

# Topcolor in the LHC Era

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- Top Mass and TopColor
- Effective Field Theory
- New Fermions, Top-Higgs, & Top-Pions
- What LHC Can See... and Has **(Not)** Seen
- Conclusions

# **TOP MASS AND TOPCOLOR**

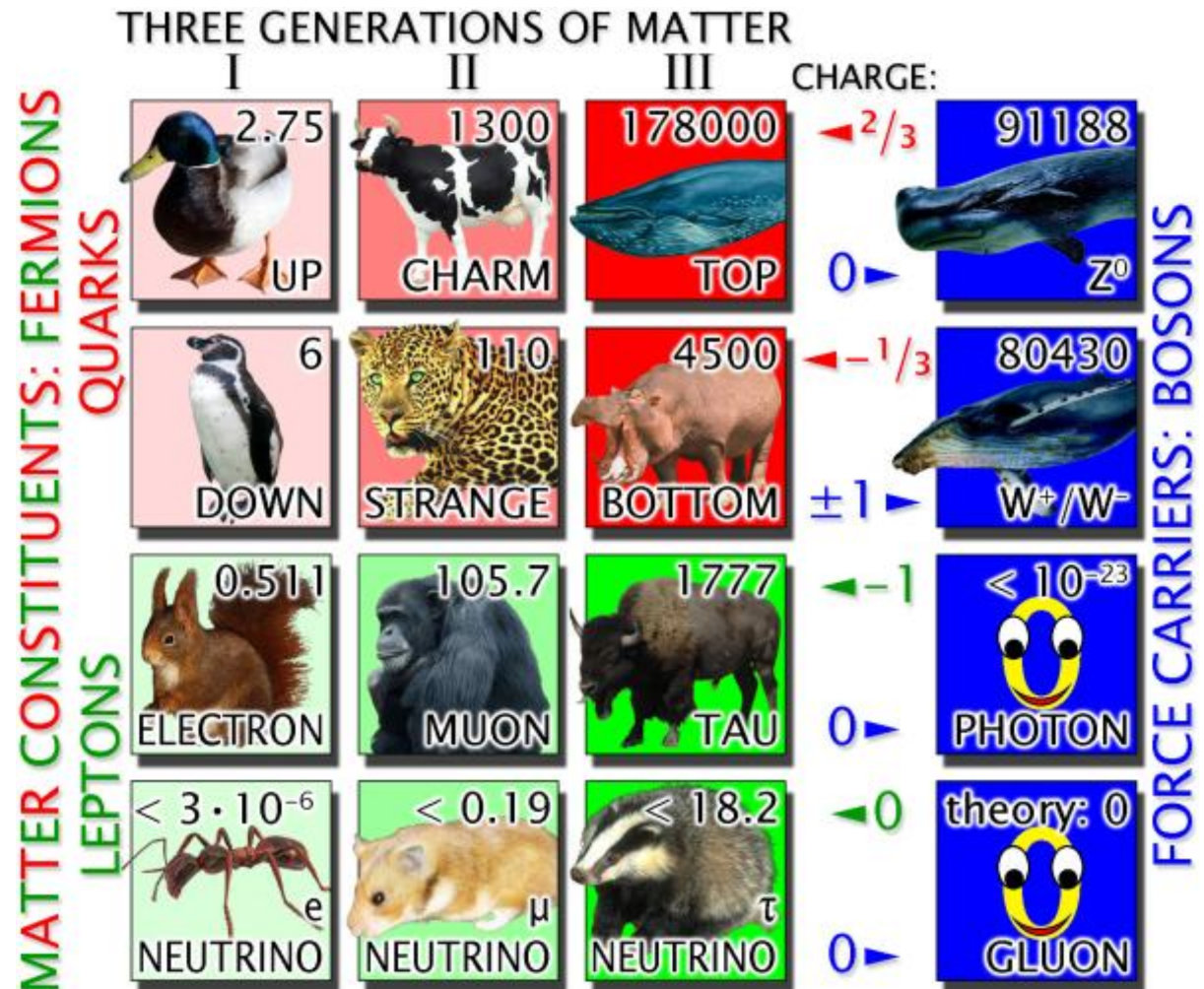
# QUESTIONS ABOUT BROKEN SYMMETRIES

## Electroweak:

**Why are the W & Z bosons heavy while the photon is massless?**

## Flavor:

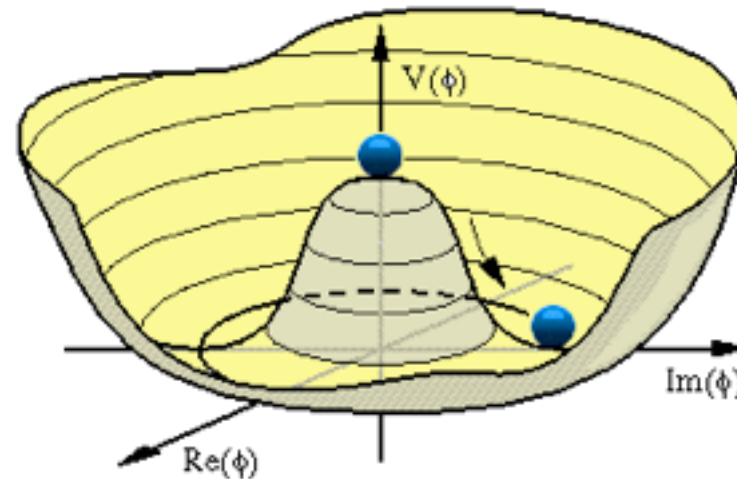
**Why do fermions with the same charge have different masses?**



ALL MASSES IN MEV;  
ANIMAL MASSES  
SCALE WITH  
PARTICLE MASSES

The Standard Model  
fundamental particle zoo

# TRIAL ANSWER: SM WITH A HIGGS DOUBLET



## Problems with the Higgs Model

- No fundamental scalars observed in nature
- No explanation of dynamics causing EWSB
- Hierarchy/Naturalness Problem  $\bigcirc$   $\Rightarrow m_H^2 \propto \Lambda^2$
- Triviality Problem...  $\bigcirc$   $\Rightarrow \beta = \frac{3\lambda^2}{2\pi^2} > 0$

# REVISED ANSWER FOR EWSB:

**Technicolor:** (as in previous talk)

Introduce  $SU(N)_{TC}$  with

**technigluons**, inspired by QCD gluons

**techniquarks** carrying  $SU(N)_{TC}$  charge:

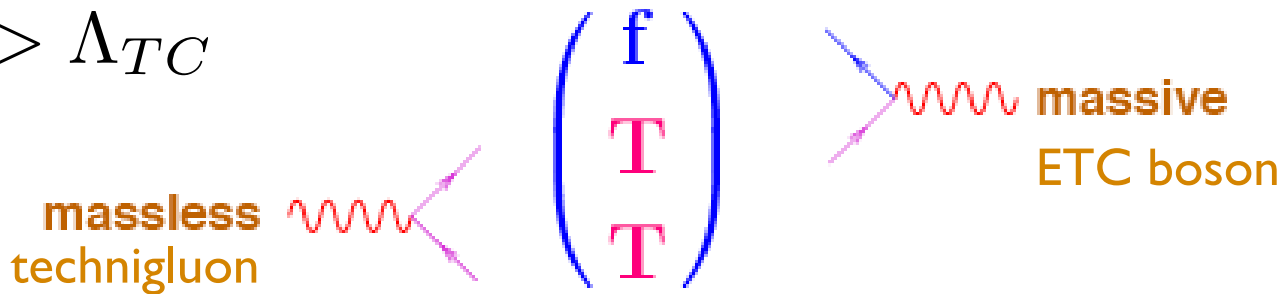
- e.g. weak doublet  $T_L = (U_L, D_L)$ ; weak singlet  $U_R, D_R$
- Lagrangian has  $SU(2)_L \times SU(2)_R$  chiral symmetry

$SU(N)_{TC}$  gauge coupling becomes large at  $\Lambda_{TC} \approx 1\text{TeV}$

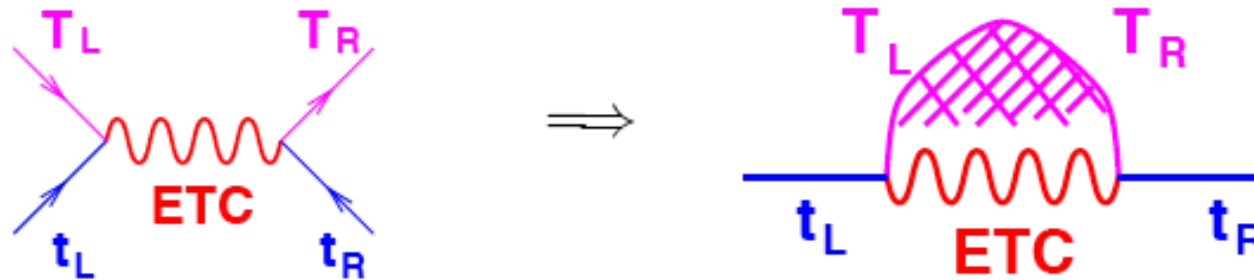
- $\langle T_L T_R \rangle \approx 250\text{ GeV}$  causes EWSB
- `technipions'  $\Pi_{TC}$  become the  $W_L, Z_L$

# REVISED ANSWER FOR FERMION MASSES: ETC\*

$$M_{ETC} > \Lambda_{TC}$$



E.g. the top quark mass arises from:



and its size is  $\left(\frac{g_{ETC}}{M_{ETC}}\right)^2 \langle \bar{T}T \rangle$  x (flavor-dependent factor)

**Challenge:** ETC must violate custodial symmetry to make  $m_t \gg m_b$ . But how to avoid large changes to  $\Delta\rho$ ?

\*Dimpoulos & Susskind; Eichten & Lane

# SIZE OF ISOSPIN VIOLATION

ETC *must* violate weak-isospin to make  $m_t \gg m_b$ .  
 ETC boson mixing with Z through technifermion loops induces dangerous contributions to  $\Delta\rho$

$$\Delta\rho \approx 12\% \cdot \left( \frac{\sqrt{N_D} F_{TC}}{250 \text{ GeV}} \right)^2 \cdot \left( \frac{1 \text{ TeV}}{M_{ETC}/g_{ETC}} \right)^2$$

How to satisfy experimental constraint:  $\Delta\rho \leq 0.4\%$ ?

- make ETC boson heavy ?

$$\frac{M_{ETC}}{g_{ETC}} > 5.5 \text{ TeV} \cdot \left( \frac{\sqrt{N_D} F_{TC}}{250 \text{ GeV}} \right)^2$$

too heavy to provide  $m_t = 172 \text{ GeV}$

- arrange for  $N_D F_{TC}^2 \ll (250 \text{ GeV})^2$  ?  
 e.g. **separate** sectors for  $m_t$  and  
 EW symmetry breaking

# TOP CONDENSATION AND EWSB

**If the top quark feels a new strong interaction,**  
a top-quark condensate  $\langle \bar{t}t \rangle \neq 0$  can provide some  
or even all of electroweak symmetry breaking

some (topcolor\*, topcolor-assisted technicolor\*)

in these models the top quark feels an additional  
gauge interaction that causes top condensation

all (top mode<sup>^</sup>, top seesaw<sup>^^</sup>)

in top seesaw models, a heavy partner quark T forms  
the condensate; the top quark mass eigenstate that we  
observe is a seesaw mixture between T and the standard  
model's top quark gauge eigenstate

\* Hill ^Bardeen,Hill &Lindner; Yamawaki; Miranski; Nambu ^^Chivukula, Dobrescu, Georgi & Hill



# PHYSICAL REALIZATION: TOPCOLOR

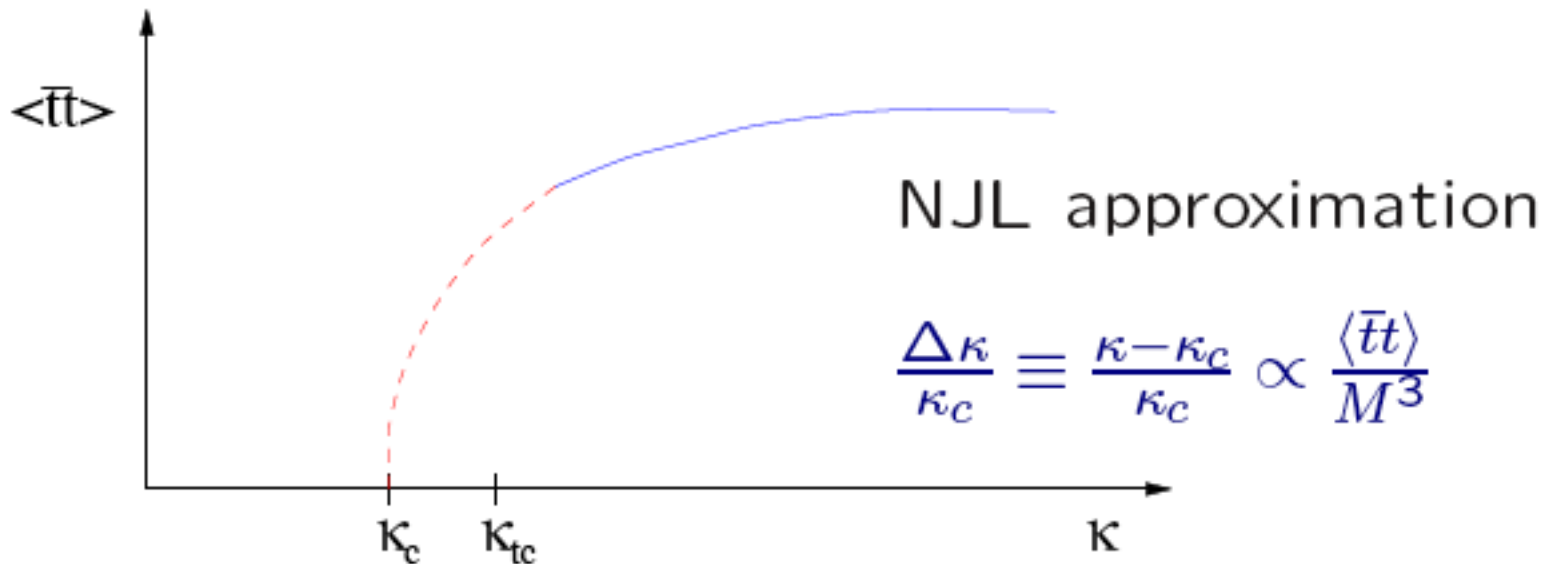
One physical realization of a new interaction for top is a (spontaneously broken) extended color gauge group: topcolor

$$SU(3)_h \times SU(3)_\ell \xrightarrow{M} SU(3)_{QCD}$$

where (t,b) feel  $SU(3)_h$  and (u,c,d,s) feel  $SU(3)_\ell$

Below the scale M, exchange of massive topgluons yields four-fermion interactions among top quarks

$$-\frac{4\pi\kappa}{M^2} \left( \bar{t} \gamma_\mu \frac{\lambda^a}{2} t \right)^2$$



Note:  
 $M \gg 1 \text{ TeV}$   
 implies fine  
 tuning

# TOPCOLOR-ASSISTED TECHNICOLOR (TC2)

$$(g_h > g_e)$$

$$(g_h > g_e)$$

$$G_{TC} \times SU(3)_h \times SU(3)_e \times SU(2)_W \times U(1)_h \times U(1)_e$$

$$\downarrow \quad M \gtrsim 1 \text{ TeV}$$

$$G_{TC} \times SU(3)_{QCD} \times SU(2)_W \times U(1)_Y$$

$$\downarrow \quad \Lambda_{TC} \sim 1 \text{ TeV}$$

$$G_{TC} \times SU(3)_{QCD} \times U(1)_{EM}$$

technicolor: provides most of EWSB

topcolor: provides most of  $m_t$

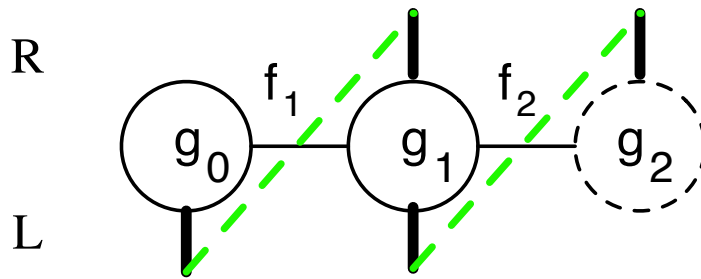
hypercharge: keeps  $m_b$  small

# **EFFECTIVE FIELD THEORY: THE TOP-TRIANGLE MOOSE**

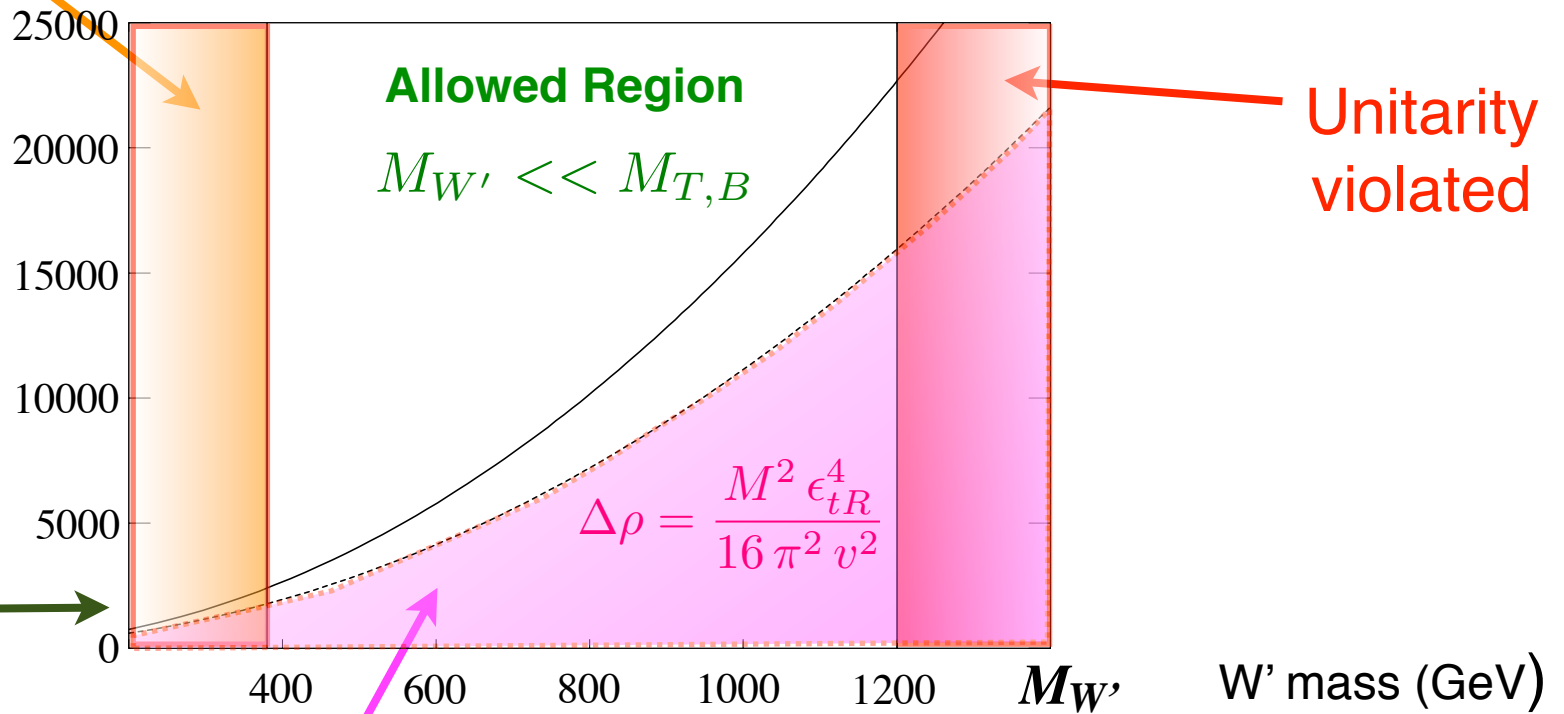
**Chivukula, Christensen, Coleppa, Simmons**  
**arXiv:0906.5667**

**Chivukula, Coleppa, Logan, Martin, Simmons**  
**arXiv:1101.6023**

# REMINDER: 3-SITE MODEL



WWZ vertex  
visibly altered



Minimum  
allowed  
fermion  
mass

1-loop fermionic EW precision  
corrections too large

# THE TOP TRIANGLE MOOSE

## Gauge structure:

$$SU(2) \times SU(2) \times U(1)$$

$$g_0, g_2 \ll g_1$$

## Top-Higgs

$$\langle \Phi \rangle = v \sin \omega$$

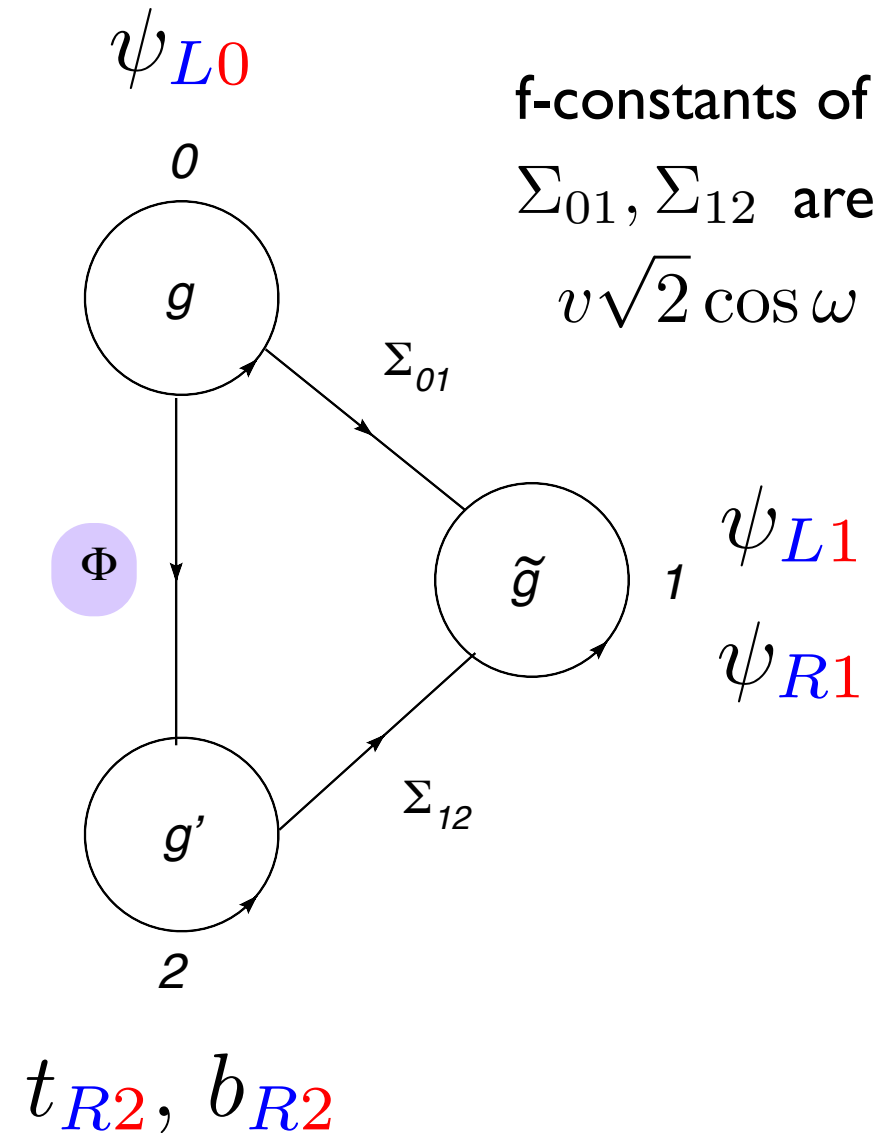
## Gauge boson spectrum:

photon, Z, Z', W, W'  
(as in 3-site, BESS or HLS)

## Fermion spectrum:

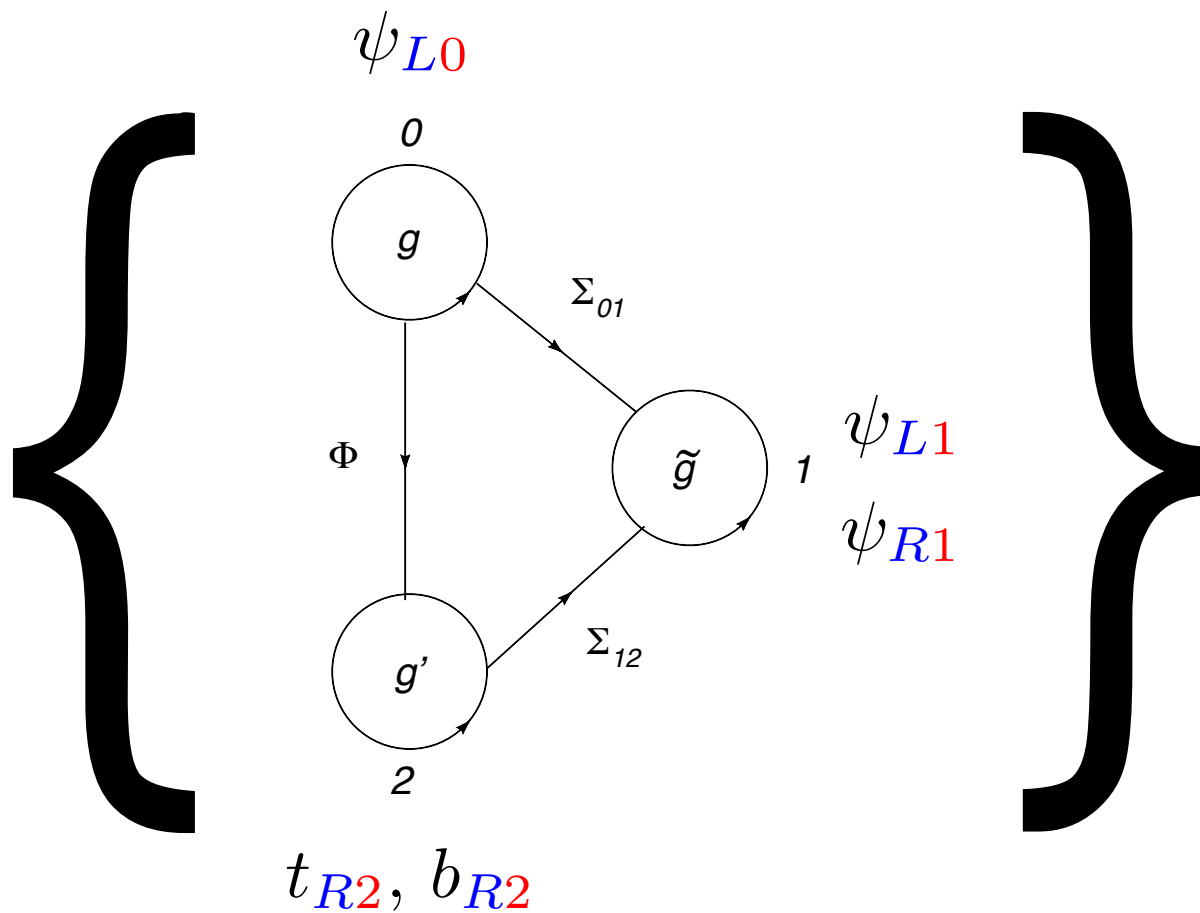
t, T, b, B; similar for light quarks & leptons

only top couples to  $\Phi$



# TRIANGLE MOOSE AND TOPCOLOR-ASSISTED TC

**Topcolor  
sector**



**(E)TC  
sector**

# KEY MASS TERMS

**Top quark:**  $-\lambda_t \bar{\psi}_{L0} \Phi t_R$

**Top-pions:**  $4\pi\kappa v^3 \text{Tr} \left( \Phi \Sigma_{01} \Sigma_{12}^\dagger \right)$

**All fermions (including top) :**

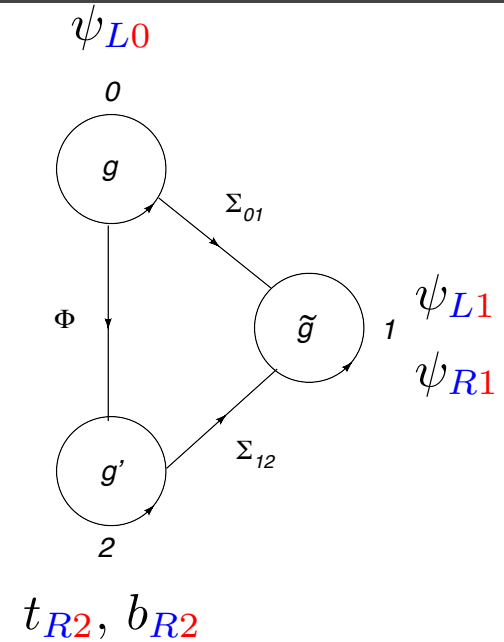
$$M_D \left[ \epsilon_L \bar{\psi}_{L0} \Sigma_{01} \psi_{R1} + \bar{\psi}_{R1} \psi_{L1} + \bar{\psi}_{L1} \Sigma_{12} \begin{pmatrix} \epsilon_{uR} & 0 \\ 0 & \epsilon_{dR} \end{pmatrix} \begin{pmatrix} u_{R2} \\ d_{R2} \end{pmatrix} \right]$$

ideal delocalization says  $\epsilon_L^2 = M_W^2 / 2M_{W'}^2$ ,

light fermion masses are still of the form  $m_f \approx M_D \epsilon_L \epsilon_{fR}$

each light mass value is tied to the value of  $\epsilon_{fR}$

Top mass value is different...



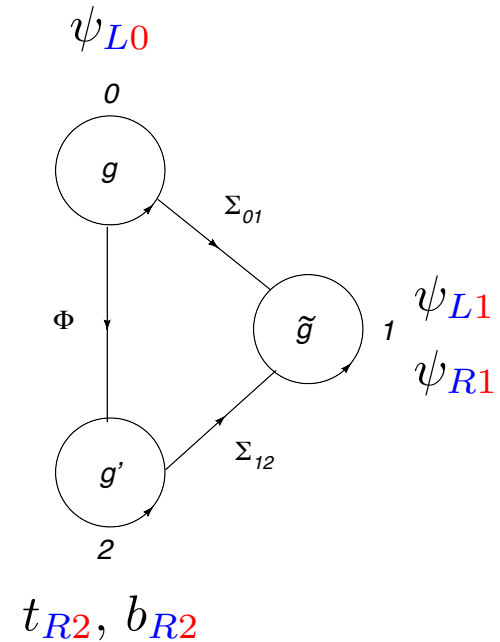
# TOP MASS

Top mass matrix:

$$M_t = M_D \begin{pmatrix} \epsilon_{tL} & a \\ 1 & \epsilon_{tR} \end{pmatrix} \quad a \equiv \frac{\lambda_t v \sin \omega}{M_D}$$

Perturbative diagonalization yields...

$$m_t = \lambda_t v \sin \omega \left[ 1 + \frac{\epsilon_{tL}^2 + \epsilon_{tR}^2 + \frac{2}{a} \epsilon_{tL} \epsilon_{tR}}{2(-1 + a^2)} \right]$$



Top mass now depends **strongly** on  $\lambda_t$ , **weakly** on  $\epsilon_{tR}$

A large top mass no longer conflicts with making  $\epsilon_{tR}$  small to minimize  $\Delta\rho$

$$\Delta\rho = \frac{M_D^2 \epsilon_{tR}^4}{16 \pi^2 v^2}$$

KK fermions are light enough to produce at LHC



# TOP STATES OF INTEREST

## top's KK partner: T

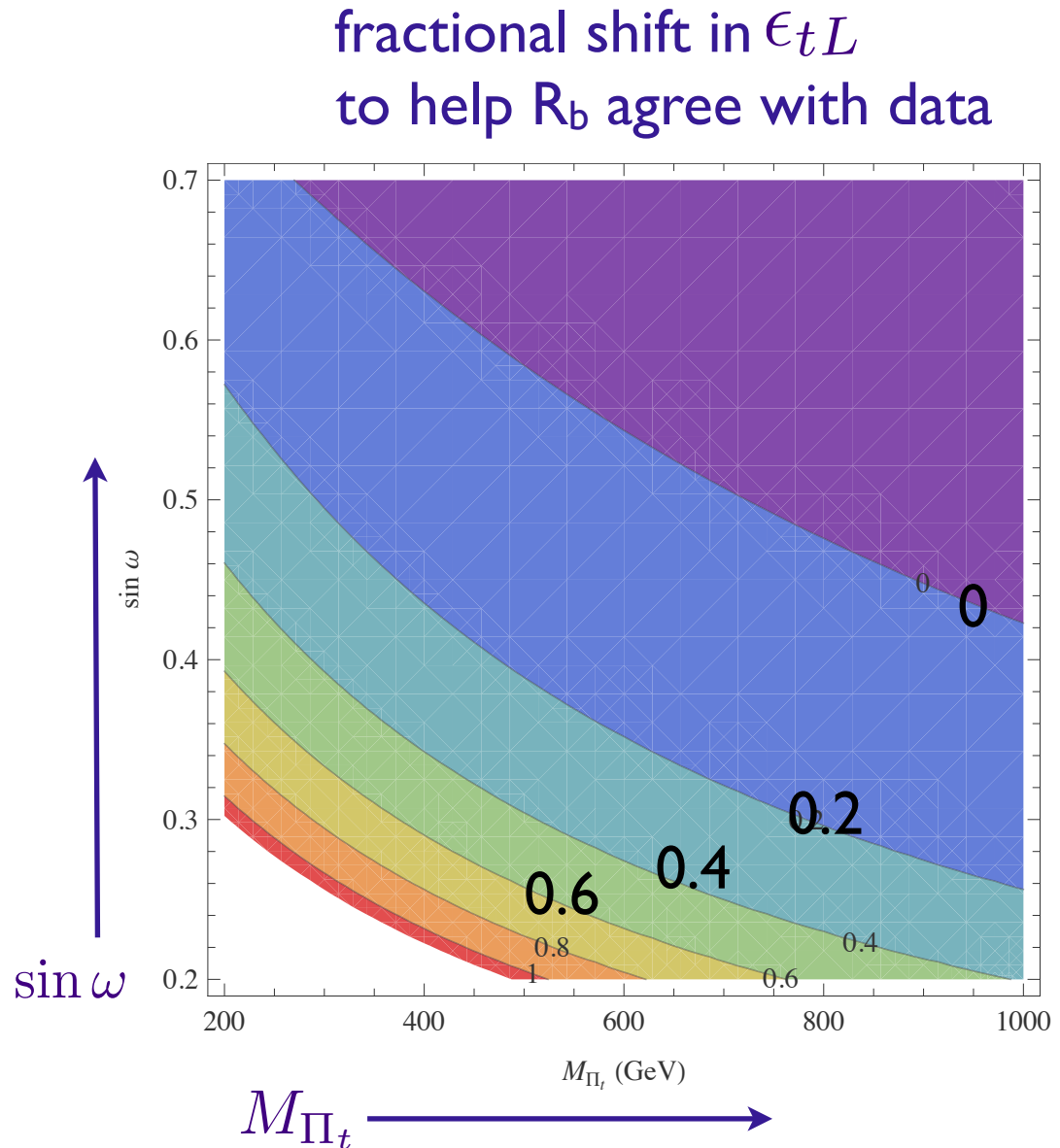
- can be produced at LHC

## top-Higgs state: $H_t$

- production in  $gg \rightarrow H_t$  higher than in SM by factor  $[\sin \omega]^{-1}$

## top-Pion states: $\Pi_t^\pm, \Pi_t^0$

- one-loop  $R_b$  contributions minimized by non-ideal delocalization of  $t_L$  as indicated in plot at right:



# WHAT THE LHC CAN SEE

## W' searches:

Belyaev, et al., arXiv:0708.2588 [hep-ph]

## KK quarks:

Chivukula, Christensen, Coleppa, Simmons  
arXiv:0906.5667 [hep-ph]

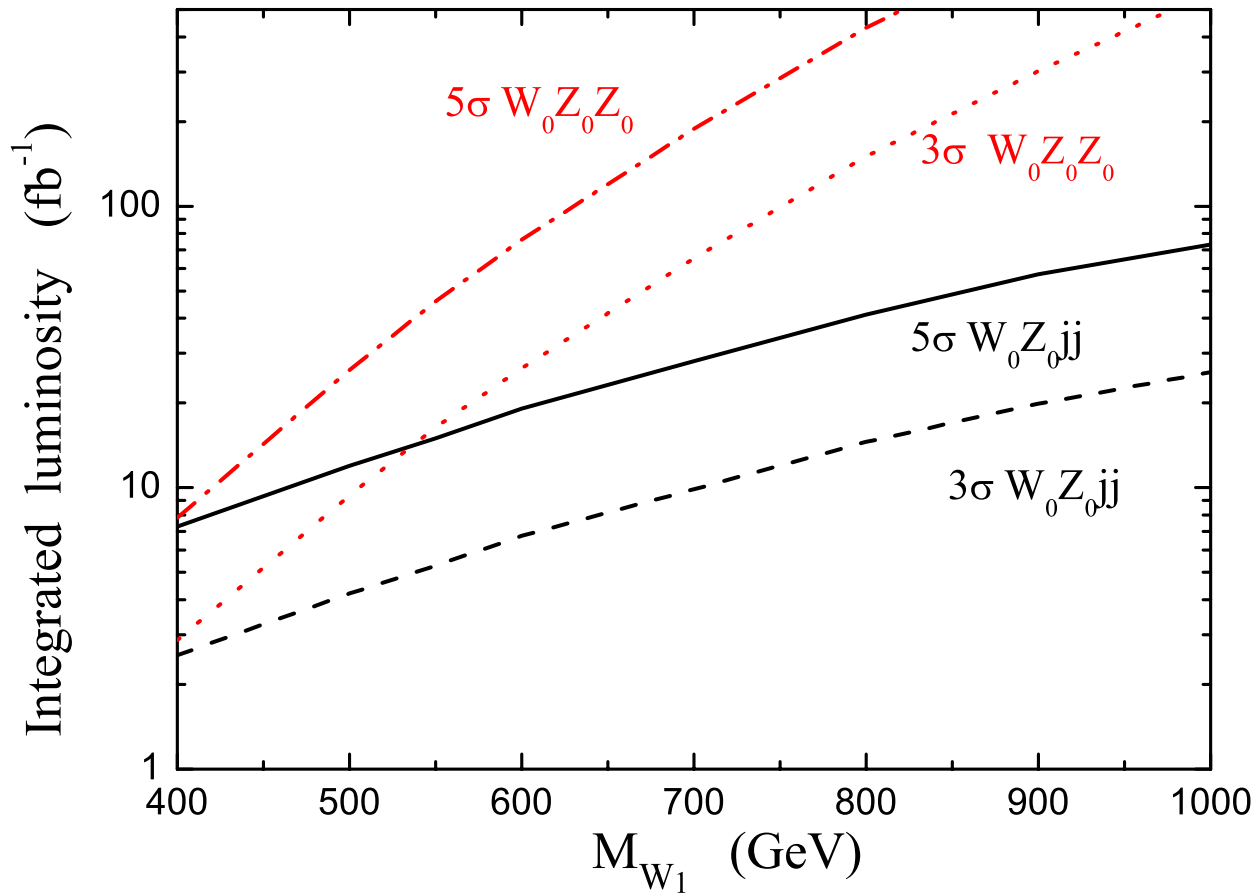
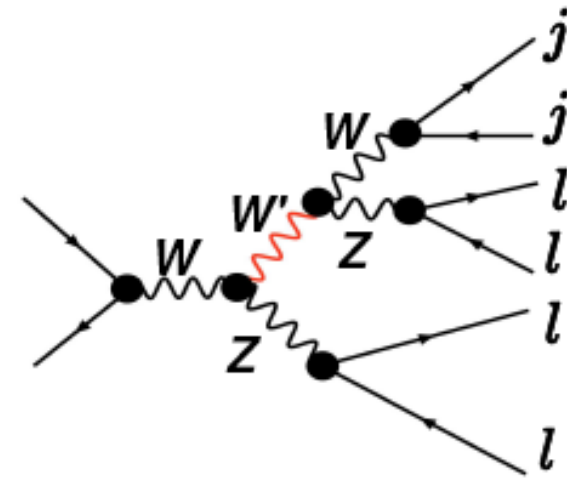
## KK top quark, top-Higgs, and top-Pions

Chivukula, Coleppa, Logan, Martin, Simmons  
arXiv:1101.6023 [hep-ph]

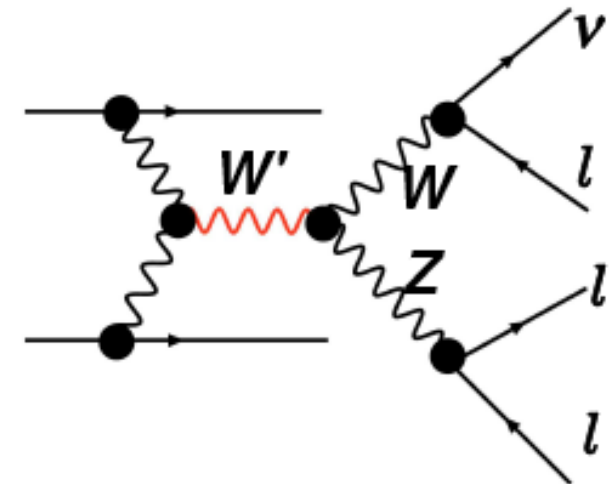
# LHC POTENTIAL FOR FINDING THE $W'$

Integrated luminosity  
needed for 14 TeV  
LHC discovery of  $W'$

Associated  
Production

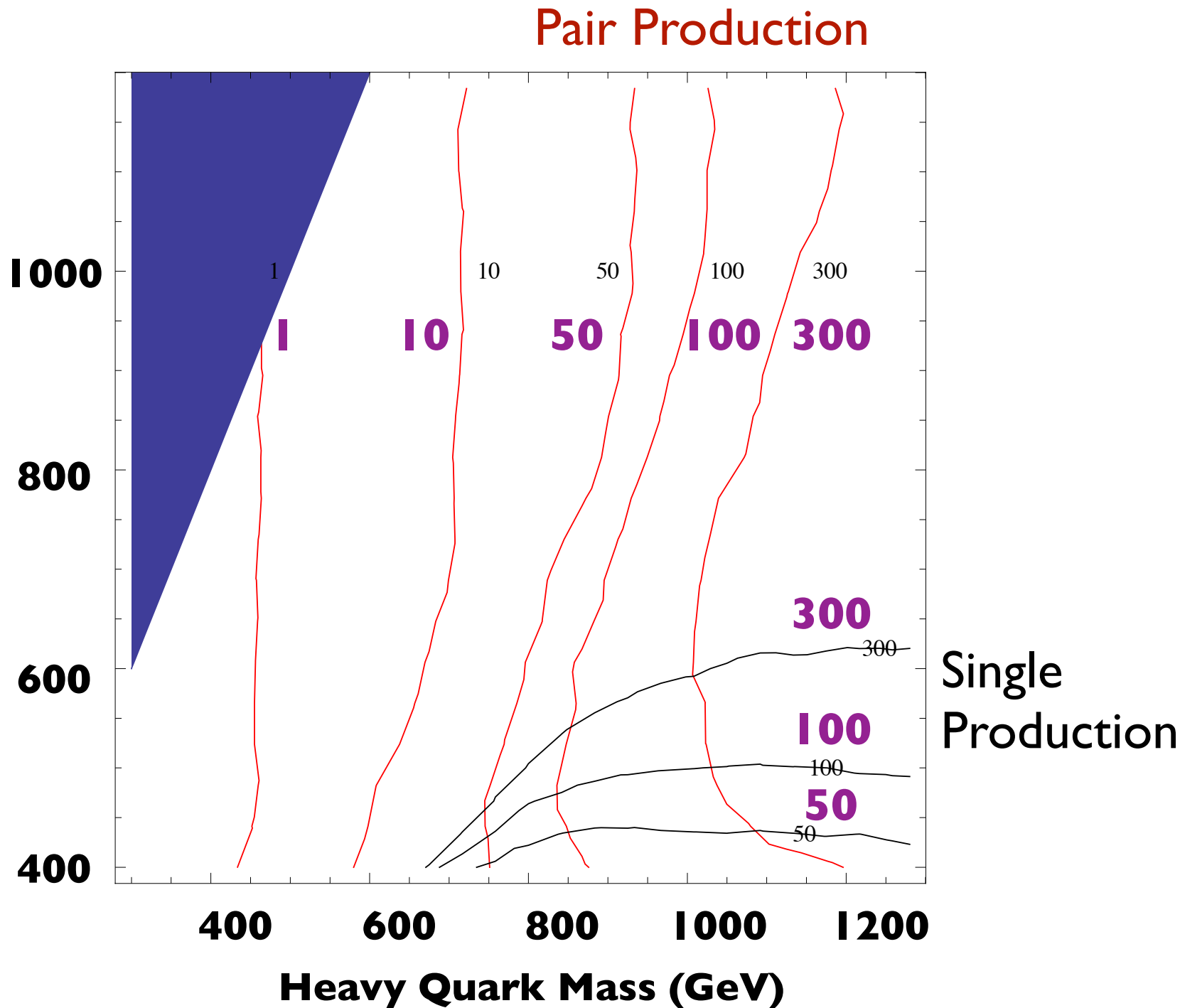


Vector Boson  
Fusion



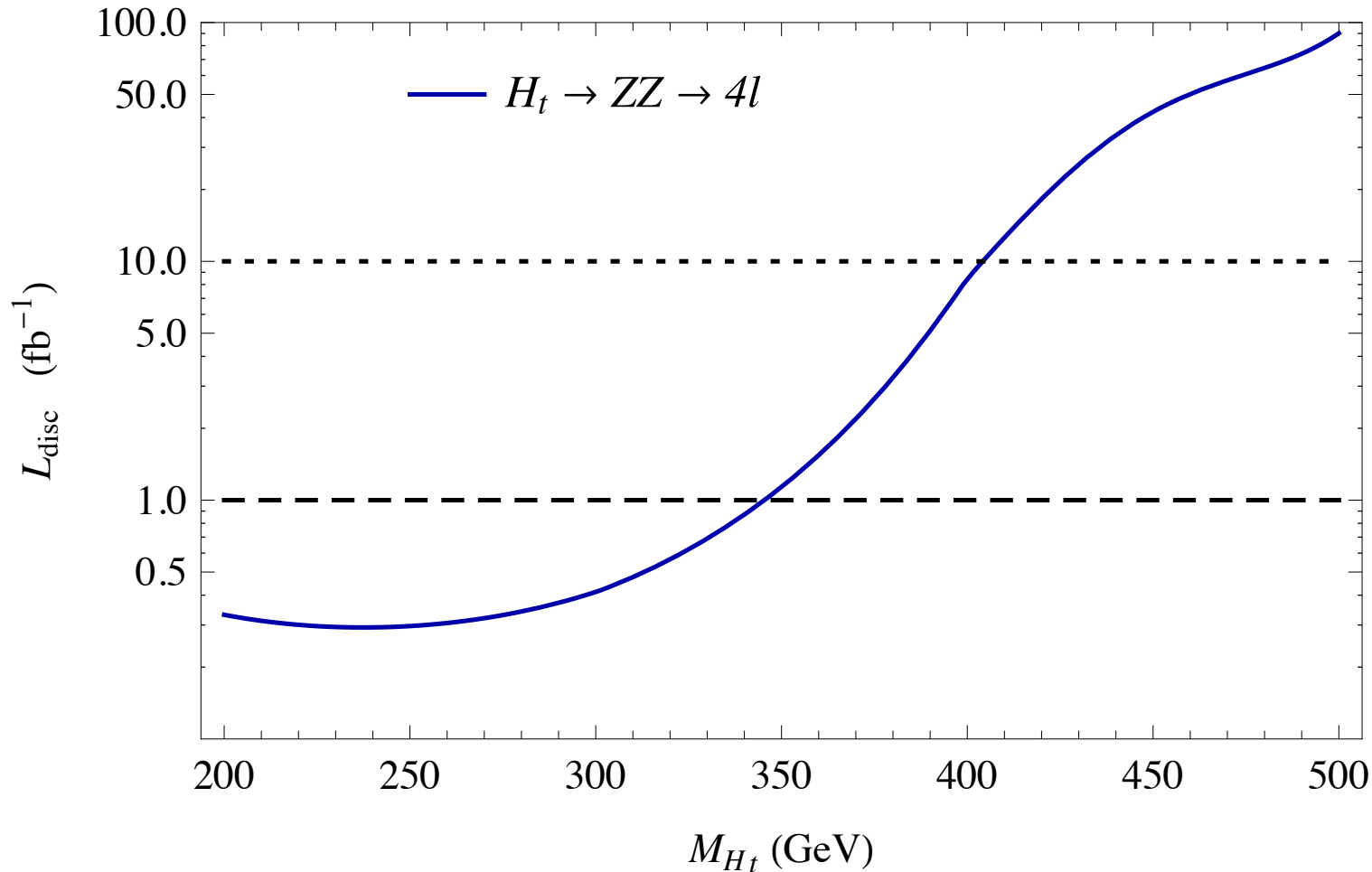
# LHC DETECTION OF KK QUARKS

Integrated Luminosity ( $\text{fb}^{-1}$ ) for  $5\sigma$  discovery of KK quarks (U,D,C,S) in LHC at 14 TeV



# TOP SECTOR AT LHC: $H_t$

Integrated luminosity needed for Top-Higgs discovery in  $H_t \rightarrow ZZ$  at 14 TeV LHC is encouragingly low:

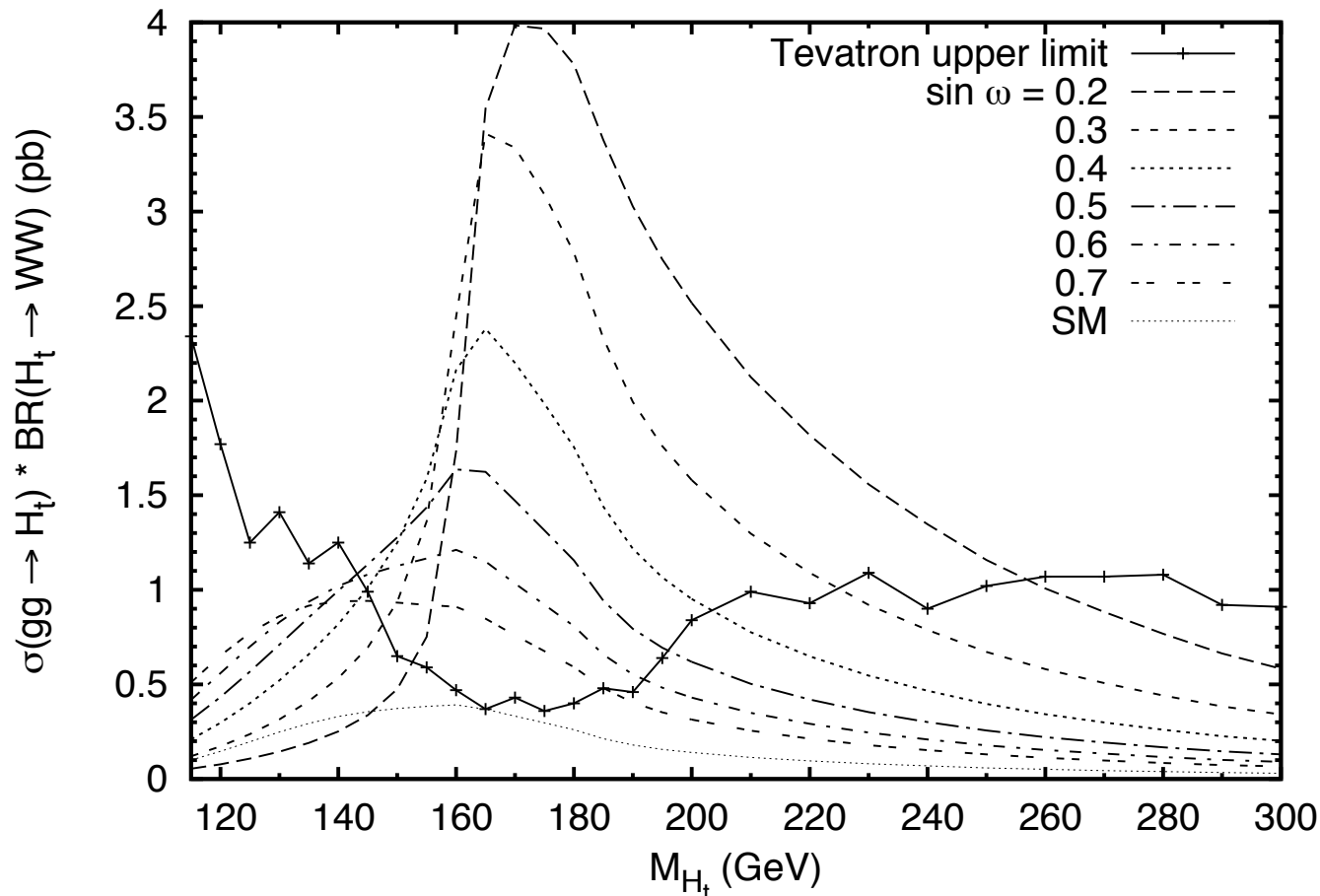


For heavier  $H_t$ , the most promising mode is  $H_t \rightarrow W \Pi_t$

# TOP SECTOR AT LHC: $H_T$

A top-Higgs of moderate mass would be visible in di-bosons due to enhancement of  $gg \rightarrow H_t$  production by  $[\sin\omega]^{-1}$ .

E.g., see enhanced production relative to Tevatron\* limit:



\*T. Aaltonen et al. [CDF and D0 Collaborations], arXiv:1005.3216

# TOP SECTOR AT LHC

## Sample strategy to find states in the top sector and confirm they belong to this kind of Higgsless model:

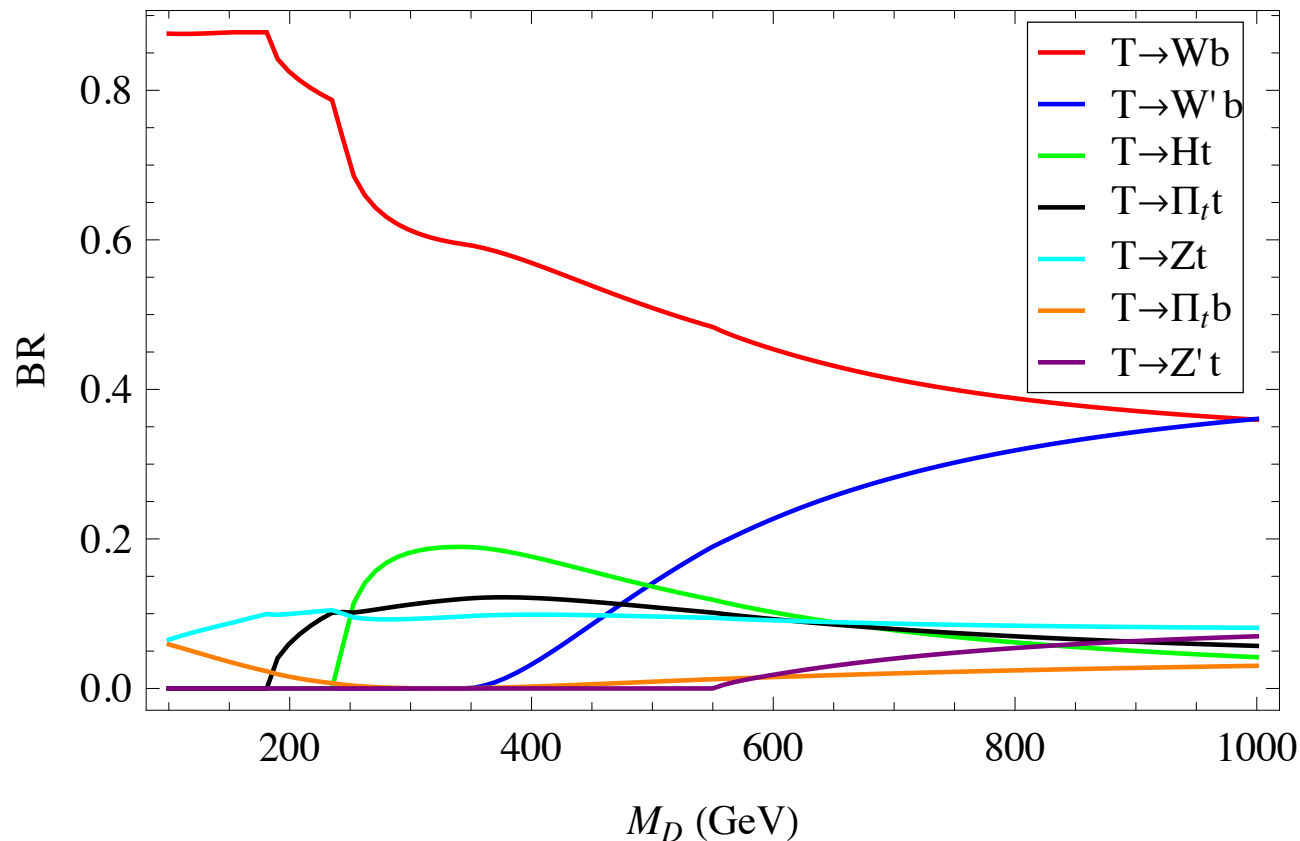
1. With initial LHC data, find  $H_t$  in  $H_t \rightarrow WW, ZZ$ ; higher-than-SM production rate will indicate that it is exotic
2. As integrated luminosity grows, find top quark's KK partner  $T$  via its dominant decay to  $T \rightarrow Wb$
3. Confirm the  $T \rightarrow H_t t$  decay; this shows  $H_t$  is strongly coupled to the top sector as well as the EW sector
4. Discover  $\Pi_t$  in  $pp \rightarrow t \Pi_t^\pm$ ; this establishes the top-pion's strong link to the top sector
5. Confirm  $\Pi_t$  in  $pp \rightarrow H_t \Pi_t^\pm$ ; this links the top-pion to the EW sector as well

# TOP SECTOR AT LHC: T

Top's KK partner, T, will be most visible in  $T \rightarrow Wb$ .

Analysis for other KK quark partners (assuming  $W \rightarrow l\nu$ ) still roughly applies; the channel with one hadronically-decaying W should offer larger signal and full reconstruction of T.

The  $T \rightarrow H_t t$  decays will also be helpful.

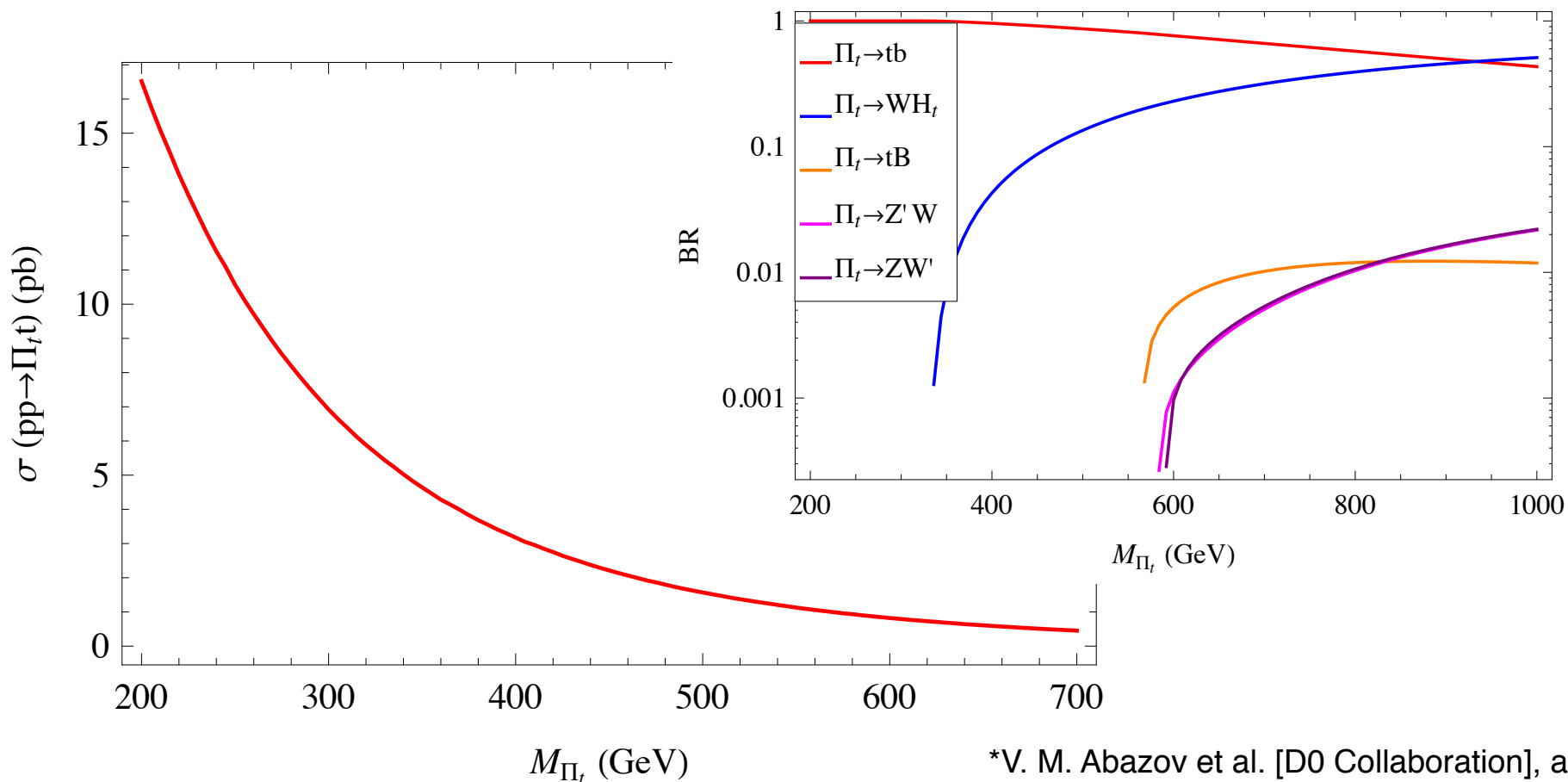
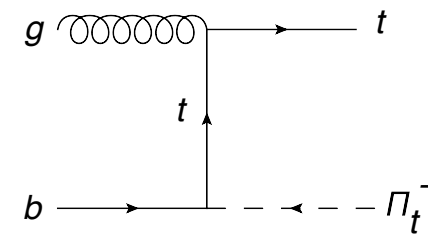
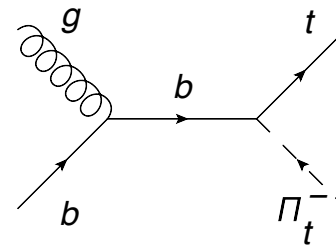




# TOP SECTOR AT LHC: $\Pi_T$

FNAL limits\* on  $t \rightarrow H^\pm b$  imply  $\Pi_t$  is heavier than  $t$ , so the main production process is  $pp \rightarrow t \Pi_t \rightarrow t t b$ .

CMS studies\*\* of  $H^\pm \rightarrow t b$  imply 30  $\text{fb}^{-1}$  of data can find a  $\Pi_t$  up to 400 GeV



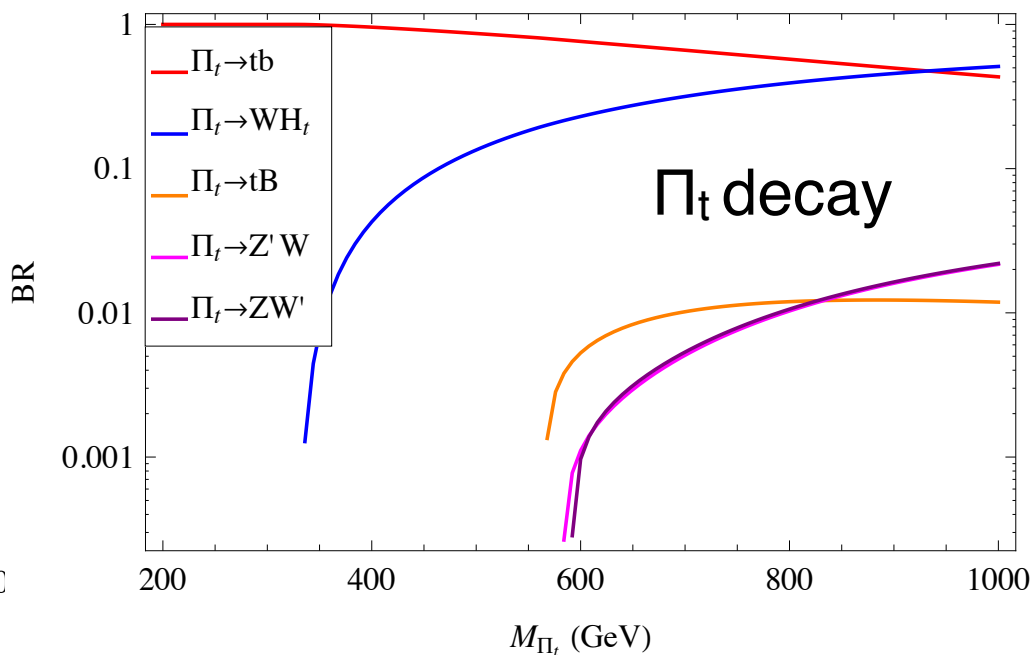
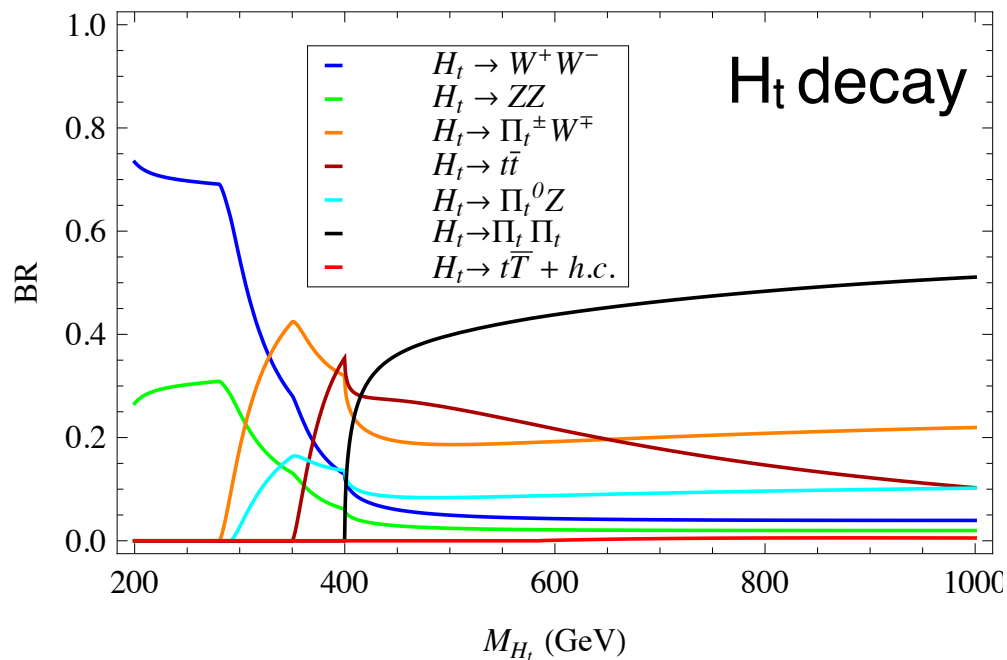
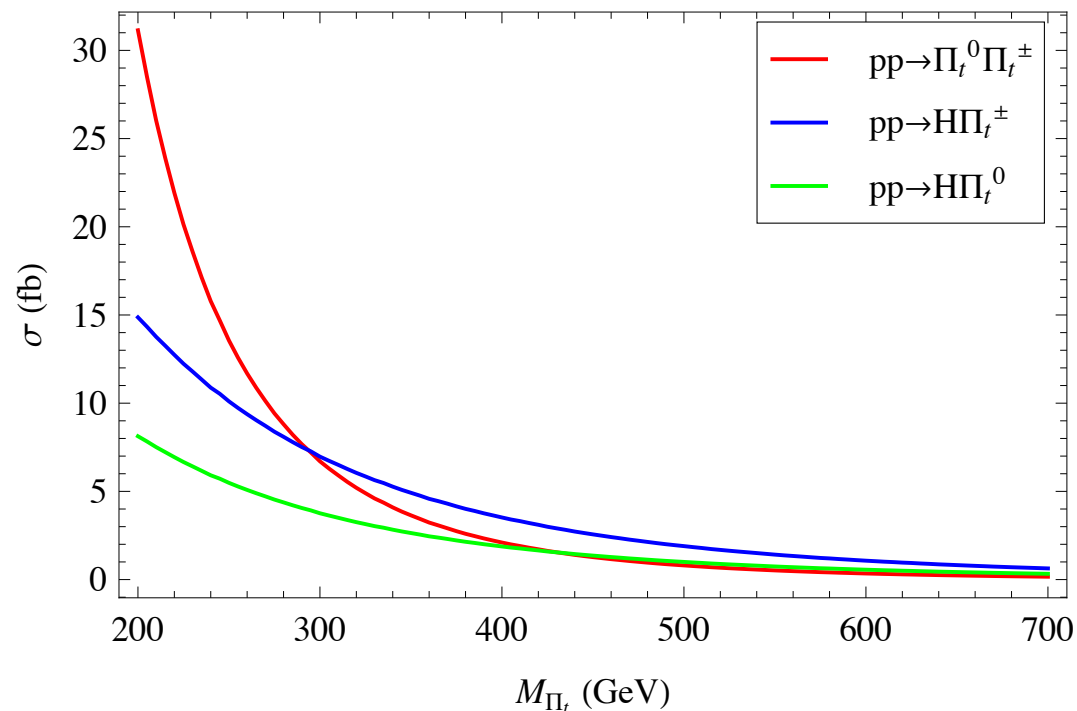
Note:  $\Pi_t$  can also decay to  $W H_t$ .

\*V. M. Abazov et al. [D0 Collaboration], arXiv:0908.1811  
 \*\*Lowette, D'Hondt, Vanlaer CERN-CMS-NOTE-2006-109

# TOP SECTOR AT LHC: $\Pi_T$

Associated production  $pp \rightarrow W^* \rightarrow H_t \Pi_t$  can provide useful confirmation of the relationship between  $H_t$  and  $\Pi_t$ .

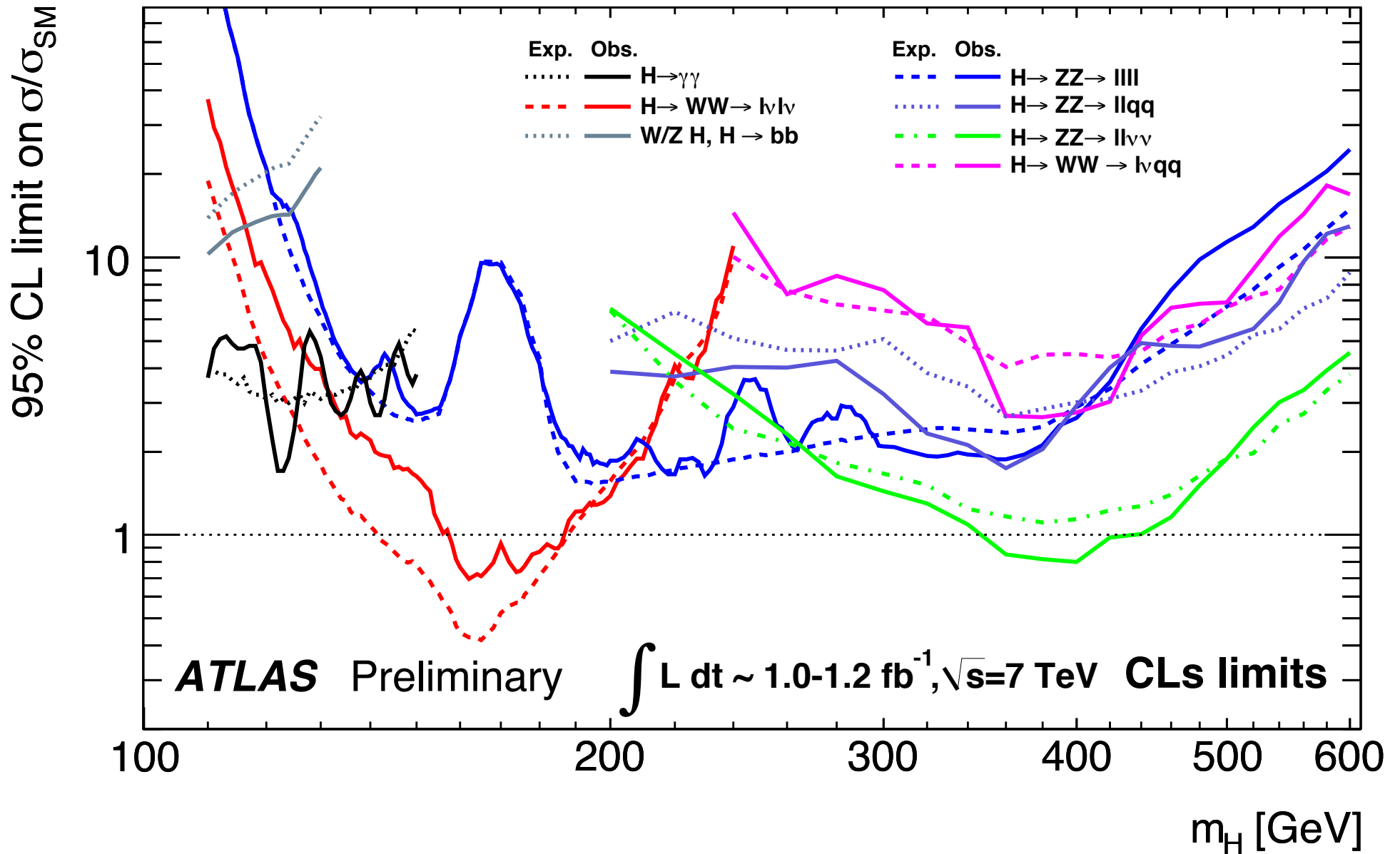
Single production followed by either  $H_t \rightarrow W\Pi_t$  or  $\Pi_t \rightarrow WH_t$  would be similarly informative.



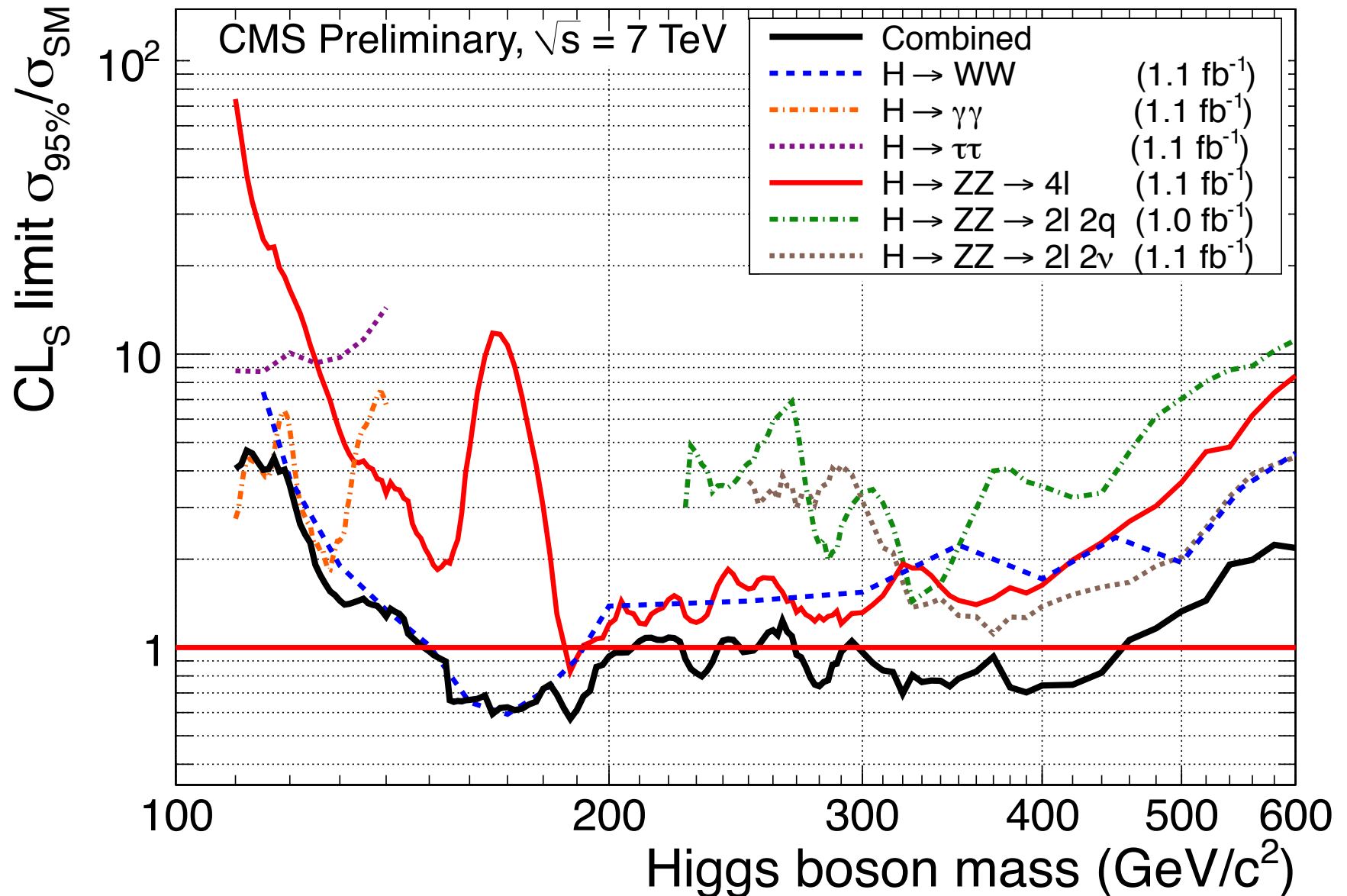
# WHAT THE LHC HAS (NOT) SEEN

Chivukula, Coleppa, Logan, Martin, Simmons  
arXiv: 1108.4000 [hep-ph]

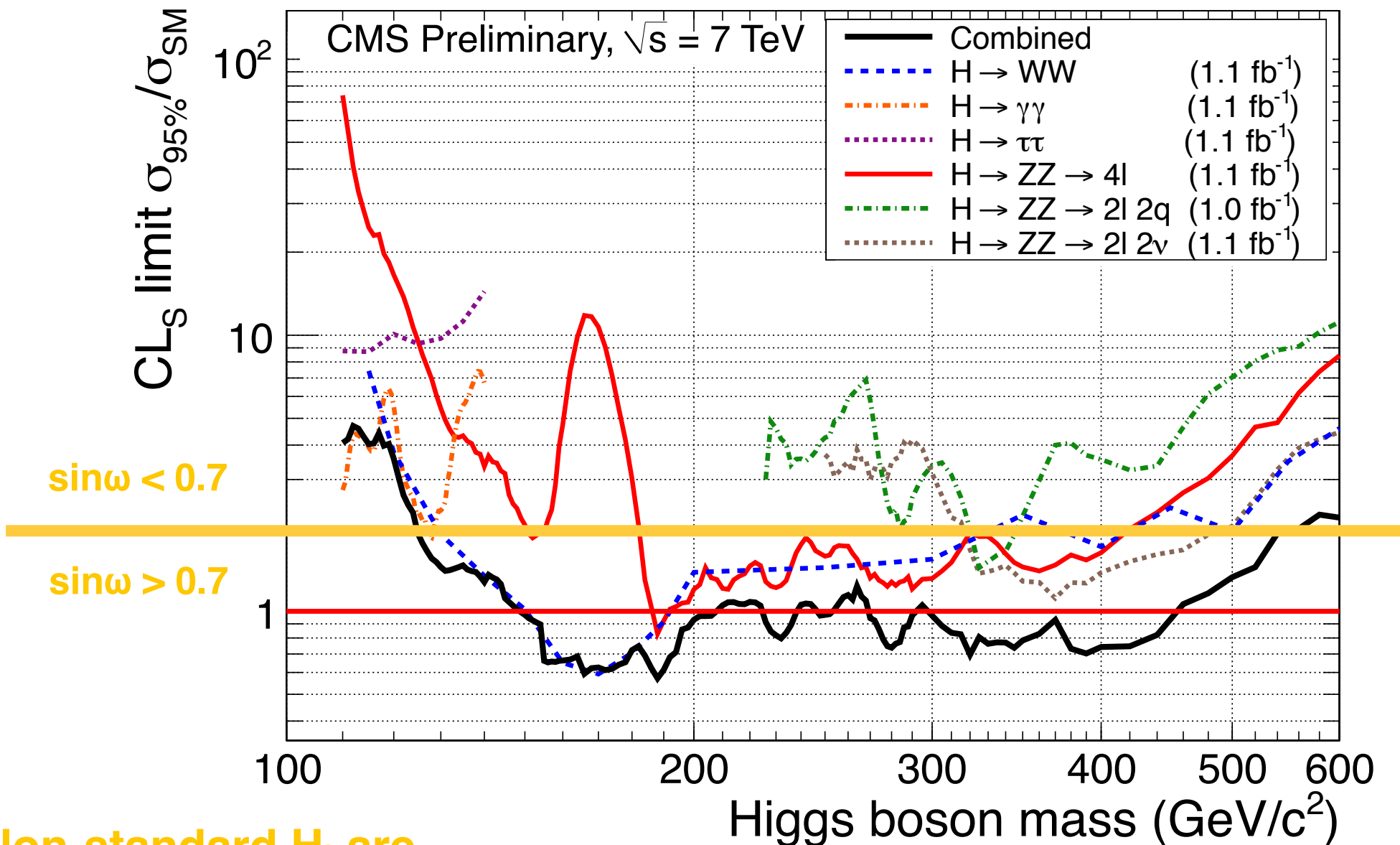
# NEW ATLAS LIMITS ON HIGGS PRODUCTION



# NEW CMS LIMITS ON HIGGS PRODUCTION

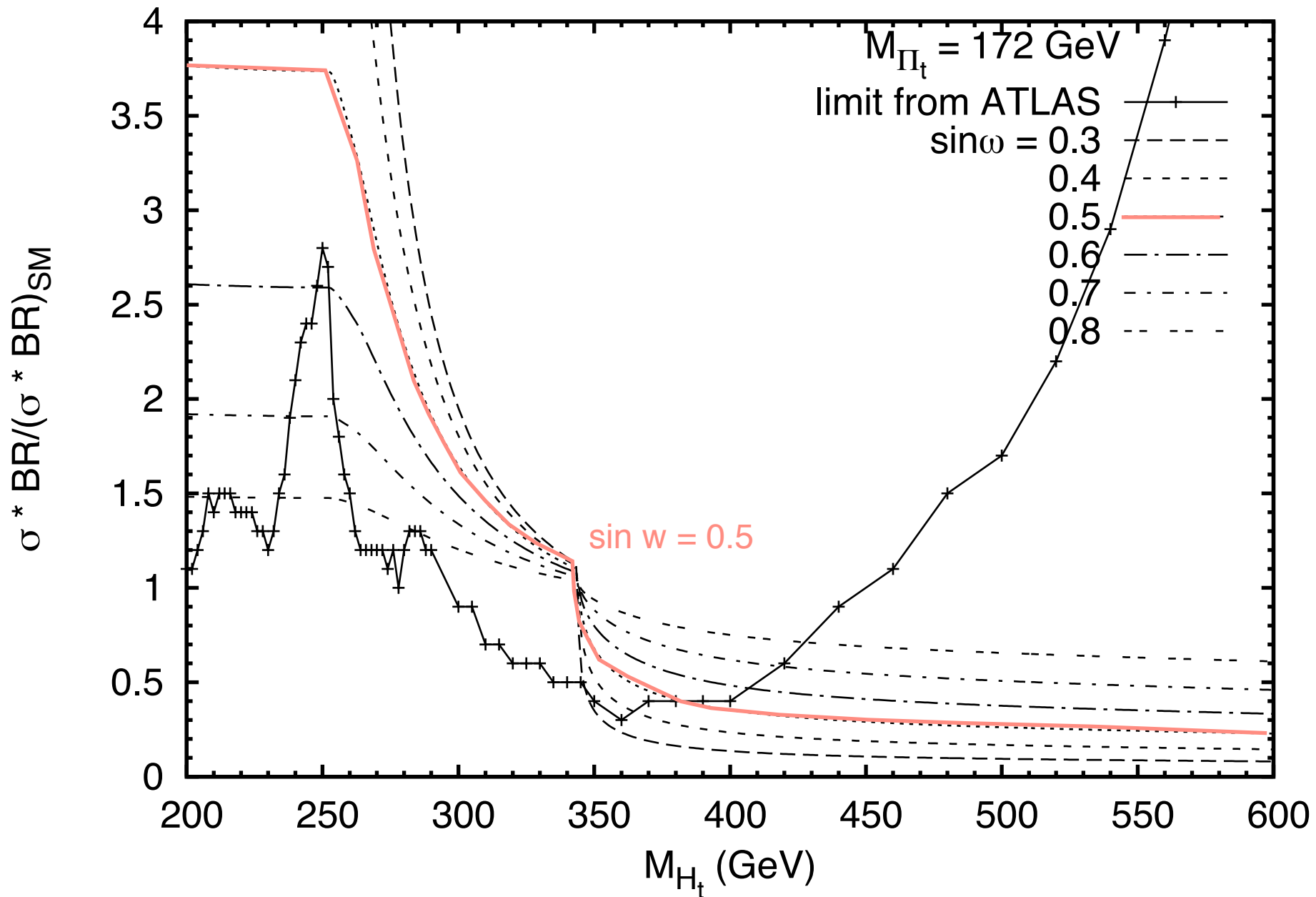


# NEW CMS LIMITS ON HIGGS PRODUCTION



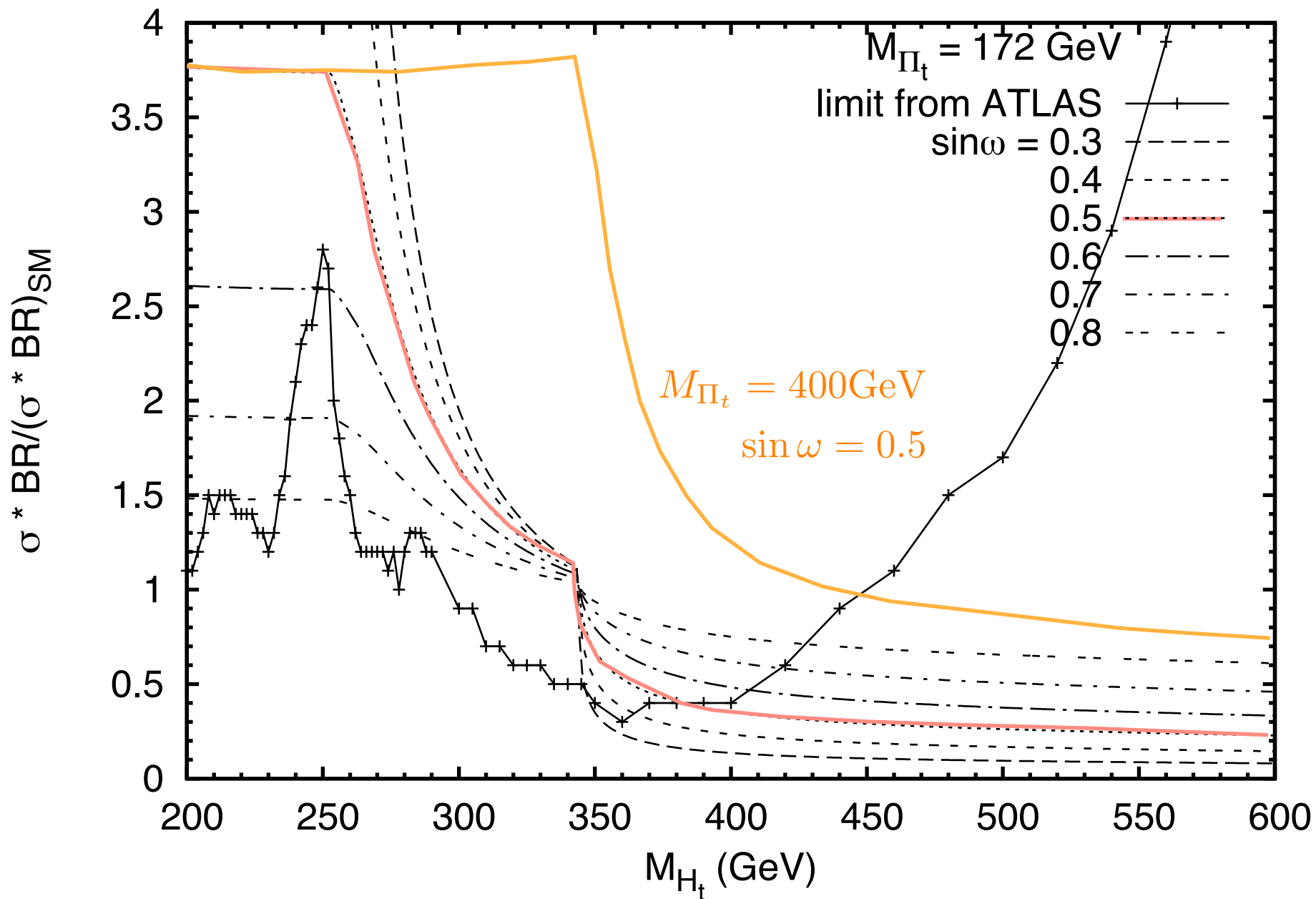
Non-standard  $H_t$  are tightly constrained

# ATLAS vs $H_T$ (LIGHT TOP-PION)



Preliminary

# ATLAS vs $H_T$ (HEAVIER TOP-PION)



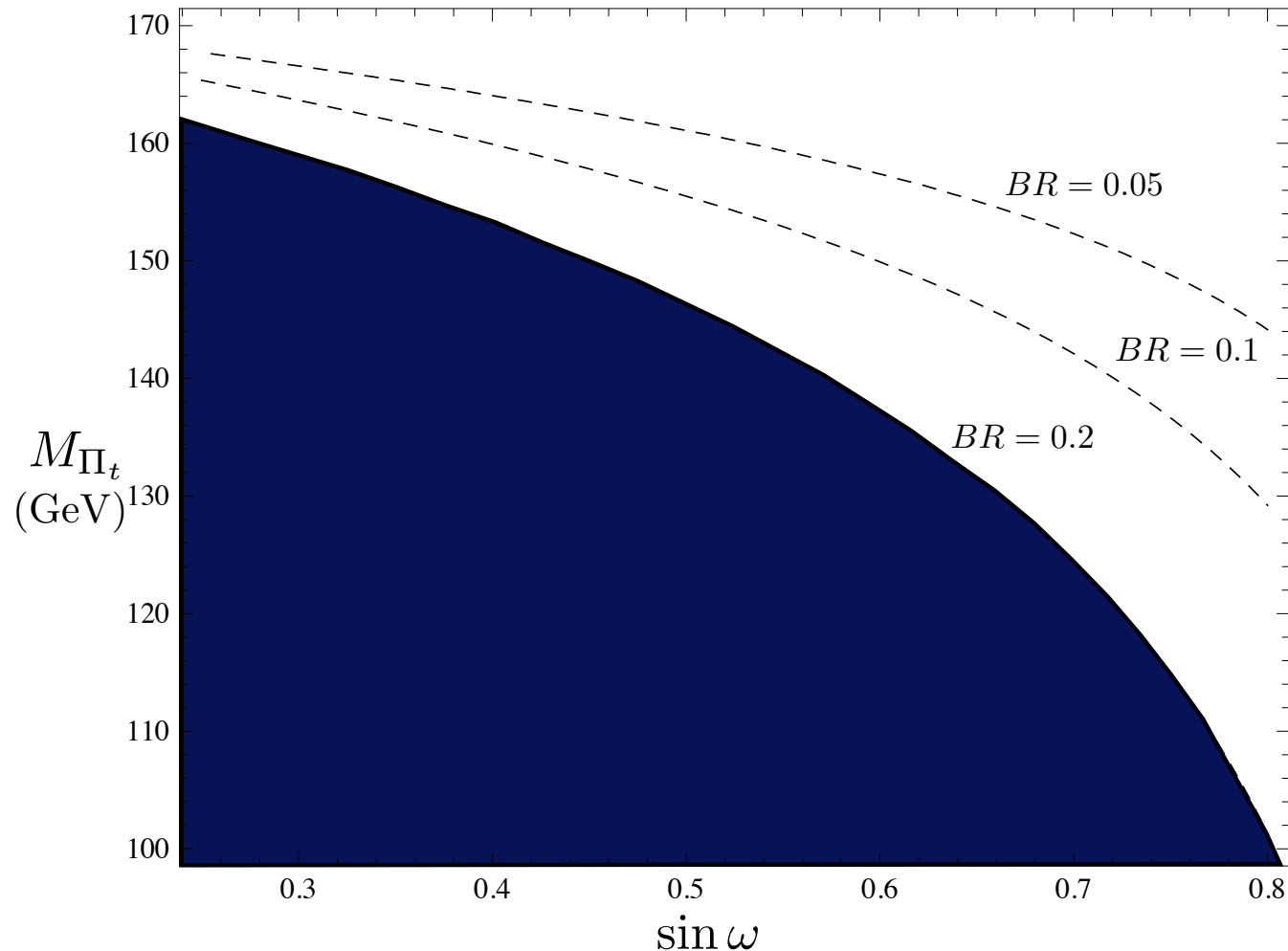
Preliminary



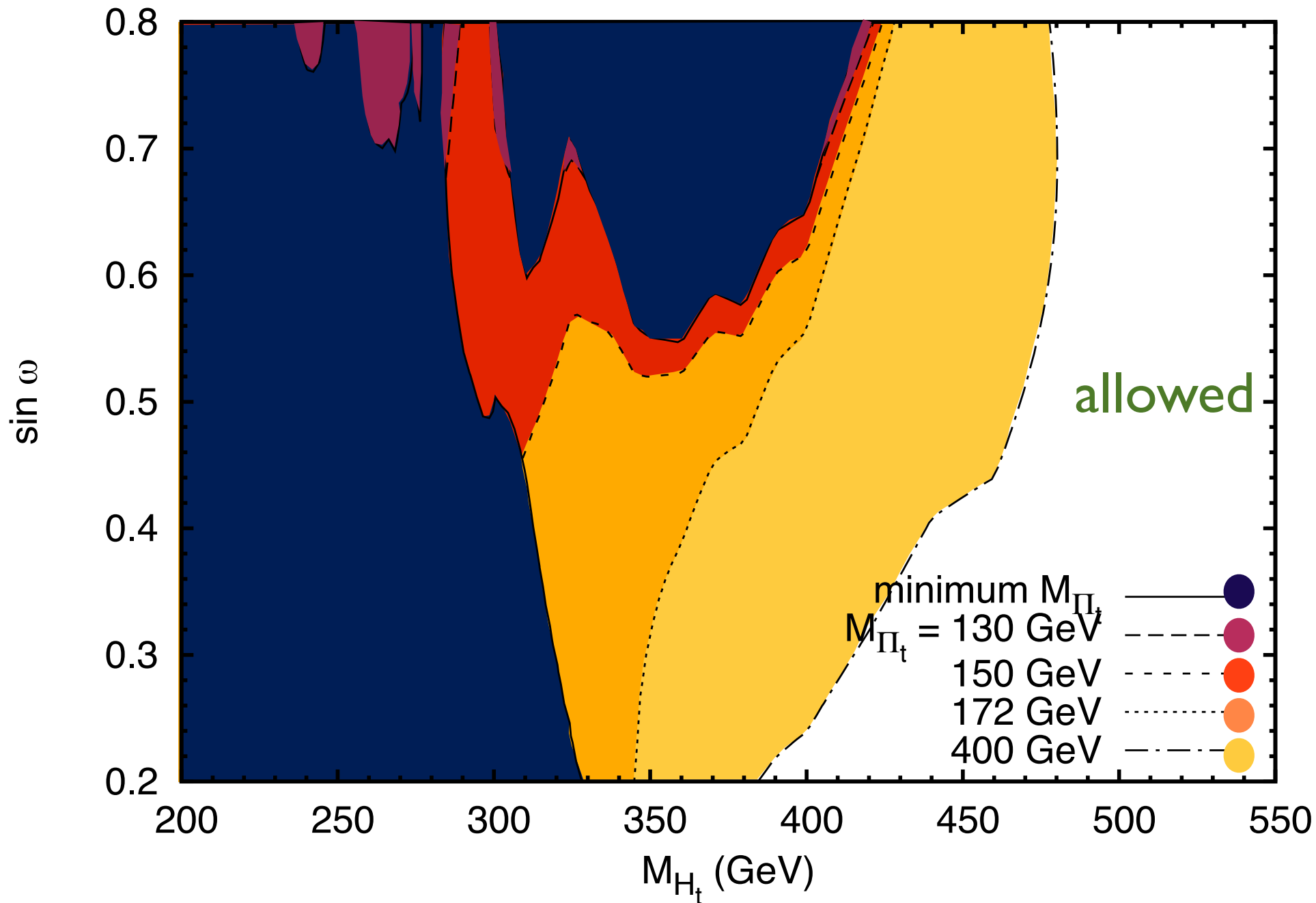
# IMPACT OF TOP-PION MASS

Tevatron bounds on top decays to charged Higgs bosons imply that  $BR(t \rightarrow \Pi_t^+ b) \leq 0.2$  and exclude the dark-blue region below:

top-pion  
mass  
(GeV)



# LHC LIMITS ON TOP-HIGGS ( $H_T$ )



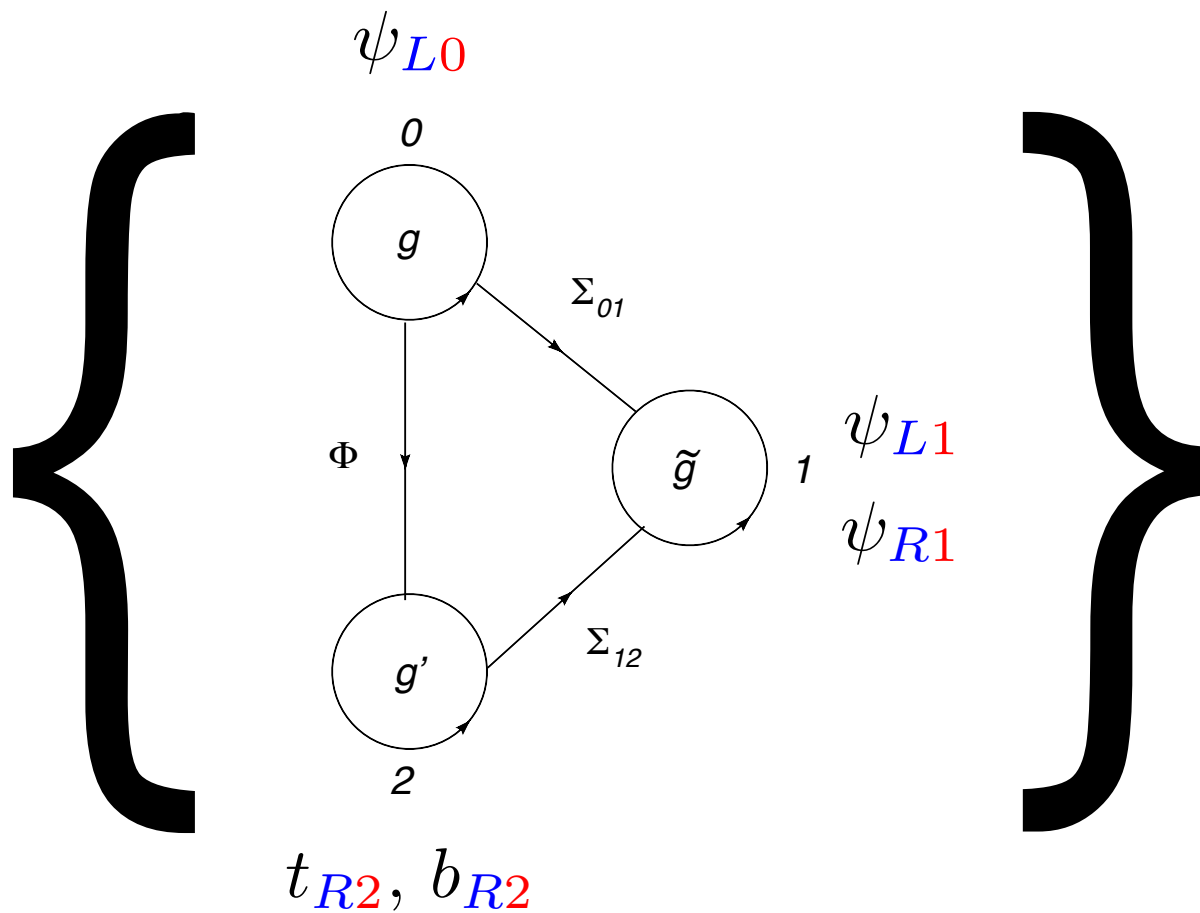
# IMPLICATIONS OF WHAT THE LHC HAS (NOT) SEEN

LHC limits on the top-Higgs in models with strong  
top quark dynamics

Chivukula, Coleppa, Logan, Martin, Simmons  
arXiv:1108.4000 [hep-ph]

# TRIANGLE MOOSE AND TOPCOLOR-ASSISTED TC

**Topcolor  
sector**



**(E)TC  
sector**

# TC2 DYNAMICS

Consider the top triangle moose as a deconstructed version of topcolor-assisted technicolor (TC2):

- A combination of topcolor dynamics and ETC give rise to the top quark mass:  $m_t \approx m_t^{dyn} + m_t^{ETC}$  where the latter is only 0.5% - 10% of the total.

- The Pagels-Stokar relation  $f_{\Pi_t}^2 = \frac{N_c}{8\pi^2} m_{t,dyn}^2 \ln \left( \frac{\Lambda^2}{m_{t,dyn}^2} \right)$  relates  $\sin \omega \equiv f_{\Pi_t}/v$  to the top mass

- The top-pion mass  $M_{\Pi_t}^2 = \frac{N_c}{4\pi^2} m_{t,ETC} m_{t,dyn} \left( \frac{\Lambda^2}{f_{\Pi_t}^2} \right)^\gamma$  should exceed the top mass to respect bounds on  $t \rightarrow bH^+$

- The dynamics imply  $M_{H_t} \lesssim 2m_{t,dyn}$

# TC2 PARAMETER RANGE AT LHC

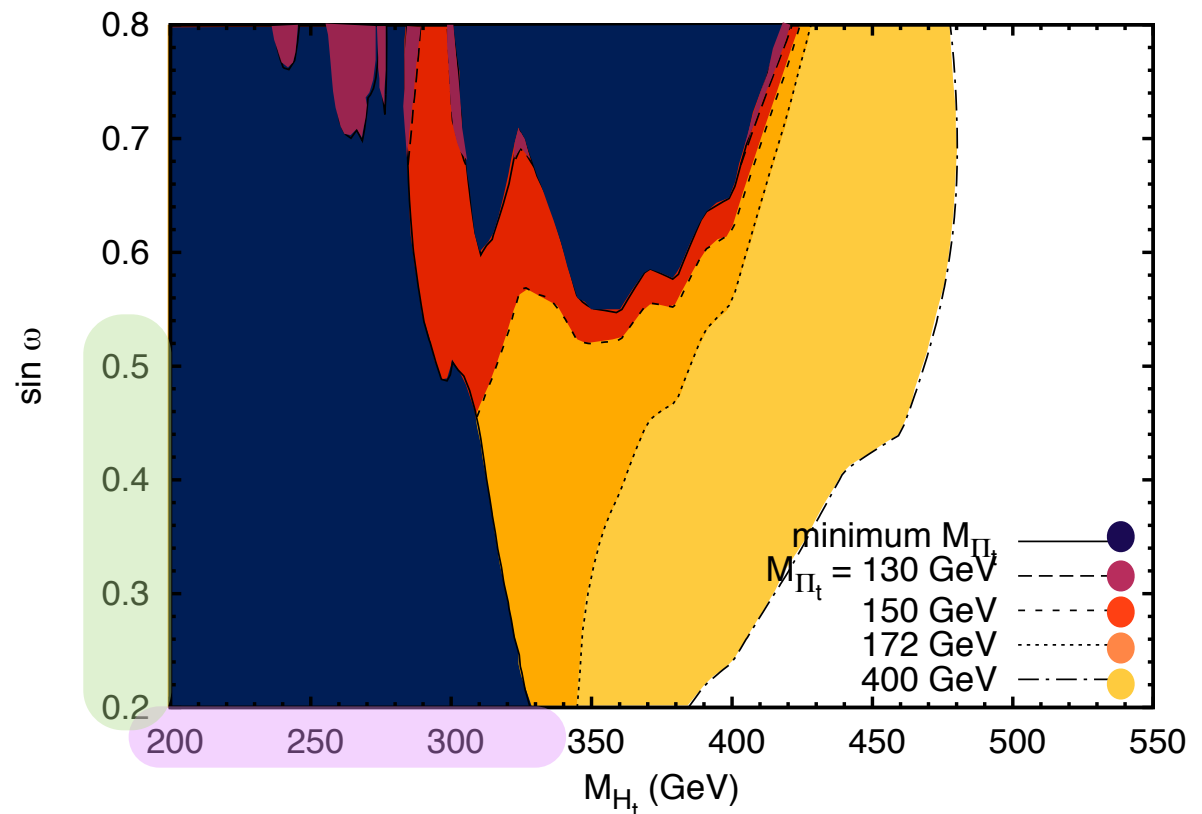
Considering the top triangle moose as a low-energy effective theory for TC2, one would then expect the model parameters to lie in the following ranges:

$$185 \text{ GeV} < M_{H_t} < 340 \text{ GeV}$$

$$172 \text{ GeV} < M_{\Pi_t} < M_{H_t}$$

$$0.2 < \sin \omega < 0.5$$

The new LHC data appears to exclude precisely this region.



# CONCLUSIONS

# CONCLUSIONS AND NEXT STEPS

- Avoiding large weak isospin violation is a challenge for dynamical models of EWSB and fermion masses.
- The **top triangle moose** is a useful effective theory for studying a range of models where a topcolor-like mechanism generates the top quark mass (such as TC2).
- In this scenario, the heavy partner (KK) quarks are light enough to produce at LHC and the top sector includes **T,  $H_t$  and  $\Pi_t$  states**. Interplay among these states would signal that top dynamics plays a role in EWSB.
- Recent **LHC data on  $H \rightarrow WW, ZZ$  exclude the most favored TC2 parameter space**. New models with heavier  $H_t$  (e.g. top-seesaw assisted TC) are required.





# WHAT THE LHC CAN SEE (DETAIL)

## W' searches:

Belyaev, et al., arXiv:0708.2588

## KK quarks:

Chivukula, Christensen, Coleppa, Simmons arXiv:0906.5667

## KK top quark, top-Higgs, and top-Pions

Chivukula, Coleppa, Logan, Martin, Simmons arXiv:1101.6023

## related work:

3-site: Ohl, Speckner arXiv:0809.0023

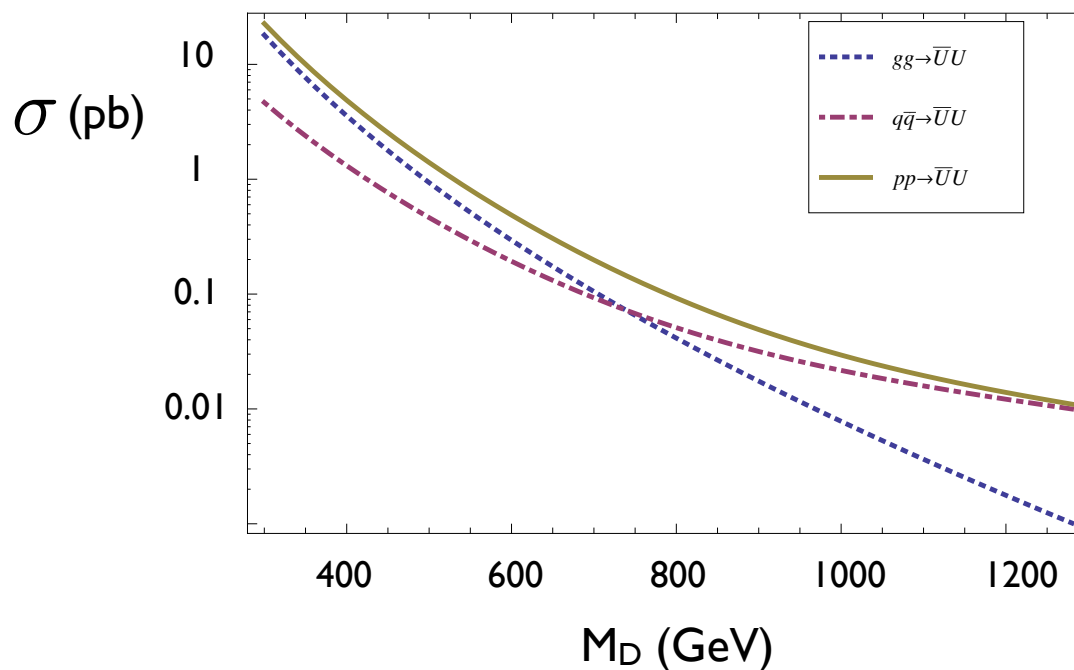
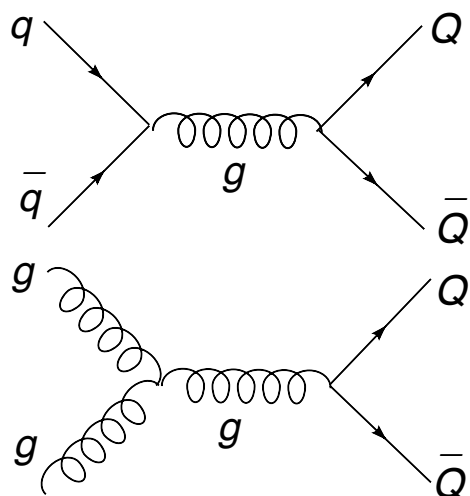
4-site: Hirn, Martin, Sanz arXiv:0712.3783

4-site: Accomando et al. arXiv:0807.5051

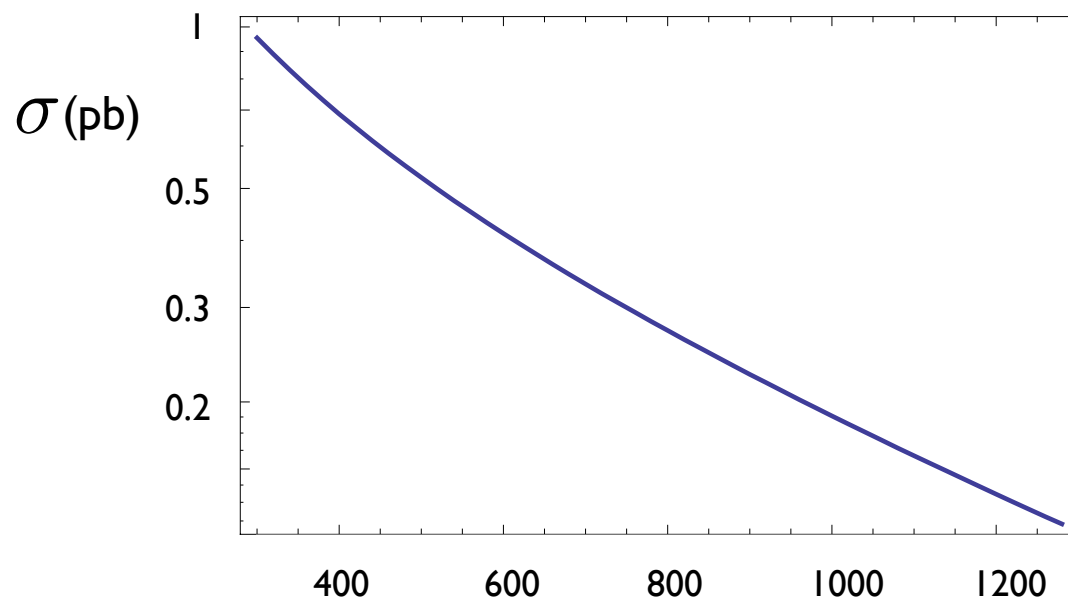
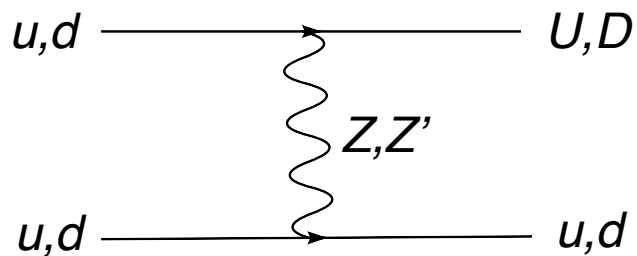
# KK QUARK PRODUCTION AT LHC

(TRIANGLE MOOSE MODEL)

## Pair Production

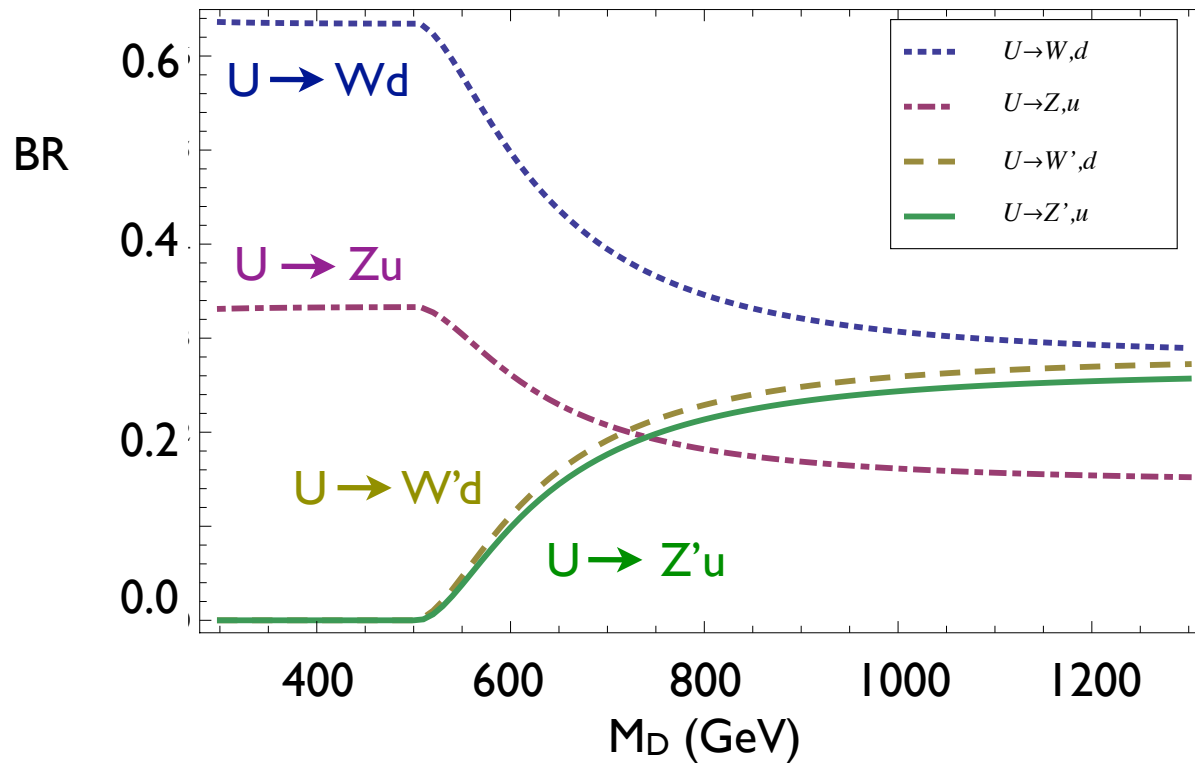


## Single Production



# KK QUARK DECAY AND DETECTION

## KK fermion decay modes



QQ signature:  $pp \rightarrow Q\bar{Q} \rightarrow WZqq \rightarrow \ell\ell\ell jj \cancel{E}_T$

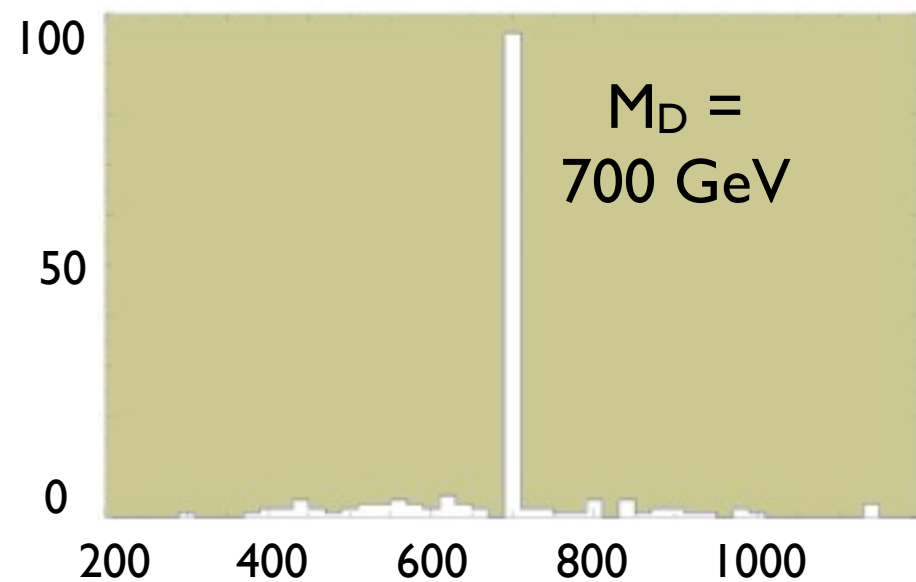
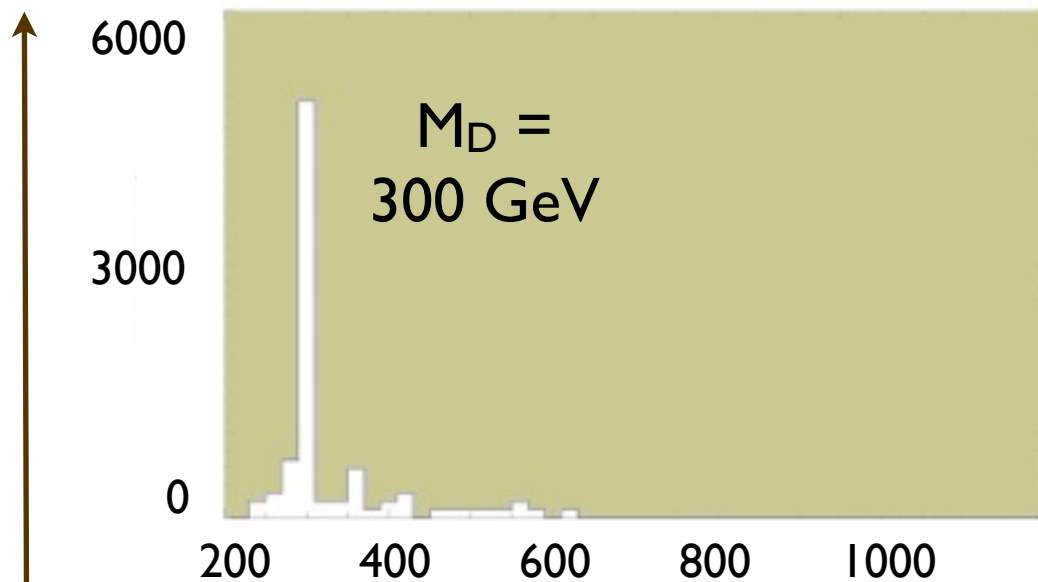
Qq signature:  $pp \rightarrow Qq \rightarrow W'qq \rightarrow WZqq \rightarrow \ell\ell\ell jj \cancel{E}_T$

# KK QUARK PAIR PRODUCTION

With basic identification and separation cuts on jets and leptons, **a hard jet  $p_T$  cut removes nearly all SM background**

Variable	Cut
$p_{Tj}$	$>100$ GeV
$p_{Tl}$	$>15$ GeV
Missing $E_T$	$>15$ GeV
$ \eta_j $	$< 2.5$
$ \eta_l $	$< 2.5$
$\Delta R_{jj}$	$>0.4$
$\Delta R_{jl}$	$>0.4$
$M_{ll}$	$89 \text{ GeV} < M_{ll} < 93 \text{ GeV}$

# events



$M_{jll}$

# KK QUARK SINGLE PRODUCTION

Identification and separation cuts on jets and leptons, a **hard jet  $p_T$  cut, and jet & lepton rapidity cuts control the SM background**

Variable	Cut
$p_{Tj}$ hard	$>200$ GeV
$p_{Tj}$ soft	$>15$ GeV
$p_{Tl}$	$>15$ GeV
Missing $E_T$	$>15$ GeV
$ \eta_j$ hard	$< 2.5$
$ \eta_j$ soft	$2 <  \eta  < 4$
$ \eta_l $	$< 2.5$
$\Delta R_{jj}$	$>0.4$
$\Delta R_{jl}$	$>0.4$

# events

