in appearance

	Neutralino scenario	Gravitino scenario
Why long-lived?	Phase space suppression	Coupling suppression
Typical signals	Missing $E_T$ + heavy charged track	Heavy charged track ( $\rightarrow$ missing $E_T$ + hard tau)
Signal with flavor violation	Variations of lifetime and lepton p distribution	Energetic e (or $\mu$ ) with small BR
Cosmological effects	<ul style="list-style-type: none"><li>• Solving Li6 (Li7) problem</li><li>• Over-production of D</li></ul>	<ul style="list-style-type: none"><li>• Solving Li6 problem</li><li>• gravitino problem</li></ul>

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Necessary to have correct pictures of these signals and effects in each case for precise understanding of the stau

# Outline

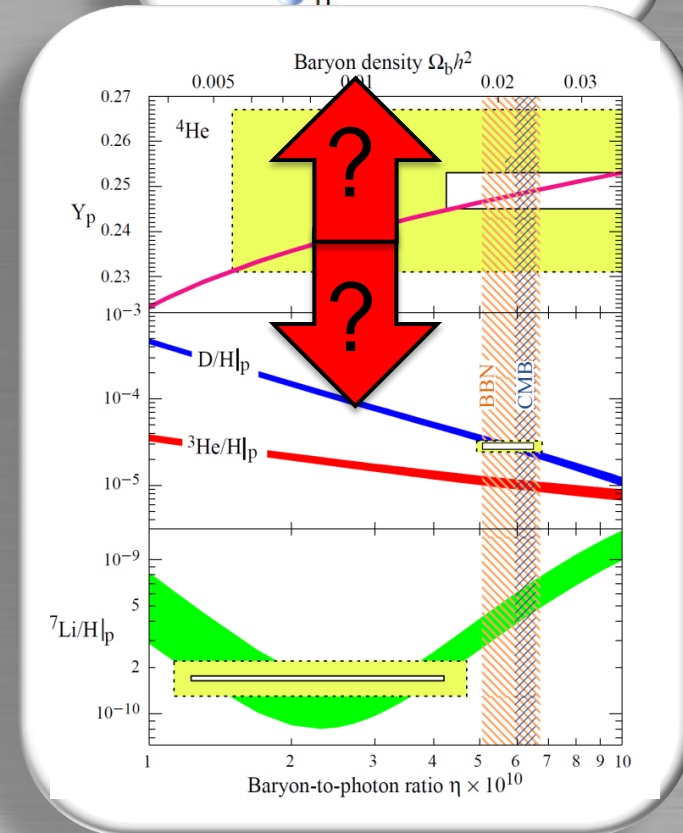
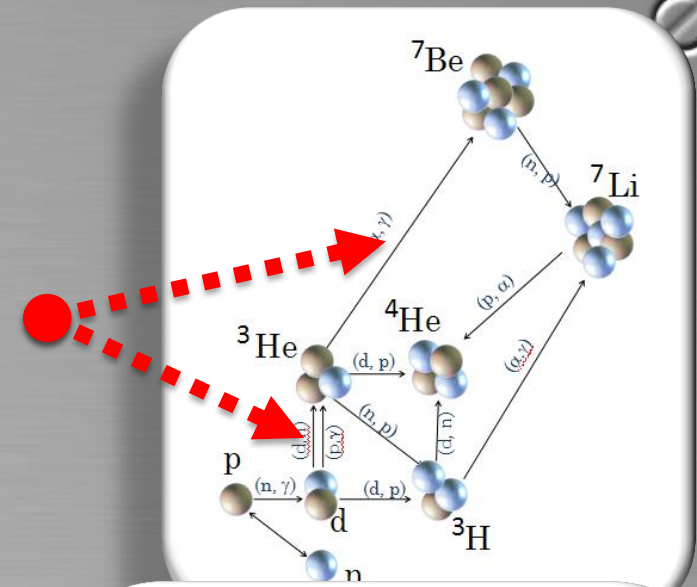
- ☑ Long-lived CHAMP in BBN
  - Energetic decay
  - Exotic nuclear reaction by bound state
  
- ☑ Long-lived CHAMP at collider
  - Flavor conserved stau
  - Flavor violating stau
  
- ☑ Summary

Long-lived CHAMP in  
big-bang nucleosynthesis (BBN)

# Various effects on BBN

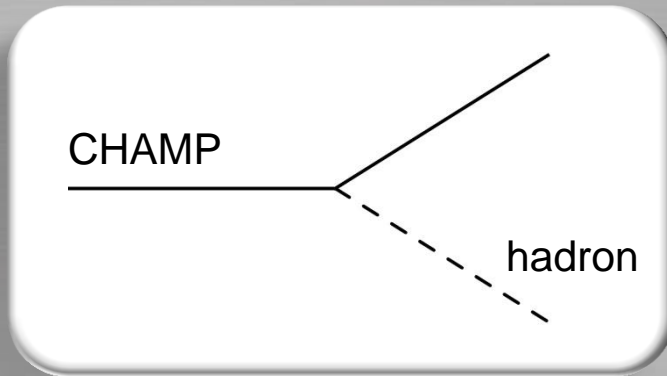
## Exotic interactions

- ☑ Over-production (-destruction) of light elements by long-lived CHAMPs
- ☑ Good accuracy of observations and calculations of light elements densities
- ☑ BBN is good probe to long-lived CHAMPs

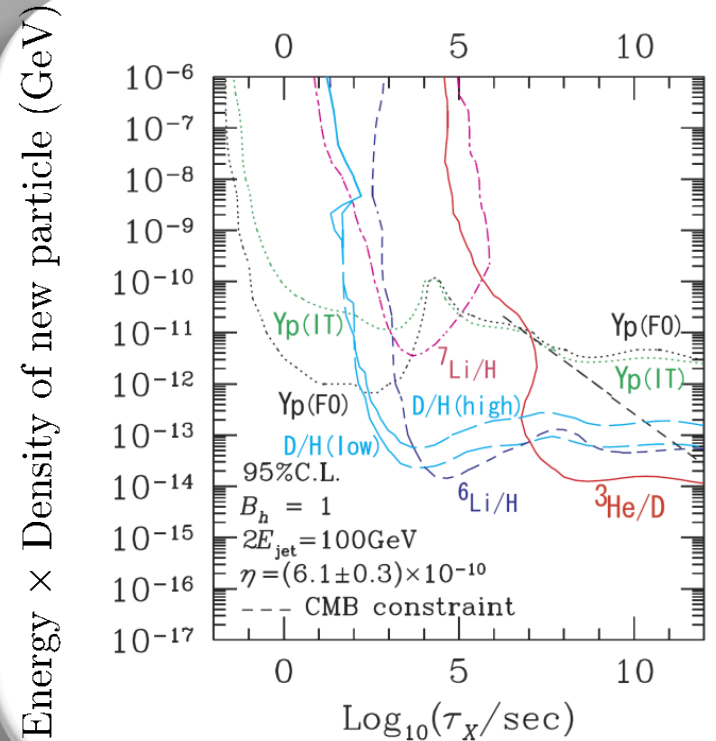




# Ex. 1: hadronic energy injection



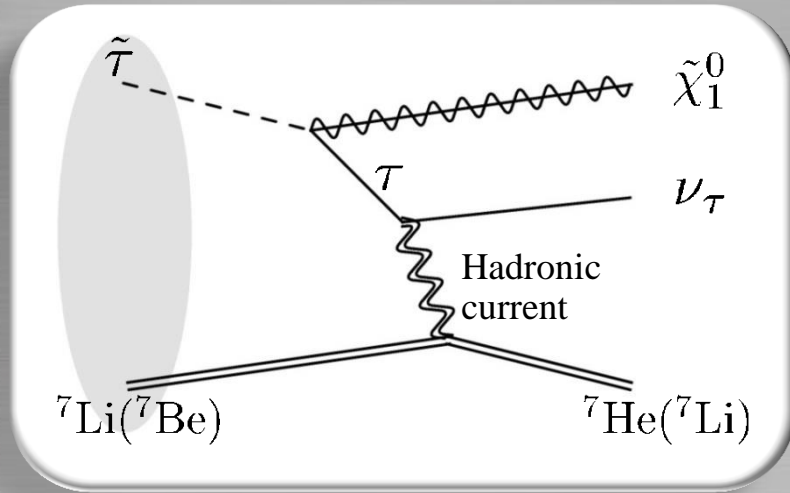
- ☑ Over-production (-destruction) of light elements by decay products
- ☑ Lifetime of hadronic decay and hadronic energy are constrained



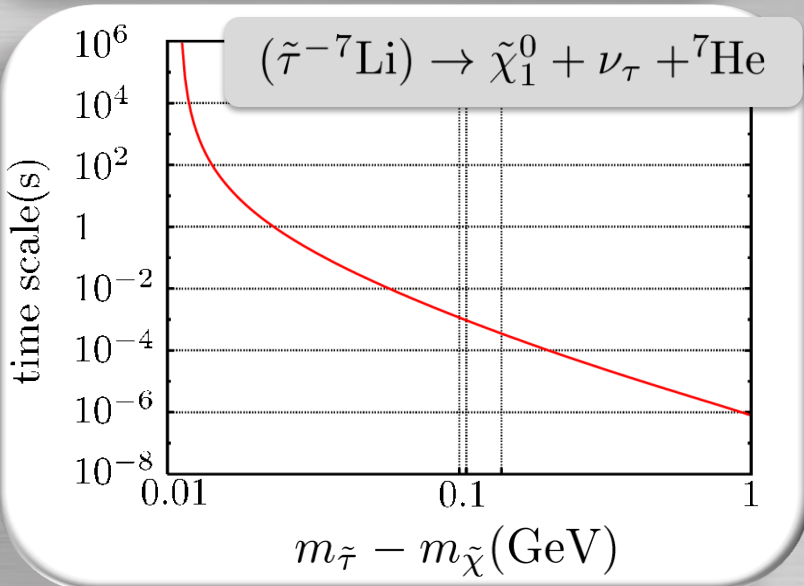
[M. Kawasaki, K. Kohri and T. Moroi (2005)]

# Ex. 2: internal conversion process

[T. Jittoh, K. Kohri, M. Koike, J. Sato, T. Shimomura and MY (2007)]



- ☑ Bound state formation of nucleus and negative charged stau
- ☑ Nuclear transformation in the bound state of nucleus and stau  
[ cf. muon capture ]



- ☑ Solving the  ${}^7\text{Li}$  problem by rapid reduction of  ${}^7\text{Li}$  and  ${}^7\text{Be}$

Discrepancy between calc. and obs.

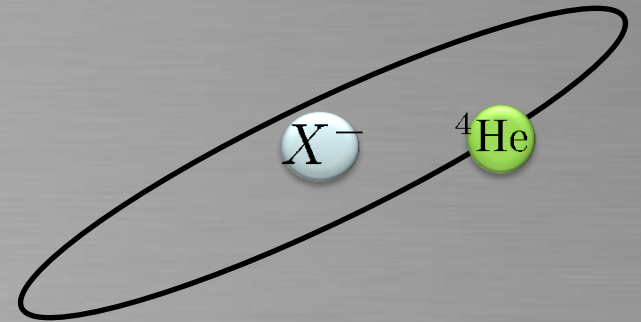
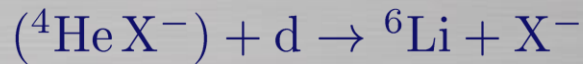
$$\text{Calc. } {}^7\text{Li}/\text{H} = (4.15^{+0.49}_{-0.45}) \times 10^{-10}$$

$$\text{Obs. } {}^7\text{Li}/\text{H} = (1.26^{+0.29}_{-0.24}) \times 10^{-10}$$

# Ex. 3: catalyzed fusion process

[M. Pospelov, PRL98]

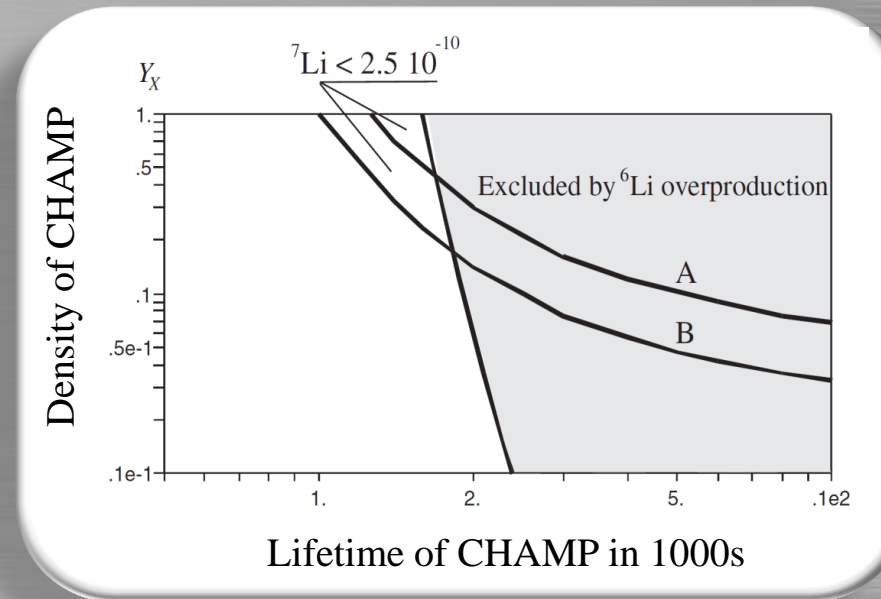
- ☑ Catalyzed fusion by the bound state of CHAMP ( $X^-$ ) and  ${}^4\text{He}$



- ☑ Solving the  ${}^6\text{Li}$  problem by enhancements of  ${}^6\text{Li}$  production

$$\frac{\langle \sigma v \rangle_{\text{catalyzed}}}{\langle \sigma v \rangle_{\text{standard}}} \simeq 10^7$$

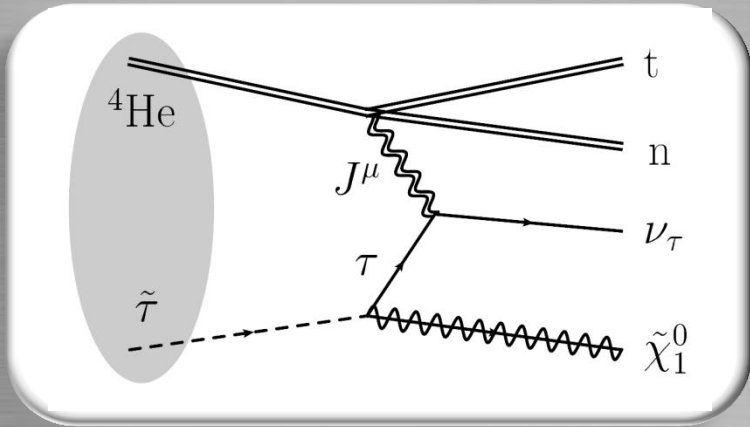
- ☑ Note: valid constraint only on gravitino dark matter scenario



[C. Bird, K. Koopmans and M. Pospelov, PRD78]

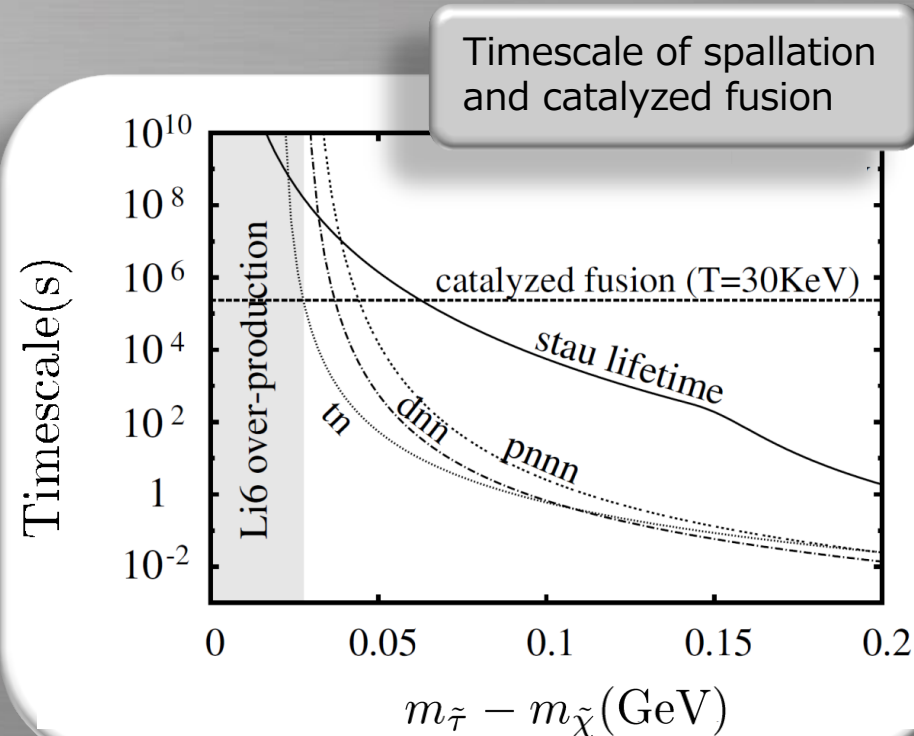
# Ex. 4: spallation process

[T. Jittoh, K. Kohri, M. Koike, J. Sato, K. Sugai, MY, and K. Yazaki (2011)]



- ☑ Spallation of He nucleus in the bound state, producing triton, deuteron, and neutron

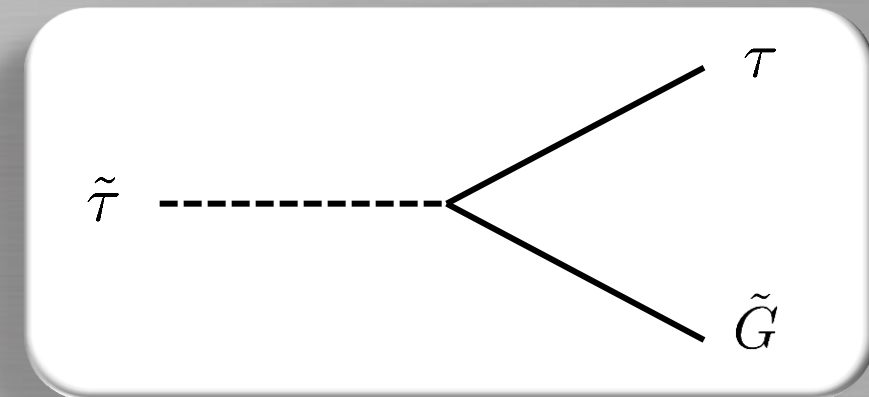
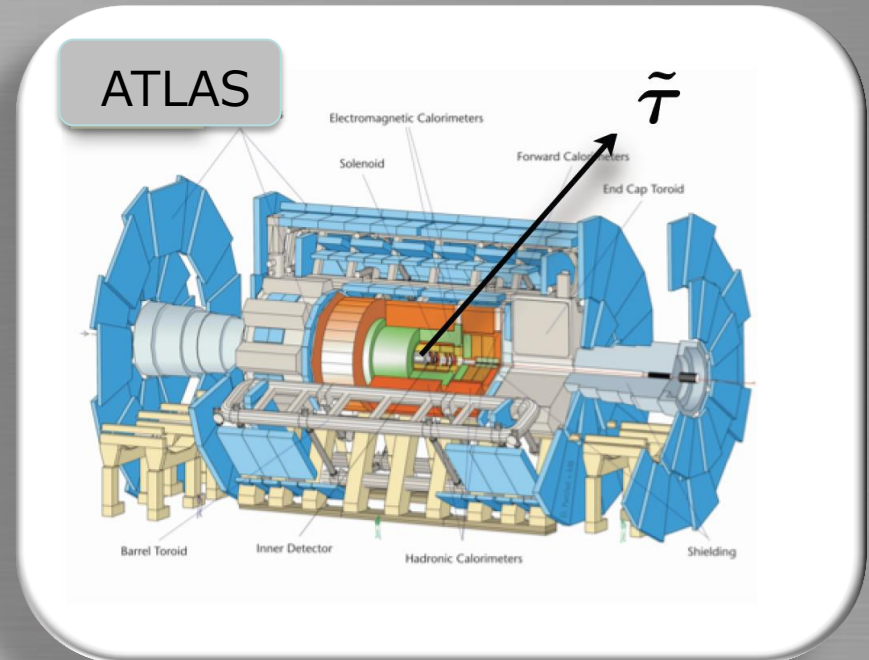
- ☑ Larger reaction rate than catalyzed fusion
- ☑ More stringent constraint to avoid over-production of deuteron



Long-lived CHAMP at collider

# Signal in gravitino DM scenario

- ☑ Signal
  - Heavy charged track
  - ( ■ Energetic tau + missing energy )
  
- ☑ Information from signals
  - Stau mass
  - SUSY breaking scale
  
- ☑ With flavor violation
  - No variation of stau lifetime
  - ( ■ Energetic e (or  $\mu$ ) with small BR )

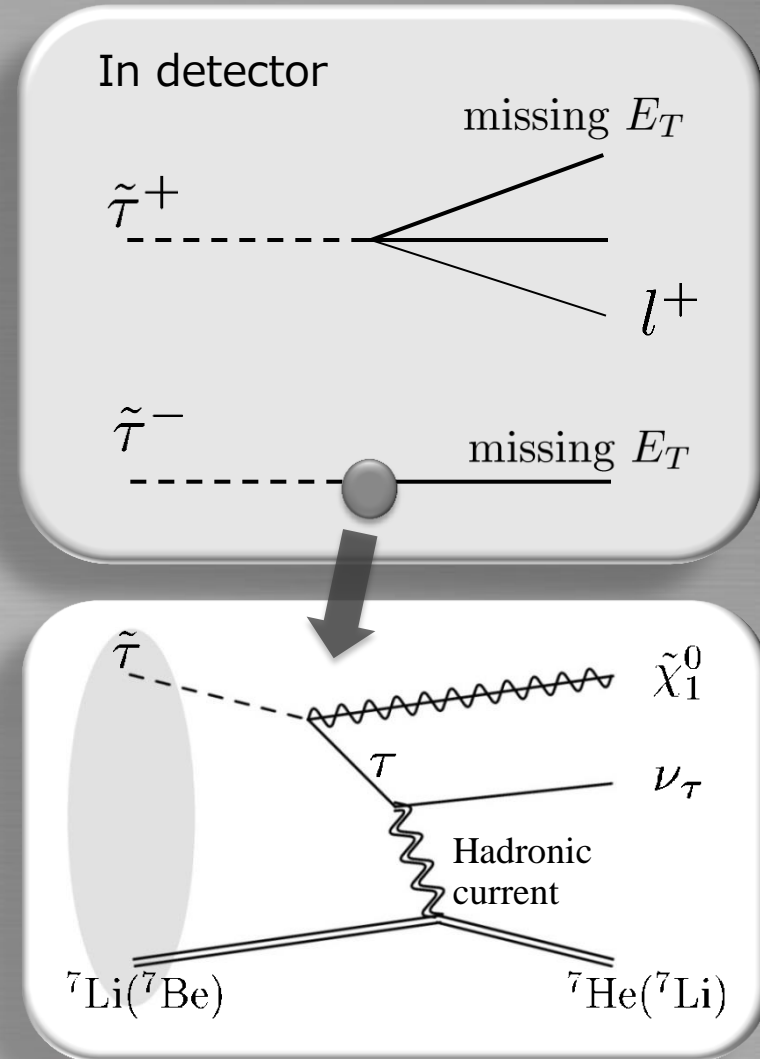




# Signal in neutralino DM scenario

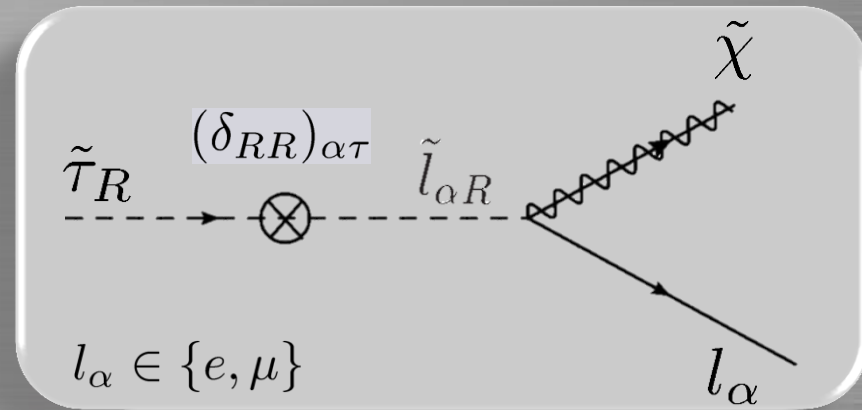
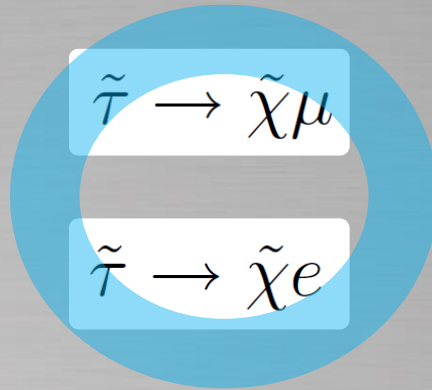
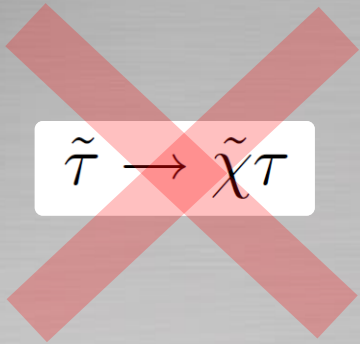
(flavor consrving)

- ☑ Bound state formation of negative charged stau and material in detector
- ☑ Internal conversion before particle decay  
[cf. muon capture process]
- ☑ Signal: missing  $E_T$  + positive track  
**No negative charged track!**
- ☑ Necessary to carefully search the signal to avoid misidentification  
[Now preparing to submit]

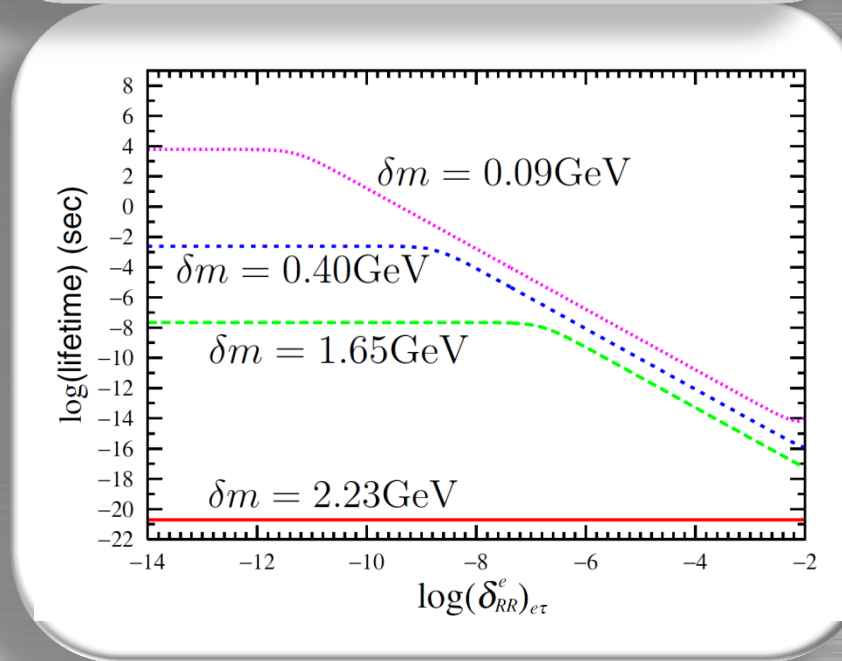


# Signal in neutralino DM scenario

(flavor violating)



- ☑ New 2-body decay channel via flavor violation
- ☑ Determination of flavor violating para. as a function of stau lifetime
- ☑ More sensitive to tiny violation than rare decay search experiments





# Summary

- ☑ Long-lived charged massive particles in many models beyond SM
  
- ☑ Important for comprehension of long-lived CHAMPs and each model
  - to identify what exotic reactions are induced by each type of CHAMP
  - to understand what light elements are over-produced (-destroyed) by each type of reactions
  
- ☑ Necessary for detecting CHAMP signal at collider to arrange depending on
  - the reason of longevity
  - the flavor is conserving or violating

Backup slides

# ${}^7\text{Li}$ problem

- ☑ Prediction

$${}^7\text{Li}/\text{H} = (4.15^{+0.49}_{-0.45}) \times 10^{-10}$$

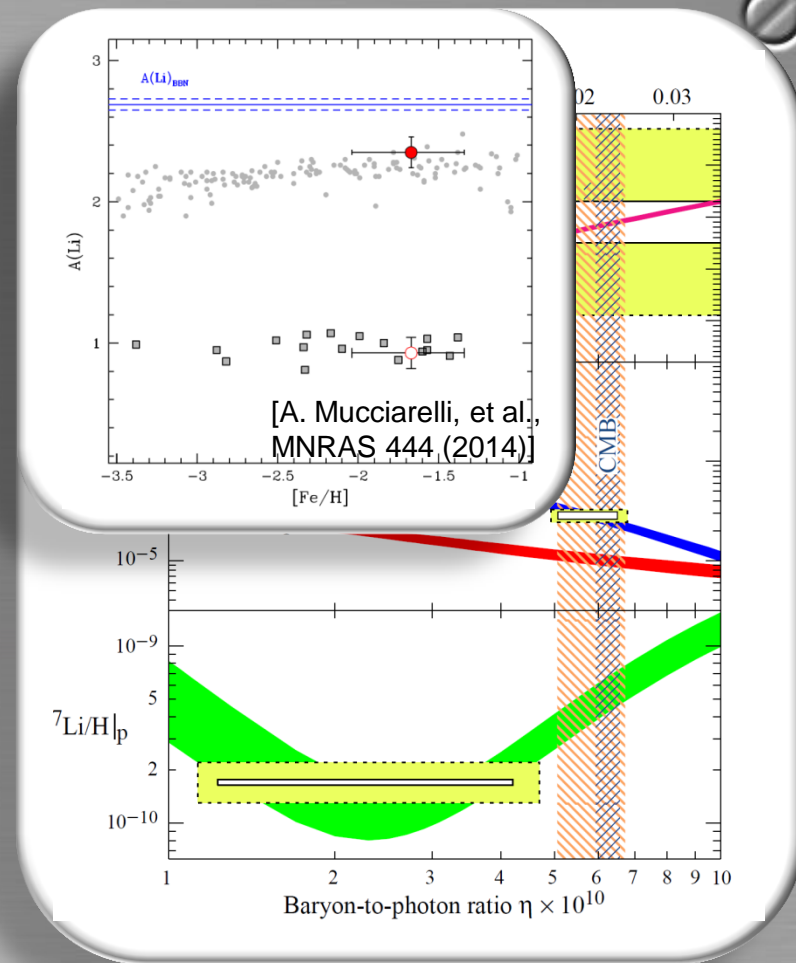
- ☑ Observation

$${}^7\text{Li}/\text{H} = (1.26^{+0.29}_{-0.24}) \times 10^{-10}$$

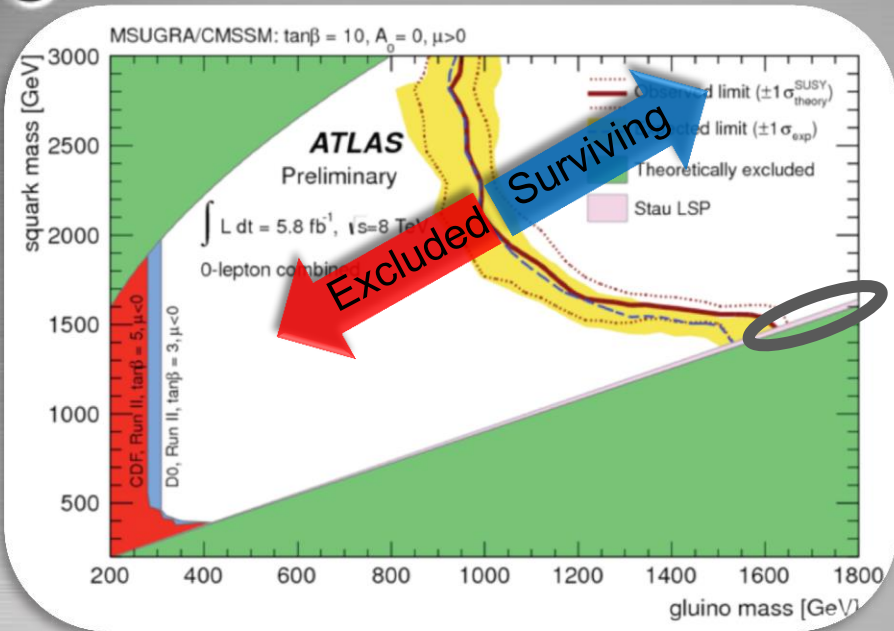
- ☑ Discrepancy:  ${}^7\text{Li}$  problem

- ☑ No solutions by modifying nucleus reaction rates

- ☑ Find mechanism to reduce both  ${}^7\text{Li}$  and  ${}^7\text{Be}$  at the BBN epoch



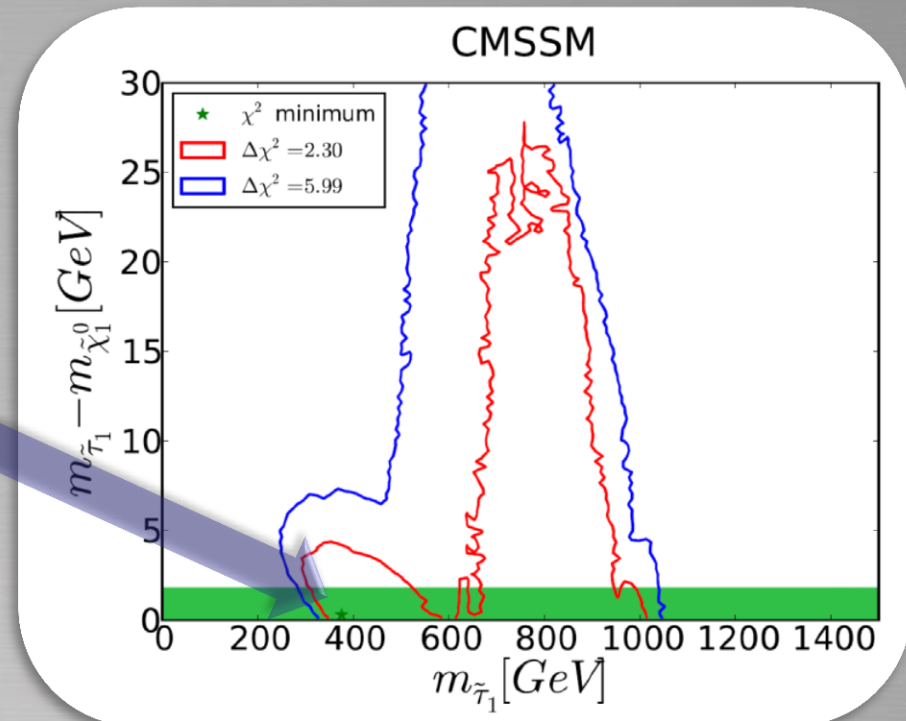
# Long-lived stau in CMSSM



- ☑ Consistent with DM abundance
- ☑ DM and stau are degenerated

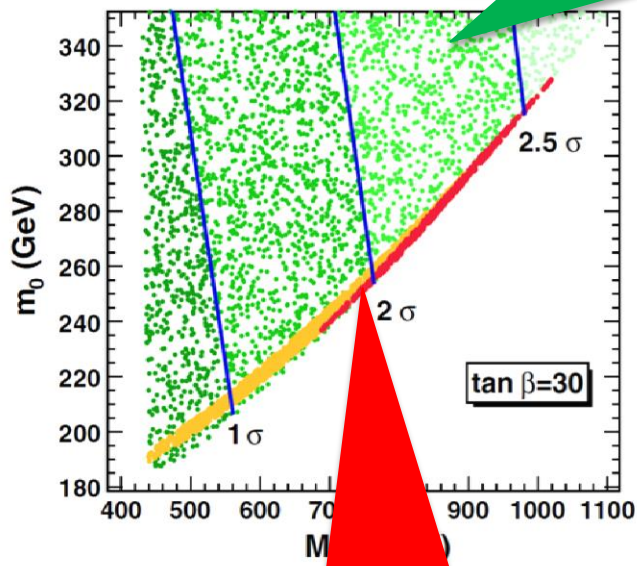
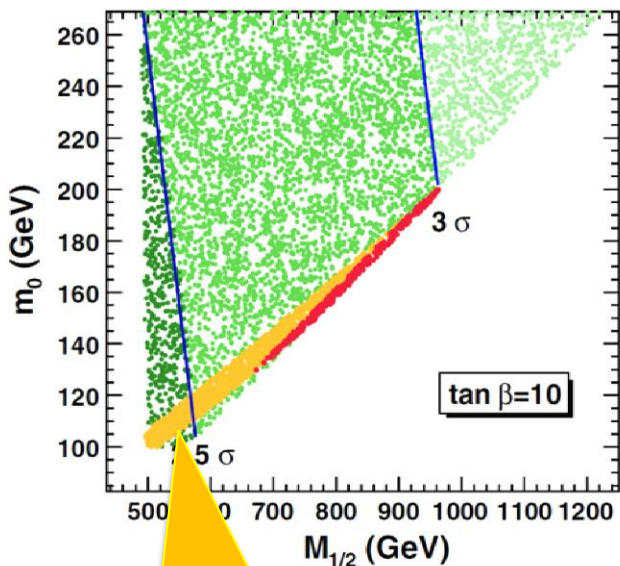
☑ Point favored from Higgs mass, DM physics, and so on

☑ Requirement:  $\delta m < m_{\tau}$



# Coannihilation region

暗黒物質残存量の  
観測値出せず



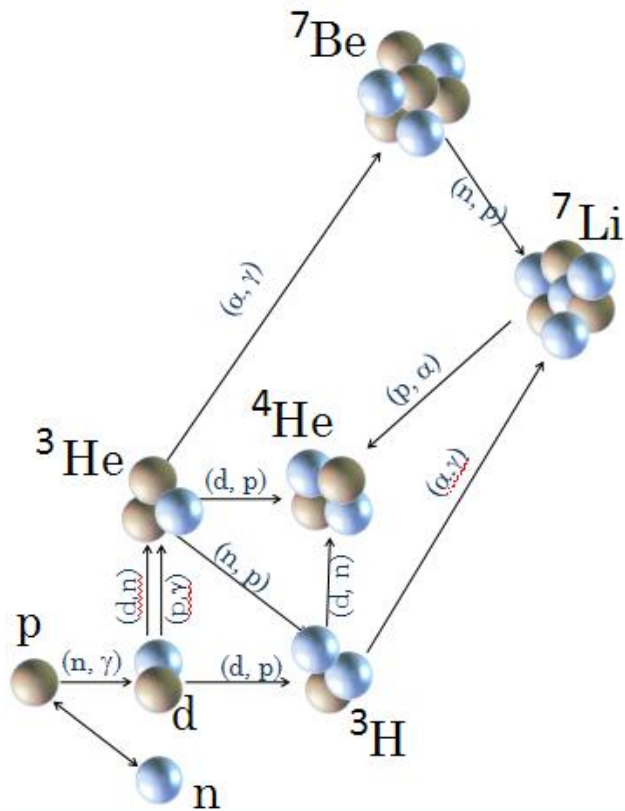
- ☑ 暗黒物質残存量OK
- ☑  $\delta r > m_\tau$

- ☑ 暗黒物質残存量OK
- ☑  $\delta m < m_\tau$

- ☑ Coannihilation region  
をズームアップ
- ☑ ポイントをランダムに  
振ってチェック
- ☑ 許容領域の大部分で  
 $\delta m < m_\tau$

$$\delta m = m_{\tilde{\tau}_R} - m_{\tilde{\chi}} : \text{ダークマターとスタウの質量差}$$

# Big-bang nucleosynthesis (BBN)



☑ Production of light elements

☑ Era: 1sec - 3min

☑ Parameter: baryon density

■ Densities of p and n

■ Ratio of p and n

☑ Input: reaction rates of nuclei



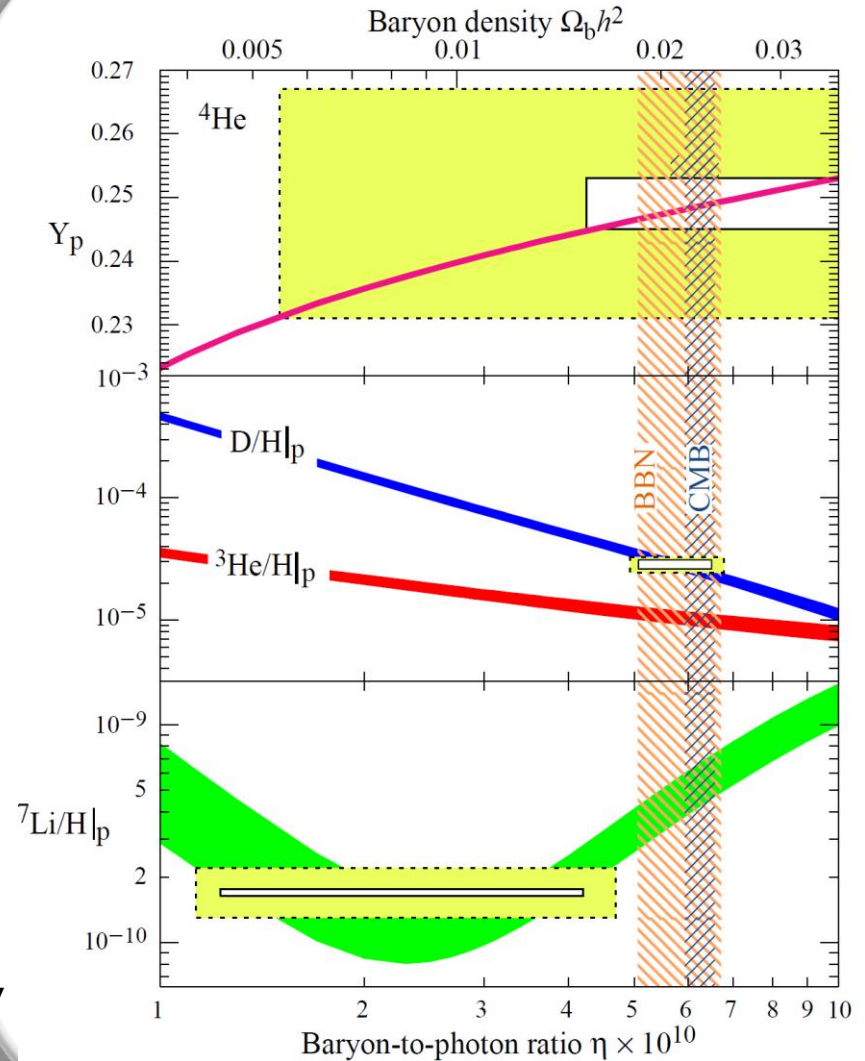
# Big-bang nucleosynthesis (BBN)

- ☑ Light elements densities are predicted for a baryon density
- ☑ Evidence for the success of the big-bang theory

Curve: theoretical prediction

Box: observation

Vertical band: observed baryon density



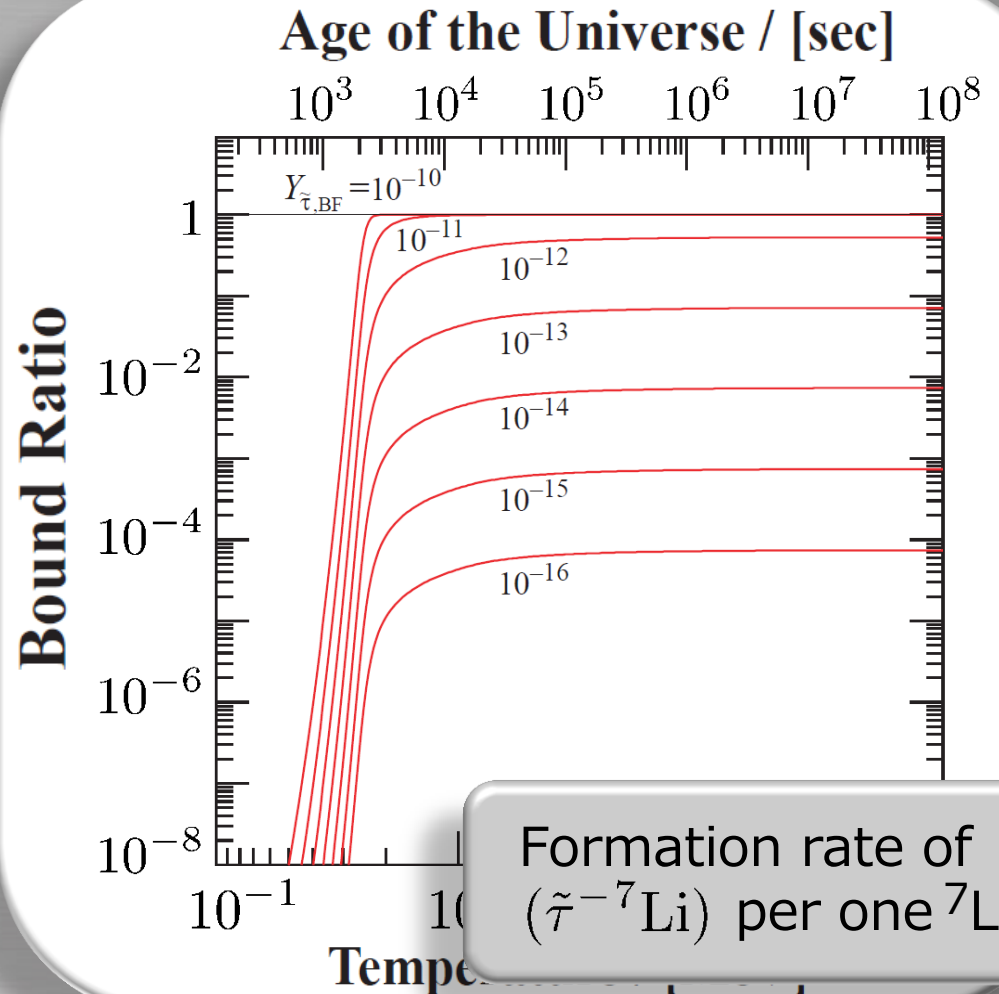
# Required lifetime and density

- Required lifetime to form the bound state?

$$\text{Lifetime} \gtrsim 1000(\text{s})$$

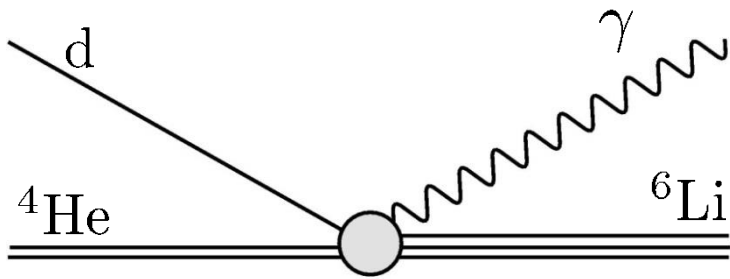
- Required density is to sufficiently reduce  ${}^7\text{Li}$ ?

$$Y_{\tilde{\tau}} \gtrsim 2 \times 10^{-12}$$

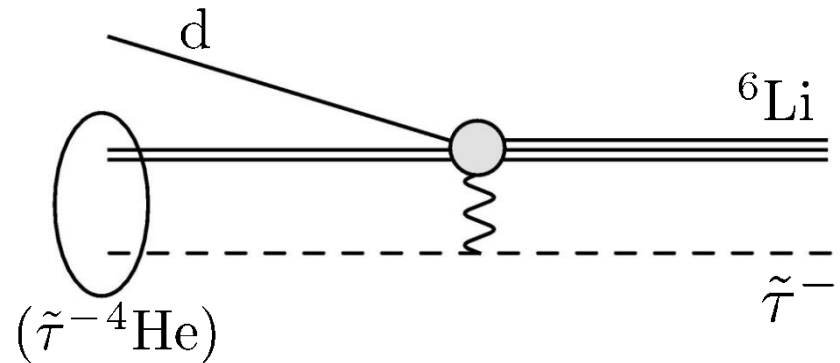




# Catalyzed fusion



Standard BBN reaction



Catalyzed BBN reaction

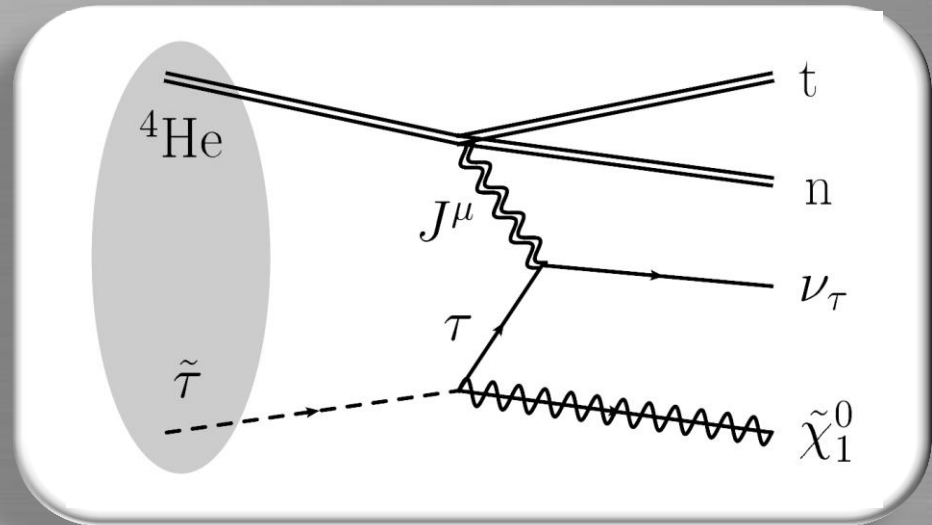
- ☑ Exotic reaction induced by the bound state ( $\tilde{\tau}^{-4}\text{He}$ )
- ☑  **${}^6\text{Li}$  over-production**

$$\frac{\langle \sigma v \rangle_{\text{catalyzed}}}{\langle \sigma v \rangle_{\text{standard}}} \simeq 10^7 \quad \left( \begin{array}{l} \dots \text{ Standard: forbidden E1 transition} \\ \dots \text{ Catalyzed: } \alpha \text{ transfer reaction} \end{array} \right)$$

# Spallation process

[T. Jittoh, K. Kohri, M. Koike, J. Sato, K. Sugai, K. Yazaki, and MY, PRD84 (2011)]

- ☑ Origin of stau's longevity: phase space suppression
- ☑ Spallation process after forming a bound state



Overlap of initial state wave function

Reaction rate  $\Gamma((\tilde{\tau} {}^4\text{He}) \rightarrow \tilde{\chi}_1^0 \nu_\tau t n) = |\psi|^2 \cdot \sigma v_{tn}$

Cross section of elemental reaction

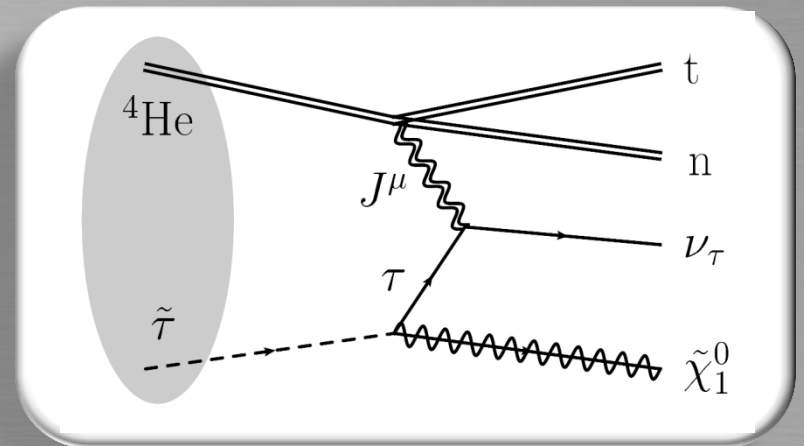
# Cross section of elemental reaction

## ☑ Cross section of elemental reaction

$$\sigma v_{\text{tn}} = \frac{1}{2E_{\tilde{\tau}}} \int \frac{d^3 \mathbf{p}_\nu}{(2\pi)^3 2E_\nu} \frac{d^3 \mathbf{p}_{\tilde{\chi}}}{(2\pi)^3 2E_{\tilde{\chi}}} \frac{d^3 \mathbf{q}_n}{(2\pi)^3} \frac{d^3 \mathbf{q}_t}{(2\pi)^3} \\ \times |\mathcal{M}((\tilde{\tau}^4\text{He}) \rightarrow \tilde{\chi}_1^0 \nu_\tau \text{tn})|^2 (2\pi)^4 \delta^{(4)}(p_{\tilde{\tau}} + p_{\text{He}} - p_\nu - q_t - q_n)$$

## ☑ Amplitude

$$\mathcal{M}((\tilde{\tau}^4\text{He}) \rightarrow \tilde{\chi}_1^0 \nu_\tau \text{tn}) \\ = \langle \text{tn} \tilde{\chi}_1^0 \nu_\tau | \mathcal{L}_{\text{int}} | ^4\text{He} \tilde{\tau} \rangle \\ = \langle \text{tn} | J^\mu | ^4\text{He} \rangle \langle \tilde{\chi}_1^0 \nu_\tau | j_\mu | \tilde{\tau} \rangle$$



leptonic part; calculated straightforwardly

# Hadronic matrix element

- Building up wave functions of  ${}^4\text{He}$ , t, d, and n

Requirement: anti-symmetric under the exchange of two nucleons

spin, isospin part  
(anti-symmetric)

$$|{}^4\text{He}\rangle = \frac{1}{2\sqrt{6}} [ |pnpn\rangle ( |\uparrow\uparrow\downarrow\downarrow\rangle + |\downarrow\downarrow\uparrow\uparrow\rangle - |\uparrow\downarrow\downarrow\uparrow\rangle - |\downarrow\uparrow\uparrow\downarrow\rangle ) \\ + \dots\dots + |nnpp\rangle ( -|\uparrow\downarrow\uparrow\downarrow\rangle + |\uparrow\downarrow\downarrow\uparrow\rangle + |\downarrow\uparrow\uparrow\downarrow\rangle - |\downarrow\uparrow\downarrow\uparrow\rangle ) ]$$

spatial part  
(symmetric)

$$\psi_{\text{He}}(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3, \mathbf{r}_4) = \left( 2 \frac{a_{\text{He}}^3}{\pi^3} \right)^{3/4} \\ \times \exp \left\{ -a_{\text{He}} \left[ \mathbf{r}_1^2 + \mathbf{r}_2^2 + \mathbf{r}_3^2 + \mathbf{r}_4^2 - \frac{1}{4} (\mathbf{r}_1 + \mathbf{r}_2 + \mathbf{r}_3 + \mathbf{r}_4)^2 \right] \right\}$$

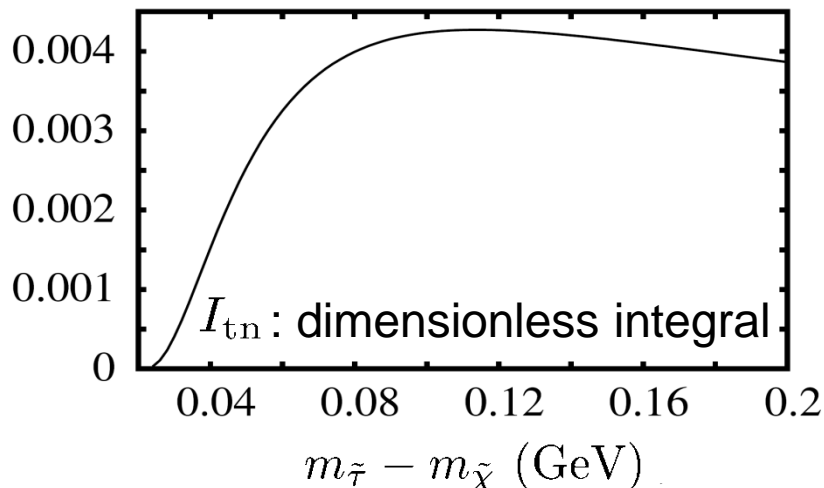
$$a_{\text{He}} = \frac{9}{16} \frac{1}{(R_m)_{\text{He}}^2}, \quad a_t = \frac{1}{2} \frac{1}{(R_m)_t^2} \quad (R_m : \text{matter radius})$$

# Cross section

## Cross section of elemental reaction

$$\sigma v_{tn} = \frac{8}{\pi^2} \left( \frac{32}{3\pi} \right)^{3/2} g^2 \tan^2 \theta_W \sin^2 \theta_\tau (1 + 3g_A^2) G_F^2$$

$$\times \Delta_{tn}^4 \frac{m_t m_n}{m_{\tilde{\tau}} m_\tau^2} \frac{a_{\text{He}}^{3/2} a_t^3}{(a_{\text{He}} + a_t)^5} I_{tn}$$



$$\Delta_{tn} \equiv m_{\tilde{\tau}} - m_{\tilde{\chi}} + \Delta_{\text{He}} - \Delta_t - \Delta_n - E_b$$

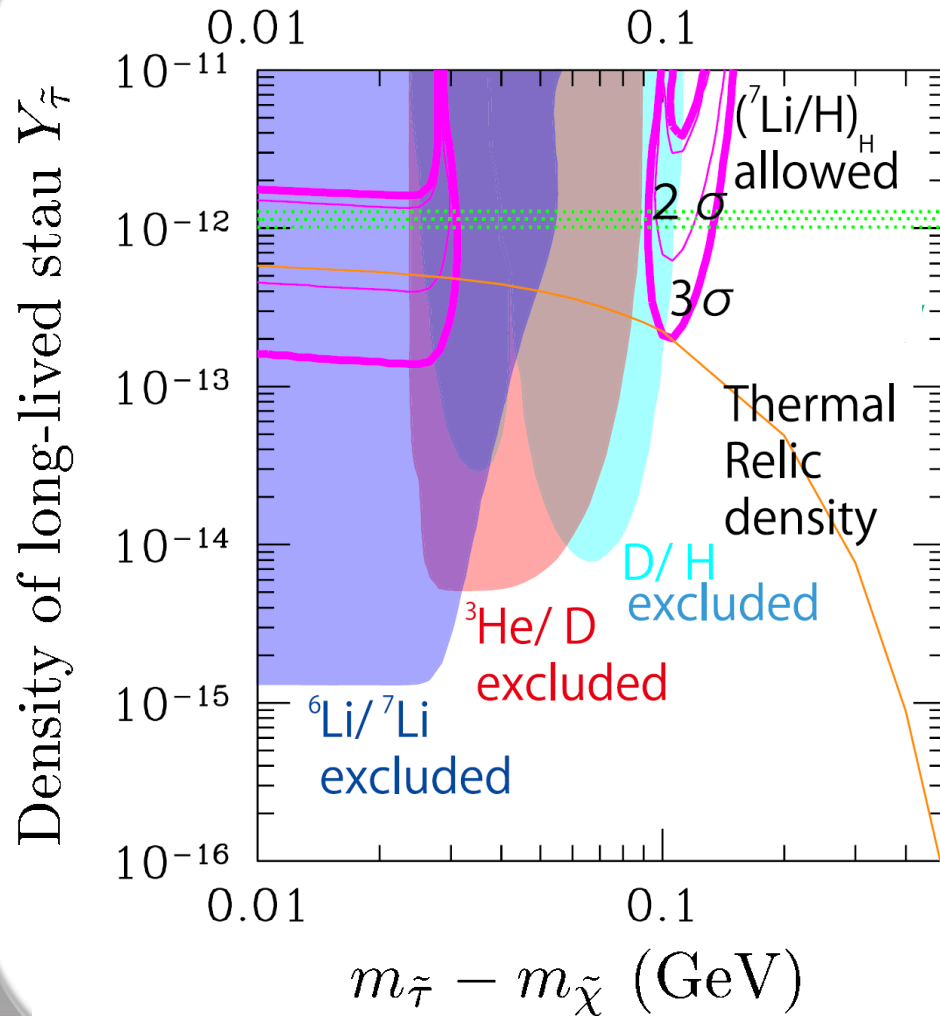
$$\Delta_{\text{He}} = m_{\text{He}} - 4A,$$

$$\Delta_t = m_t - 3A,$$

$$\Delta_n = m_n - A$$

$A$ : Unified atomic mass unit

# Prediction of property of the stau

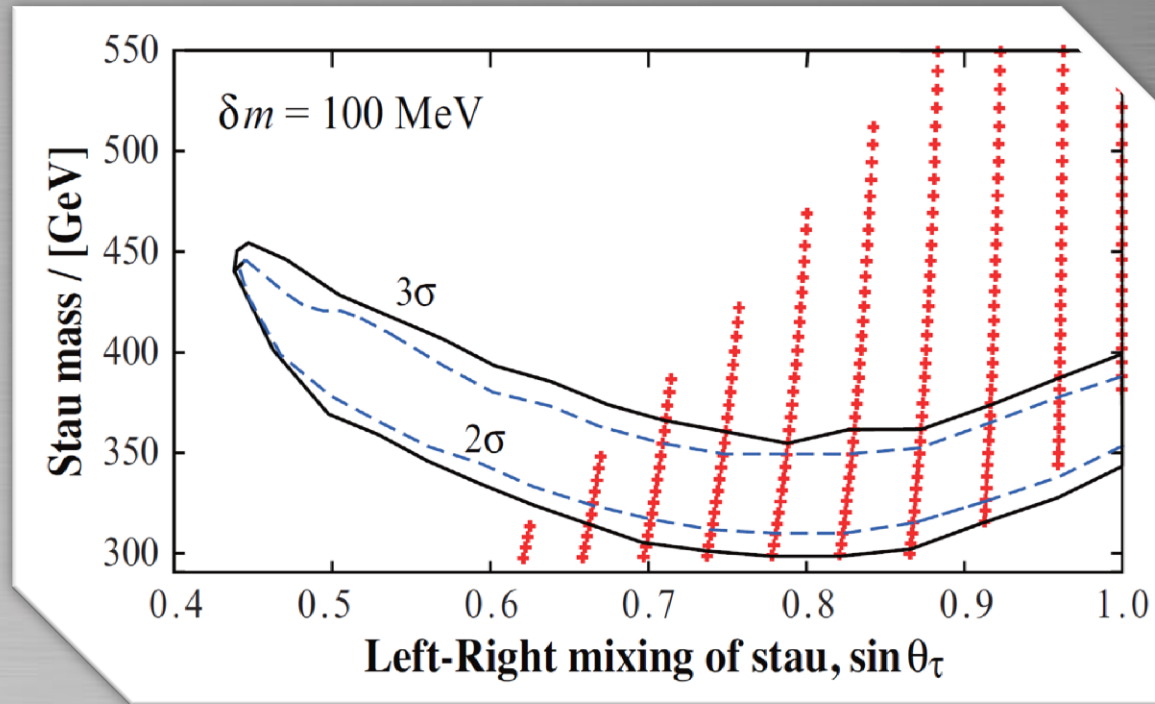


Region surrounded by purple line:  
Consistent with observed  ${}^7\text{Li}$

Solid line (orange line):  
Relic density of long-lived stau

Colored region:  
excluded by over-production

# Prediction on the long-lived stau



Region in solid line:  
Consistent with observed  
dark matter abundance

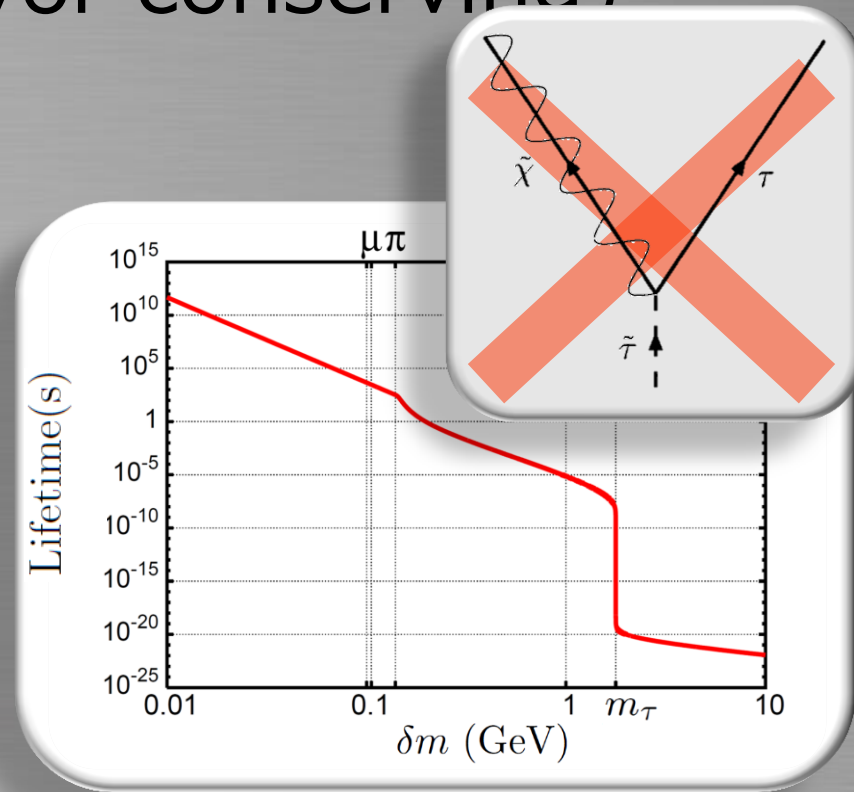
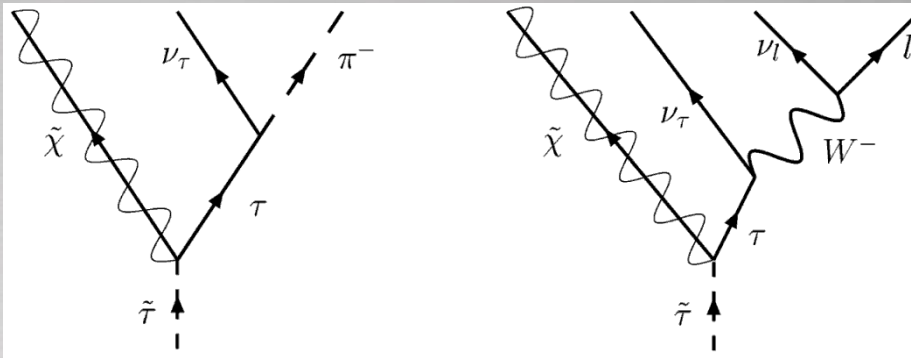
Red cross points:  
Consistent with observed  
light elements abundance



# Collider signal (flavor conserving)

- ☑  $\delta m < m_\tau$  の領域では位相空間の抑圧によりスタウNLSPが長寿命化

- ☑ 可能な崩壊モード

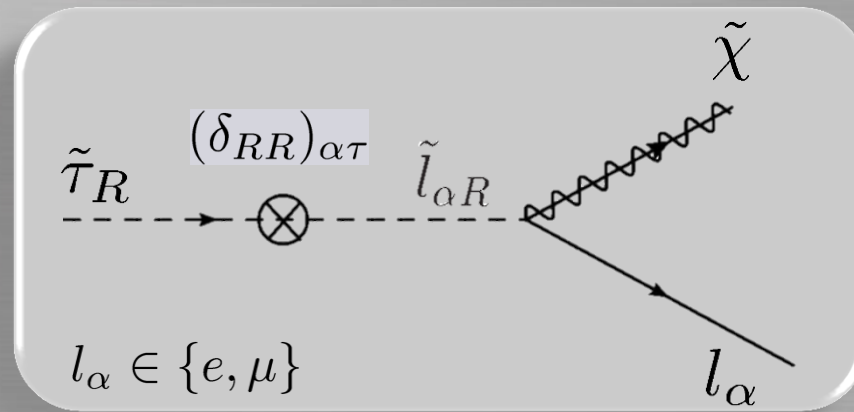


- ☑ 期待されるシグナル: ほとんどのスタウは既存の検出器を突き抜ける  
もし検出器内で崩壊すれば、ソフトなレプトン

- ☑ 既存の検出器の外に、ストッパー兼検出器が必要となりそう



# Collider signal (flavor violating)



$$\Gamma(\tilde{\tau}_R \rightarrow \tilde{\chi} l_\alpha) = \frac{g_2^2}{2\pi m_{\tilde{\tau}_R}} |g_{\tau\alpha}|^2 (\delta m)^2$$

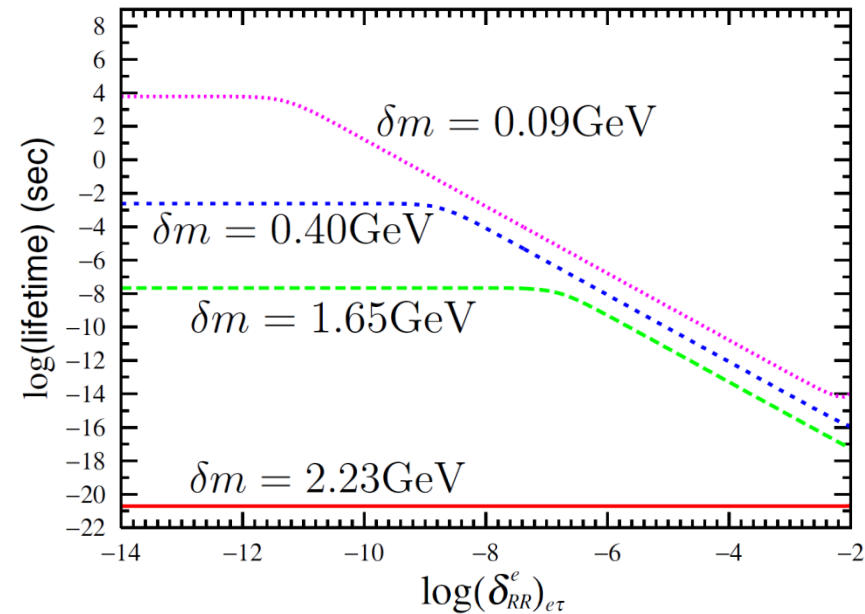
$$g_{\tau\alpha} = \tan \theta_W \frac{M_{R\tau} M_{R\alpha}}{M_{R\tau}^2 - M_{R\alpha}^2} (\delta_{RR}^e)_{\alpha\tau}$$

$$(\delta_{RR})_{\alpha\tau} = \frac{\Delta M_{RR\alpha\tau}^2}{M_{R\alpha} M_{R\tau}}$$

# Signal in neutralino DM scenario (flavor violating)

$\beta\gamma = 2$

	5 cm	50 cm	3.1 m	5.8 m	25.0 m
$10^{-5}$ sec	0.04	0.36	2.2	4.1	17.8
$10^{-6}$ sec	0.36	3.6	22.1	41.3	175.1
$10^{-7}$ sec	3.6	35.6	216.0	395.3	1461.9
$10^{-8}$ sec	35.6	343.0	1731.0	2658.3	4223.5
$10^{-9}$ sec	343.0	2425.6	4265.5	4289.7	4290.0
$10^{-10}$ sec	2425.6	4289.0	4290.0	4290.0	4290.0
$10^{-11}$ sec	4289.0	4290.0	4290.0	4290.0	4290.0
$10^{-12}$ sec	4290.0	4290.0	4290.0	4290.0	4290.0



## ☑ 質量差がタウ質量以下の場合

- 寿命測定により世代混合を決定
- かなり小さな世代混合も決定可能

検出器内のスタウ飛跡の数え上げ  
(ある距離までに崩壊する数)

# Lifetime in gravitino DM scenario

$$\Gamma(\tilde{\tau} \rightarrow \tilde{G}\tau) \simeq \frac{m_{\tilde{\tau}}^5}{48\pi m_{\tilde{G}}^2 M_{\text{pl}}^2} \left(1 - \frac{m_{\tilde{G}}^2}{m_{\tilde{\tau}}^2}\right)^4$$

Lifetime (decay length) of NLSP stau

e.g., for  $m_{\tilde{\tau}} = 100 \text{ GeV}$ ,

